

# Quantum Chromo-Dynamics (QCD)

[Theory of Strong (Nuclear) Force]: a brief/rough history (based on section 17.1 of Peskin, Schroeder)

(1949 Nobel prize)

- Begin with Yukawa's theory: strong (nuclear) force between protons, neutrons (spin- $\frac{1}{2}$ ) due to their coupling to / exchange of pions (spin-0), as discussed briefly in  $\pi$ -nucleon system in the context of (global)  $SU(2)$  symmetry (strongly interacting particles)
- Later on, a plethora of other hadrons were discovered, classified as mesons (spin-0, 1...) and baryons/anti-baryons (spin- $\frac{1}{2}, \frac{3}{2} \dots$ )
- In order to have a simpler underlying model for this hadron "zoo", Gell-Mann, Ne'eman, Zweig [in 1960's] proposed that hadrons have sub-structure, i.e., are made of <sup>all</sup> up(u), down(d) and strange(s) quarks (<sup>much</sup> smaller number of constituents), with fractional electric charges of  $+\frac{2}{3}$ ,  $-\frac{1}{3}$  &  $-\frac{1}{3}$ , respectively : there is an approximate  $SU(3)$  global symmetry (rotating u, d, s into each other), which can be used to classify the bound state hadrons; also it matches  $SU(2)$  of  $\pi$ -N system [i.e., restricting to hadrons made of u, d (lighter quarks) only (s is heavier, but still lighter than <sup>typical</sup> binding energy of  $\sim$  GeV, which accounts for large fraction of hadron masses)].

- The quark theory [predicted] new hadrons/  
bound states (and their properties), which were  
observed subsequently (2)
- While quark theory was successful as above, it  
[lacked] answers to questions such as what force  
binds quarks into hadrons in such a way that  
isolated / fractionally charged quarks are not  
seen?
- More empirically, there is a problem related  
to spin- $\frac{3}{2}$ , doubly charged particle/called  $\Delta^{++}$ .  
It can be interpreted as (uuu) bound state/baryon,  
with zero orbital angular and spins of all 3 u's  
being parallel: however, such a totally symmetric  
combination (of fermions) violates spin-statistics theorem  
also in 1960's
- So, Gell-Mann, Greenberg (@ UMD!) proposed that  
quarks carry (in addition to spin and flavor) an  
internal quantum number ("color"): each quark  
is triplet  $(\bar{3})$  of global at this stage -  $SU(3)$ /color  
symmetry [eventually, this became QCD: see below].
- It is also assumed that all hadrons are color singlet: 2 options are (as discussed in group  
theory - detour in context of Yukawa couplings of SM  
fermions)  $[\bar{q}_\alpha q'_\alpha]$  ( $\alpha = 1, 2, 3$  is color), giving mesons  
and  $[\bar{q}_\alpha q'_\beta q''_\gamma \epsilon^{\alpha\beta\gamma}]$ , giving baryons (and their  
anti-particles, made of  $\bar{q}$ 's, i.e., anti-quarks).

- So,  $\Delta^{++}$  is symmetric in spin & flavor space, ③  
but antisymmetric in color, thus being consistent  
with spin-statistics theorem

- The "colored" (quark model) raised its own [questions]:  
what is the physical role of color? Why should hadrons be color singlet (that seems like an ad-hoc assumption, even if it explains  $\Delta^{++}$  state)?

- Han, Nambu (still in 1960's) then proposed to make  $SU(3)$  color symmetry local, i.e., a non-abelian gauge theory [note that Yang, Mills in 1950's had introduced such a theory as a more mathematical/theoretical possibility, i.e., not for explaining specific forces in Nature], thus giving a more physical role to color

- I guess idea was that  $SU(3)$  color gauge boson ("gluon") exchange binds quarks into hadrons [again, prototype here being the highly successful  $U(1)$  gauge theory of QED, which binds proton & electron into hydrogen or electron-positron into positronium]

- However, perhaps gauged/colored quark model is still not convincing: how do we "make sense of" (e.g., calculate<sup>"in"</sup>) a strongly coupled gauge theory (cf. use of perturbation theory for - weakly coupled - QED)?! Hadrons being color singlets is still a puzzle [after all, isolated electrically charged particles such as electron are observed, so why not colored/ $SU(3)$ ?

quarks (maybe answer lies in strong coupling)?!)

- Almost independently of above more theoretical developments, came (also in 1960's) deep inelastic scattering (DIS) — type of experiments, e.g. electron - nucleon collisions with energy transfer  $\gtrsim \text{GeV}$  (mass/binding energy of nucleon).
- DIS showed that protons/neutrons are made of constituents (dubbed "partons"), which are weakly coupled at energies  $\gg \text{GeV}$  (but presumably strongly coupled / bound into protons/neutrons at lower energies).
- It was natural to identify (empirical) partons with quarks: so it boils down to searching for interactions (gauge/Yukawa... couplings) of quarks which are asymptotically free (AF), i.e., become stronger (weaker) in IR (UV)
- Of course, it was known that gauge coupling, e.g., in QED (or Yukawa couplings) "run"  
<sup>presumably</sup> but initial candidates were IR free instead,  
as we saw in <sup>case of</sup> QED ...
- ... it all came together with the discovery (in 1970's)
- by Gross, Wilczek; Politzer; 't Hooft (Nobel prize for first 3 in 2004) — that (in general) non-abelian gauge theories can be AF if running is dominated by contributions of gauge

## boson loops / self-interactions.

- So, <sup>above</sup>  $SU(3)$  color - gauged  $\boxed{QCD}$  - could do the job; well, we'd better address the issues mentioned earlier with the gauged/colored quark model (of Han, Nambu)!
- Indeed, the answers lie in the 2 regimes of  $\boxed{QCD}$  following from AF, i.e., at energies  $\gg$  GeV, we can indeed calculate <sup>(analytically)</sup> using perturbation theory (since QCD coupling constant is weak) <sup>in this limit</sup>
- Whereas, in the opposite case of energies  $\ll$  GeV, i.e., strong QCD coupling constant (non-perturbatively) binding quarks into hadrons, we can use [lattice] gauge theory, i.e., discretize space-time. In this way, <sup>i.e., numerically</sup>, Wilson showed "color is confined", i.e., observed / finite-energy asymptotic states are color singlets, so earlier assumption is a consequence of non-abelian gauge theory
- Here's a rough/intuitive picture of color confinement, i.e., why isolated quarks are not seen. Suppose we try to separate a color singlet state, e.g., a  $q\bar{q}'$  meson. In this process (see figure)



a "tube" of gauge field forms between  $q$  &  $\bar{q}$ , with

- (6)
- [fixed] energy density / radius, in turn, due to strong coupling (cf. EM). Thus, energy "cost" of separation  $\propto$  energetically distance between  $q$  &  $\bar{q}$ . Eventually, it is favorable for tube to "break", i.e., form two mesons instead of isolating quark and anti-quark.
- Henceforth, we focus on short-distance/ high-energy ( $\gg$  GeV) limit of QCD, where, we can use Feynman diagrams/ perturbation theory to make predictions, i.e., we will calculate (underlying) processes with weakly-coupled quarks & gluons
- However, in the end, we have to "connect" these weakly-coupled [partons] to states which are observed, i.e., hadrons
- So, there's "no escape" from other (strongly-coupled) regime! Nonetheless, we will show how this strong coupling can be "by-passed" (herein lies subtlety/non-triviality of this program), allowing us to calculate (some) observables involving hadrons.