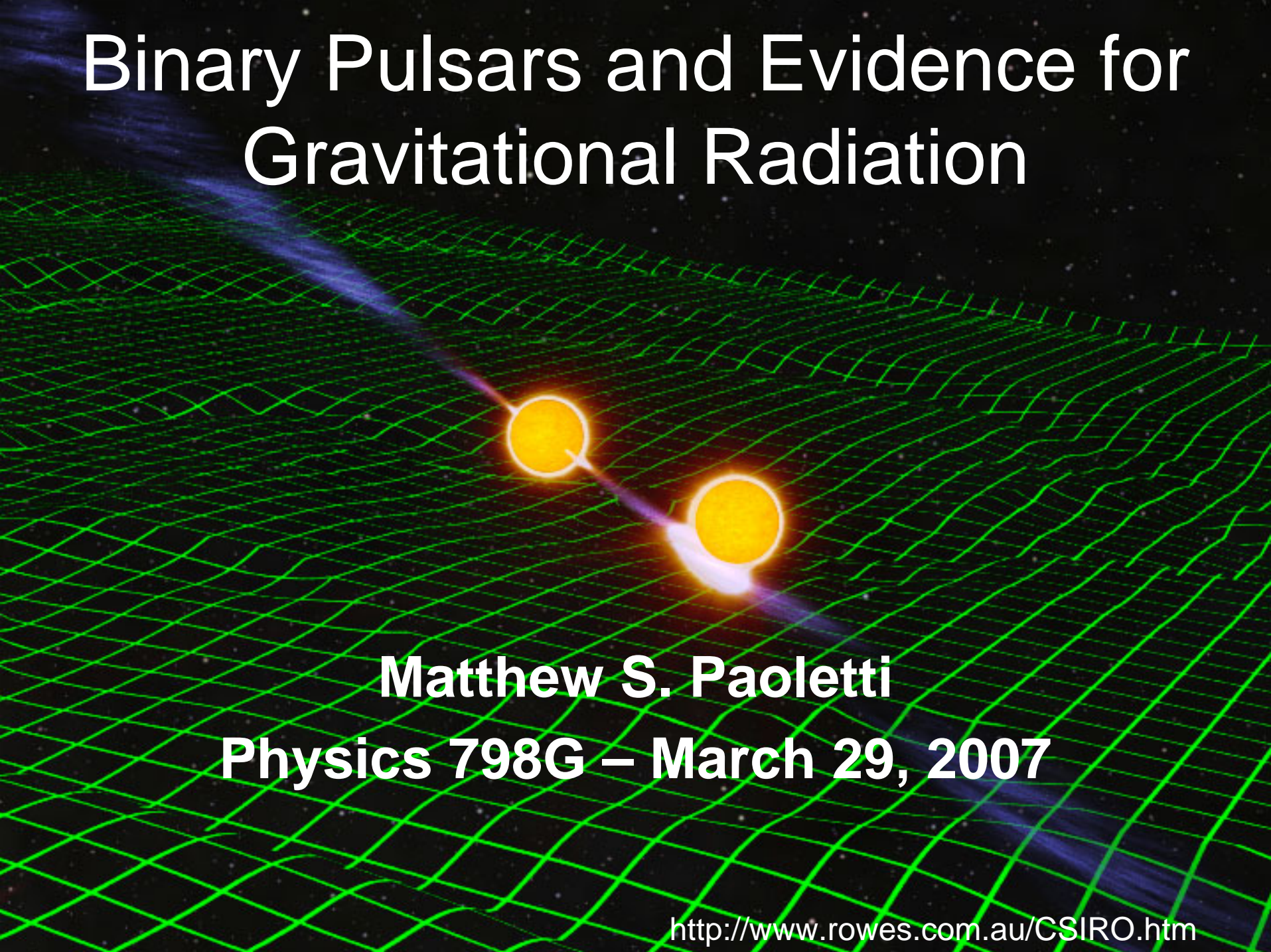


Binary Pulsars and Evidence for Gravitational Radiation



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Physics 798G – March 29, 2007

Motivation

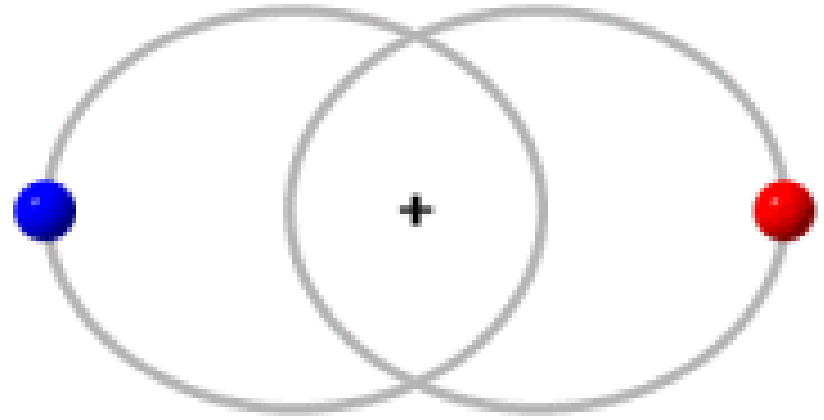
- Three classical tests of GR
 - Bending of light as it passes the sun
 - Gravitational redshift
 - Precession of perihelion of Mercury
- However, these interactions restricted to the **weak-field, slow-motion** interactions present within solar system

Motivation

- In **weak-field, slow-motion** limit nonlinear and gravitational radiation effects are negligible
- Post-Newtonian effects insignificant and barely detectable
- Classical tests do not provide sufficient test bed for competing theories of gravity
- **Gravitational radiation predictions do differ among theories of gravity, but need a significant source of gravitational radiation**

Binary Pulsars

- Composed of at least one pulsar and a companion massive object
- Pulsar regularly emits detectable pulses of radiation – **provide extremely stable clocks**



<http://commons.wikimedia.org/wiki/Image:Doublesystar.gif>

Binary Pulsars

- Masses of two bodies on order of solar mass
- Rapidly orbit each other

**Binary pulsars go beyond the weak-field,
slow-motion interactions
experimentalists were restricted to
prior to their discovery**

Objective

Use the stable “clocks” of binary pulsars to indirectly measure gravitational radiation emission to test theories of gravity in their relativistic limits

Discovery of First Pulsar

- Discovered in 1967 by Burnell and Hewish
- Team found a regular signal of pulsed radiation with a period of roughly a few seconds
- The team determined the radiation source was extraterrestrial

What could possibly be the source of such a perfect signal?

Discovery of First Pulsar

- Team dubbed the source of radio waves “LGM-1” for “Little Green Men”



<http://www.igougo.com/travelcontent/>

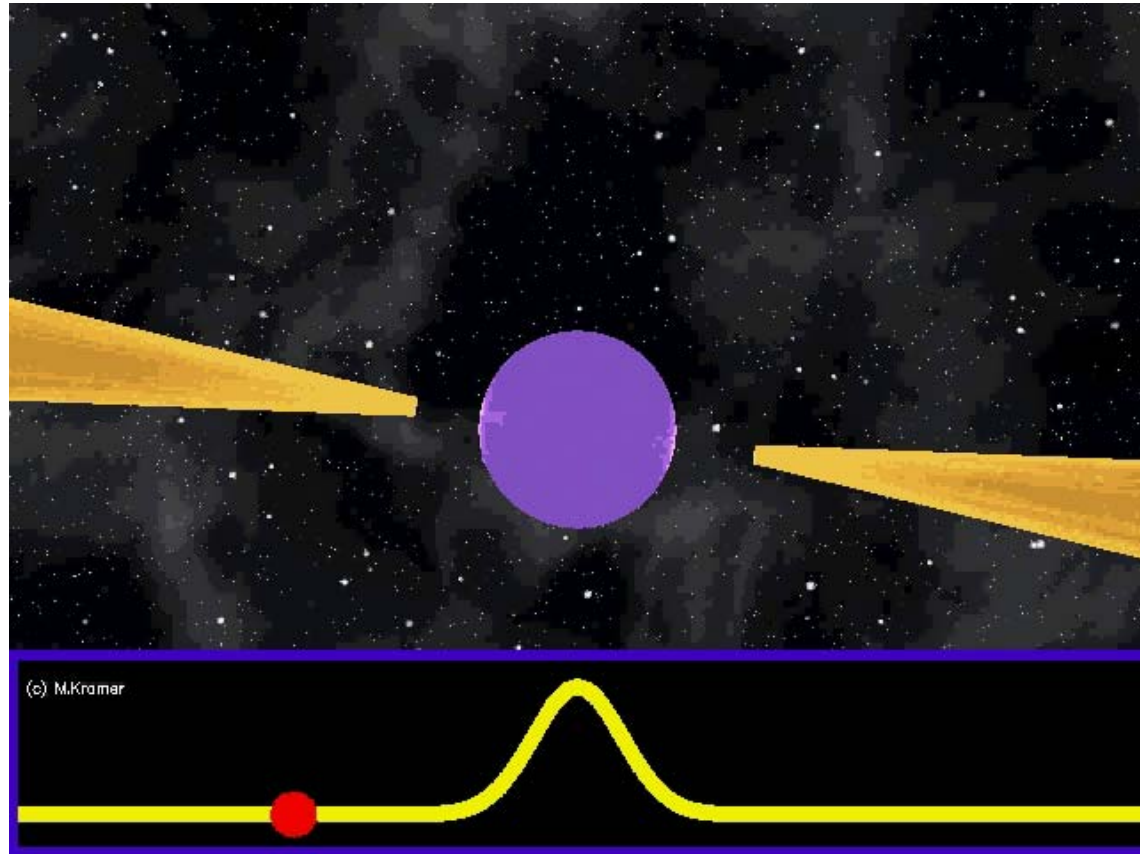
Discovery of First Pulsar

- Later determined source of radiation was a rapidly rotating, highly magnetized neutron star
- Radiation mechanism still not understood:
“Pulsars are a physicist's dream come true. They are made of the most extreme matter that we know of in the Universe, and their highly stable rotation makes them super-precise cosmic clocks - but, embarrassingly, we do not know how these clocks work.”

<http://www.pparc.ac.uk/Nw/rel241.asp?Tx=1>

Pulsar Emission

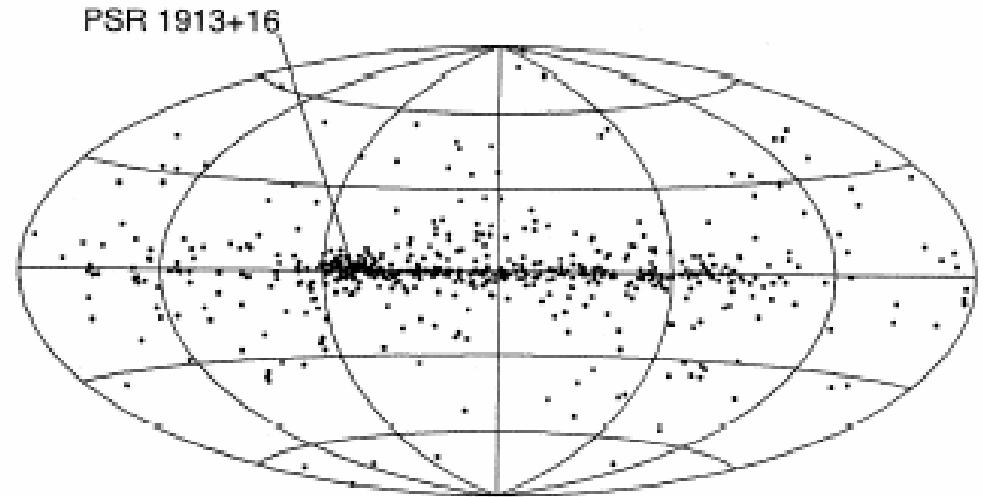
- Pulsar behaves like a lighthouse, emitting a finite cone of light that rotates
- Light comes in strong, short pulses allowing them to serve as clocks



<http://www.jb.man.ac.uk/~pulsar/doublepulsarcd/>

Galactic Map

- As of July 1994, 558 pulsars had been located within the galaxy
- Image shows celestial map in Galactic coordinates



J.H. Taylor, *Rev. Mod. Phys.* **66**, 711 (1994)

Discovery of First Binary Pulsar

- After discovery of first pulsar, search for more ensued by Hulse and Taylor using 305 m radio telescope at Arecibo Observatory in Puerto Rico



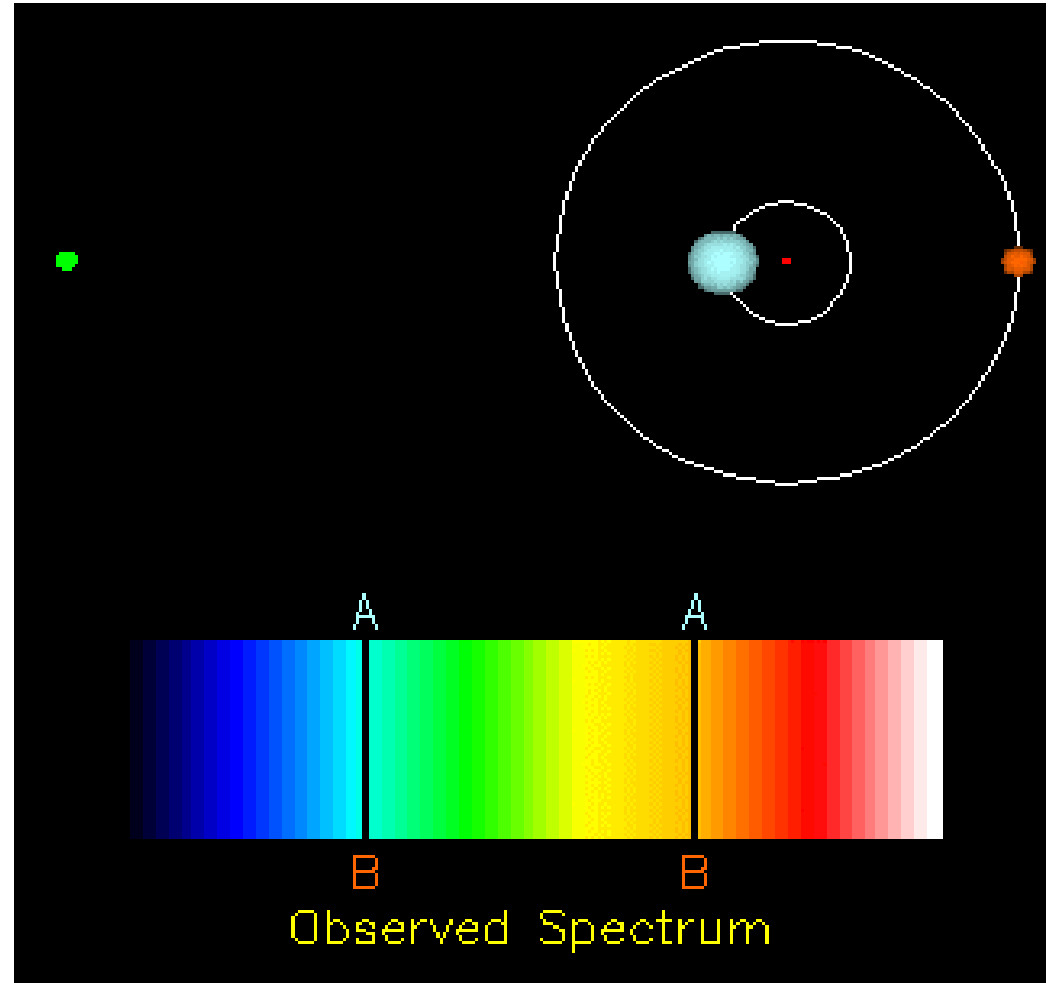
<http://burro.astr.cwru.edu/Academics/Astr201/Telescopes/arecibo.jpg>

Discovery of First Binary Pulsar

- Team found 40 pulsars prior to PSR 1913+16
- Sought to measure period to within $\pm 1 \mu\text{s}$
- Impeded by apparent changes in period of up to $80 \mu\text{s}$ from day to day
- At times period changed $8 \mu\text{s}$ over 5-minute observation
- Largest changes in other pulsars on order of $10 \mu\text{s}$ per year, typical changes many orders of magnitude lower

Discovery of First Binary Pulsar

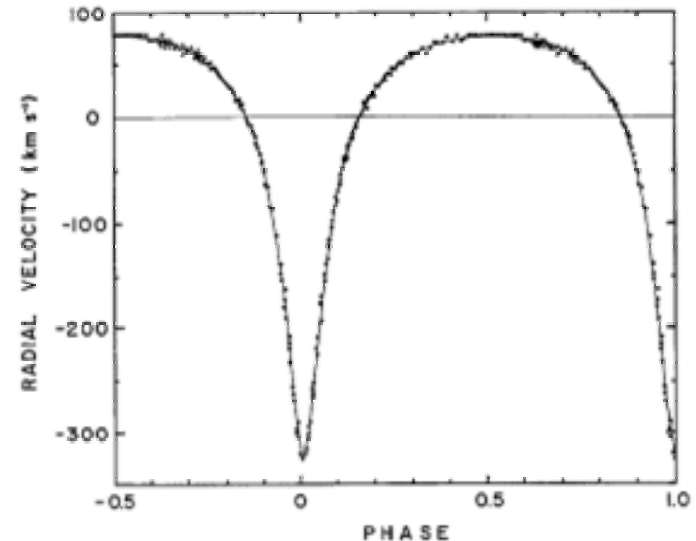
- Doppler shifts produced by orbital motion explained observed period changes (analogous to spectral line shifts)



http://ircamera.as.arizona.edu/NatSci102/NatSci102/movies/spcbin_an.gif

Discovery of First Binary Pulsar

- From Doppler shifts radial velocity determined
- Period and eccentricity of orbit:
 - $P_b = 27908 \pm 7 \text{ s}$
 - $e = 0.615 \pm 0.010$
- Taking orbit into account, period of pulsar determined to be an extremely stable 59 ms



R.A. Hulse and J.H. Taylor,
Astrophys. J. Lett. **195**, L51
(1975)

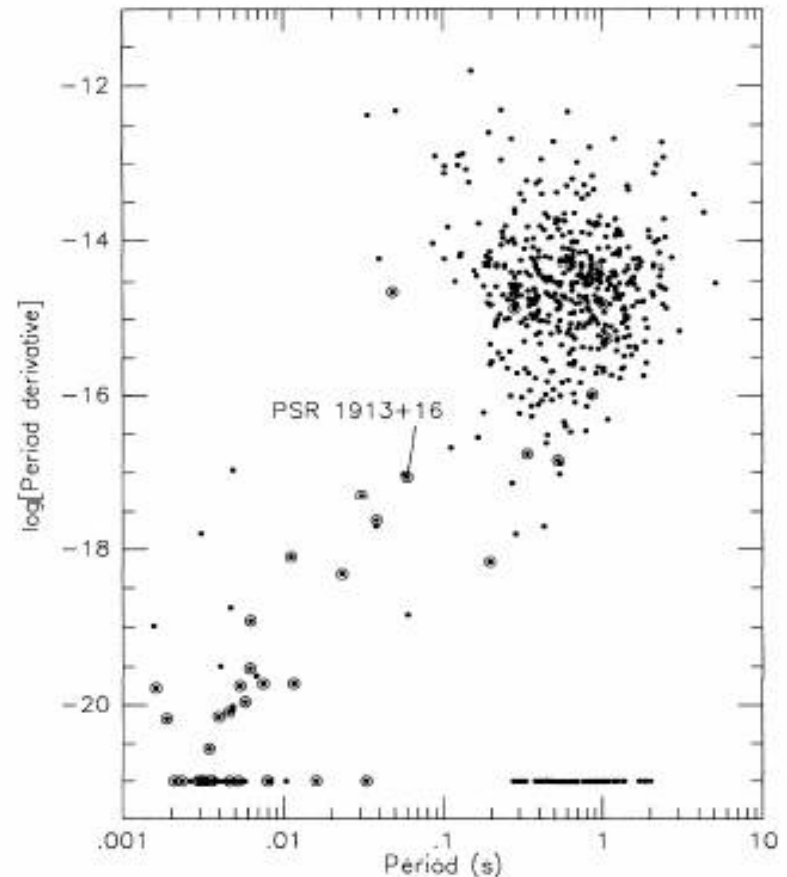
Gravitational Radiation

- General relativity and competing theories predict that orbiting massive bodies should emit quadrupolar gravitational radiation
- Gravitational radiation carries energy and angular momentum away from the system

These losses produce decrease in orbital period and eccentricity

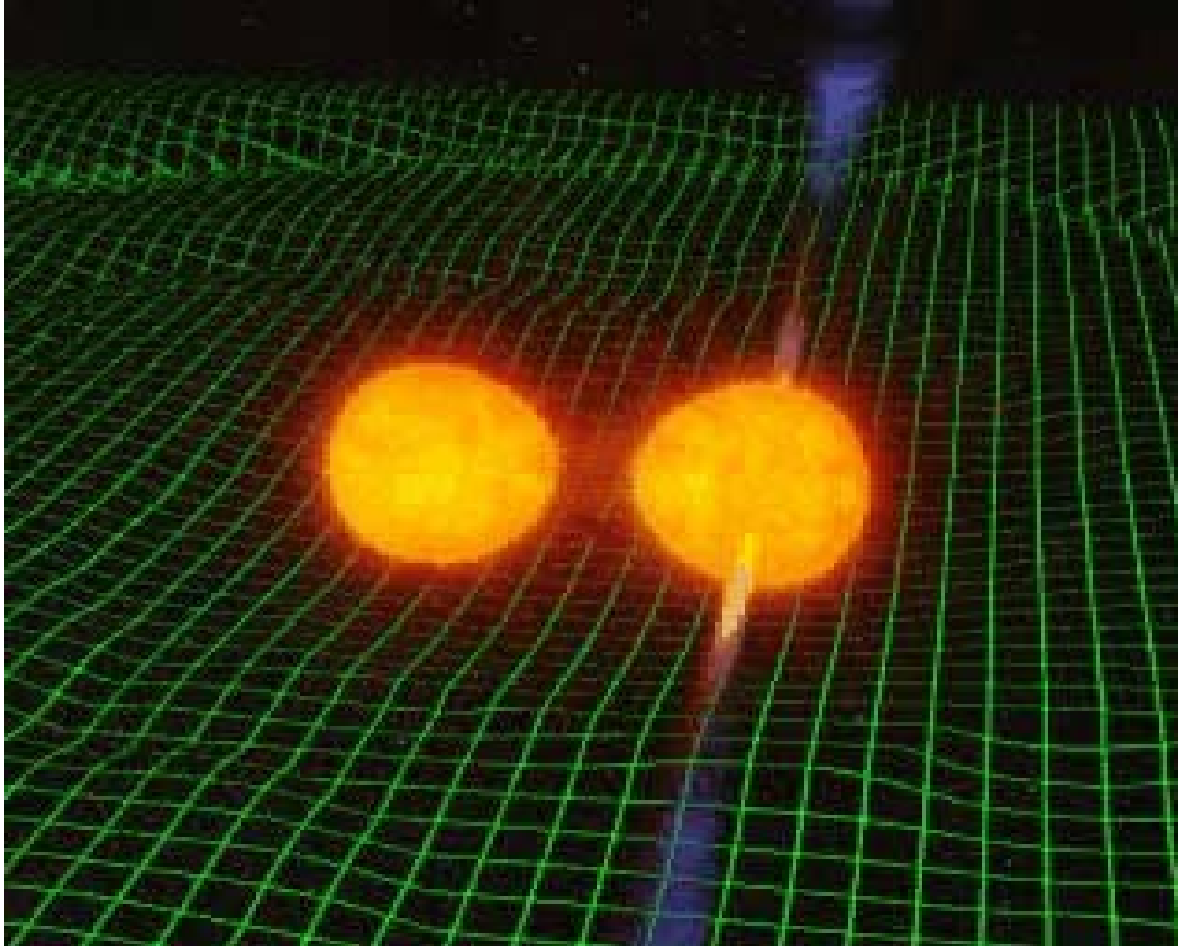
Gravitational Radiation

- Decay of orbital period is indirect test of predictions for gravitational radiation emission
- Spin-down rates span nine orders of magnitude, thereby spanning several regimes



J.H. Taylor, *Rev. Mod. Phys.*
66, 711 (1994)

Merger of Binary and Companion



<http://www.jb.man.ac.uk/~pulsar/doublepulsarcd/>

Decay of Binary Orbit

- General relativity predicts that decay of orbital period is given by:

$$\dot{P}_{b,GR} = -\frac{192\pi G^{5/3}}{5c^5} \left(\frac{P_b}{2\pi}\right)^{-5/3} (1-e^2) \times$$
$$\left(1 + \frac{73}{24}e^2 + \frac{37}{96}e^4\right) m_p m_c (m_p + m_c)^{-1/3}$$

- Notice, it is always negative (as expected)
- Becomes more negative with time implying flux of radiation increases with time

Masses are free parameters and need to be determined by other measurements

Determination of Masses

- Non-relativistic analysis yields five orbital parameters
- Relativistic analysis produces another three

Measured Orbital Parameters for B1913+16 System

Fitted Parameter	Value
$a_p \sin i$ (s)	2.3417725 (8)
e	0.6171338 (4)
T_0 (MJD)	52144.90097844 (5)
P_b (d)	0.322997448930 (4)
ω_0 (deg)	292.54487 (8)
$\langle \dot{\omega} \rangle$ (deg/yr)	4.226595 (5)
γ (s)	0.0042919 (8)
\dot{P}_b (10^{-12} s/s)...	-2.4184 (9)

J.M. Weisberg and J.H. Taylor, *Binary Radio Pulsars ASP Conference Series*, 1 (2004)

Determination of Masses

- Orbit and masses may be fully specified by first seven orbital parameters, **eighth over determines system and serves as test bed of theories**

General Relativity must be assumed correct to place restrictions on masses

- Assuming GR, restrictions on masses appear as curves or bands in companion mass versus pulsar mass parameter space

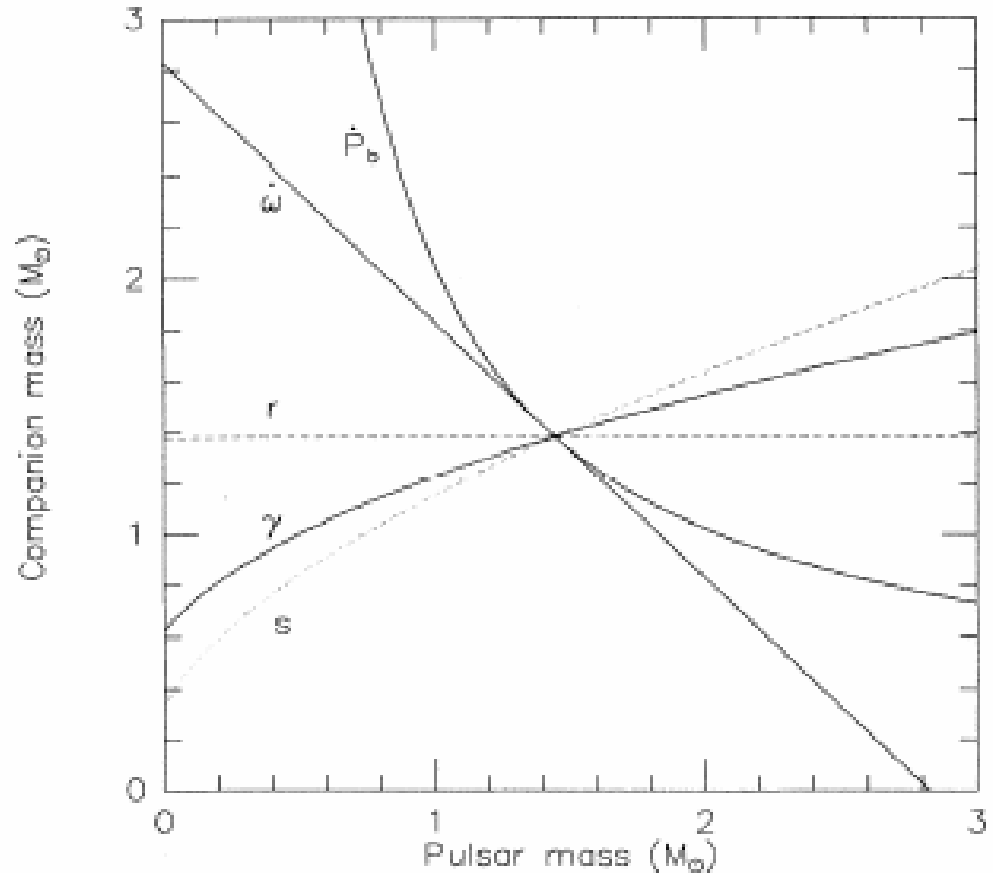
Determination of Masses

- Intersection of curves at single point precisely determines masses:

$$m_1 = 1.4414 \pm 0.0002$$

$$m_2 = 1.3867 \pm 0.0002$$

times the mass of the
sun



J.H. Taylor, *Rev. Mod. Phys.* **66**,
711 (1994)

Evidence for Gravitational Radiation

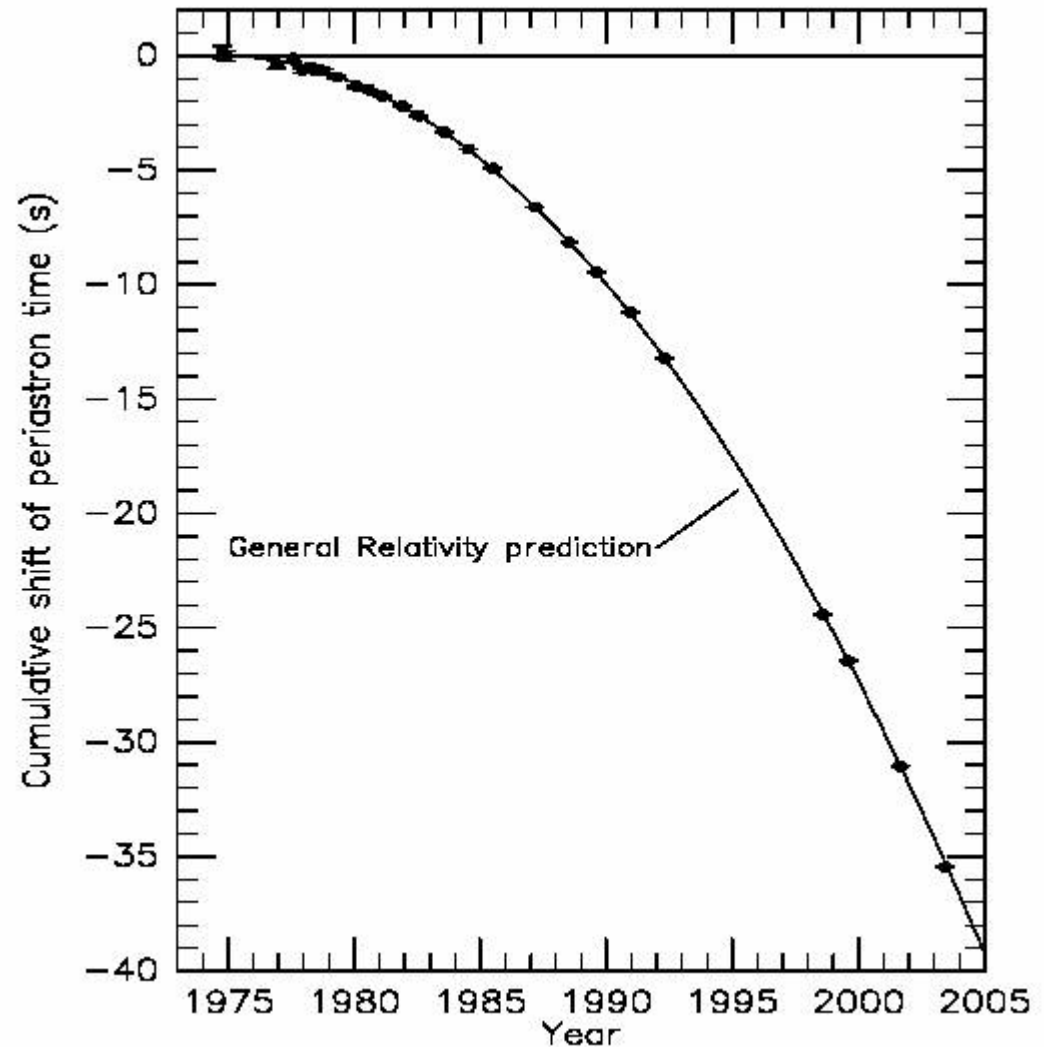
- Knowing the masses, GR can predict the decay of the orbit and may be compared to observed value

$$\frac{\dot{P}_{b,corrected}}{\dot{P}_{b,GR}} = 1.0013 \pm 0.0021$$

- Agree at the $(0.13 \pm 0.21)\%$ level

Evidence for Gravitational Radiation

- Orbital decay has been observed and compared to GR prediction for over 30 years



Conclusions

- Binary pulsar PSR 1913+16 enables tests of GR in strong-field, rapid-motion limit
- Observations of orbital decay confirm the GR prediction of gravitational radiation emission

Observed orbital decay is in good agreement *only* with GR

- Predictions of alternate, competing theories conflict strongly with observations presented here

Conclusions

- Despite repeated experimental verifications of GR, theory is not quantum mechanical
- Universe appears to be quantum mechanical, so GR cannot be final theory

But, any new theory of gravity will have to asymptote to GR in a wide range of limits to agree with experiment

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