

PHYS 272 (Spring 2018): Introductory Physics: Fields Summary of topics/formulae for final exam

Chapter 21 of Giancoli

1. Basics of Coulomb's law (force between $Q_{1,2}$): $F = \frac{1}{4\pi\epsilon_0} \frac{Q_1 Q_2}{r_{12}^2}$ (along line joining $Q_{1,2}$)
2. Basics of Electric Field (force on "test" charge q due to source charge Q): $\mathbf{F} = q\mathbf{E}$, where E (due to charge Q at distance r from it) $= \frac{1}{4\pi\epsilon_0} \frac{Q}{r^2}$ (directed away/toward Q)
3. Principle of superposition for force, electric field and potential

Chapter 22 of Giancoli

1. Flux, $\Phi_E = \int \mathbf{E} \cdot d\mathbf{A}$
2. Gauss's law: $\oint \mathbf{E} \cdot d\mathbf{A} = \frac{Q_{\text{encl}}}{\epsilon_0}$
3. Conductors: only surface charge; $\mathbf{E} = 0$ inside; $\mathbf{E} = \frac{\sigma}{\epsilon_0}$ at surface (normal to surface) and entire conductor has *same* potential

Chapter 23 of Giancoli

1. Potential energy of charge q in a potential V (due to other charges), $U = qV$
2. Basics of potential and field: $V = -\int^b_a \mathbf{E} \cdot d\mathbf{l}$; $\mathbf{E}_x = -\frac{\partial V}{\partial x}$
3. V due to point charge Q at a distance r from it $= \frac{Q}{4\pi\epsilon_0} \frac{1}{r}$
4. Potential energy of point charges: $U = \frac{1}{4\pi\epsilon_0} \sum_{i \neq j} \frac{Q_i Q_j}{r_{ij}}$

Chapter 24 of Giancoli

1. Capacitance: $Q = CV$; Parallel plate capacitor: $C = \frac{\epsilon A}{d}$, with $\epsilon = \epsilon_0 K$ (K is dielectric constant)
2. Equivalent capacitance of combination of two capacitors: $C_1 + C_2$ (in series: charges same, voltages add up to that of equivalent); $\left(\frac{1}{C_1} + \frac{1}{C_2}\right)^{-1}$ (in parallel: voltages same, charges add up to that of equivalent)
3. Energy stored in capacitor: $U = \frac{1}{2} CV^2$
4. Energy stored in electric field: $u = \frac{1}{2} \epsilon E^2$

Chapter 25 of Griffiths

1. Ohm's law: $V = IR$; $I = \int \mathbf{j} \cdot d\mathbf{A}$; $\mathbf{j} = nq\mathbf{v}_d = \sigma\mathbf{E}$ (where σ is conductivity and \mathbf{v}_d , q and n are drift velocity, charge and number density, respectively, of charge carriers)
2. For wire with uniform cross-section, $R = \rho \frac{l}{A}$ (where resistivity, $\rho = \frac{1}{\sigma}$)
3. Power: $P = VI$ (in general) $= I^2 R$ (in resistor)

Chapter 26 of Giancoli

1. Equivalent resistance of combinations of resistors: $R_{\text{eq}}^{\text{series}} = R_1 + R_2$ and $R_{\text{eq}}^{\text{parallel}} = (1/R_1 + 1/R_2)^{-1}$
2. Kirchhoff's junction rule: sum of all current entering any junction is equal to sum of all currents leaving that junction and Kirchhoff's loop rule: sum of potential differences across all the components along any closed path of the circuit (loop) must be zero.
3. Combinations of resistor and capacitor (RC circuit): voltage across capacitor while it is being charged by a battery via a resistance, $V_C = V_0(1 - e^{-t/\tau})$, where V_0 is the steady-state voltage (i.e., that of the battery) and $\tau = RC$ is the time constant. Whereas, during discharging of capacitor, $V_C = V_0e^{-t/\tau}$.

Chapter 27 of Giancoli

1. Force due to magnetic field: $\mathbf{F}_{\text{mag}} = q(\mathbf{v} \times \mathbf{B})$ (point charge, giving uniform circular motion for $v \perp \mathbf{B}$); $\mathbf{F}_{\text{mag}} = I \int d\mathbf{l} \times \mathbf{B}$ (line current): in particular, $\mathbf{F}_{\text{mag}} = I\mathbf{l} \times \mathbf{B}$ for a straight wire of length l in a uniform magnetic field
2. Lorentz force equation: $\mathbf{F} = q[\mathbf{E} + (\mathbf{v} \times \mathbf{B})]$
3. Torque on loop carrying current I : $\boldsymbol{\tau} = \boldsymbol{\mu} \times \mathbf{B}$, where magnetic dipole moment of current loop, $\boldsymbol{\mu} = NIA\mathbf{A}$ (with \mathbf{A} being area of loop, directed along normal to surface, using right-hand rule)

Chapter 28 of Giancoli

1. Bio-Savart law for magnetic field due to a wire carrying current I : $\mathbf{B} = \frac{\mu_0 I}{4\pi} \int \frac{d\mathbf{l} \times \mathbf{r}}{r^3}$, where \mathbf{r} is the vector from the infinitesimal element $d\mathbf{l}$ to the field point
2. Magnetic field due to an infinitely long straight wire carrying current I at a perpendicular distance r : $B = \frac{\mu_0 I}{2\pi r}$ (circumferential)
3. Magnetic field due to circular loop of radius R carrying current I at a distance x along axis: $B = \frac{\mu_0 IR^2}{2(x^2 + R^2)^{3/2}}$ (directed along axis)
4. Magnetic force (per unit length) between two long straight wires carrying currents $I_1, 2$ and distance d apart: $F_{\text{mag}} = \frac{\mu_0 I_1 I_2}{2\pi d}$
5. Ampere's law: $\oint \mathbf{B} \cdot d\mathbf{l} = \mu_0 I_{\text{enclosed}} = \int \mathbf{j}_{\text{enclosed}} \cdot d\mathbf{A}$, where j is the current density (i.e., current per unit cross-sectional area) and use right-hand rule to determine direction of positive current
6. Magnetic field due to a solenoid with n turns per unit length carrying current I : $B = \mu_0 nI$ (inside, directed along axis) and *vanishing* outside

Chapter 29 of Giancoli

1. Faraday's law for emf induced in a circuit (including motional): $\mathcal{E} = -\frac{d\Phi_B}{dt}$, where magnetic flux, $\Phi_B = \int \mathbf{B} \cdot d\mathbf{A}$ (including factor for number of loops in coil)

2. Lenz's law: direction of induced current is such that the flux it creates opposes the change of flux that induced it in the first place
3. A related version of Faraday's law (changing magnetic field/flux produces an electric field): $\oint \mathbf{E} \cdot d\mathbf{l} = -\frac{d\Phi_B}{dt}$

Chapter 30 of Giancoli

1. Mutual inductance between coil 1, which carries current I_1 creating magnetic flux Φ_{21} through coil 2 with N_2 turns: $M = \frac{N_2\Phi_{21}}{I_1}$ so that induced emf in coil 2 due to current in coil 1: $\mathcal{E}_2 = -M\frac{dI_1}{dt}$
2. Self-inductance of a single coil with N turns, which carries current I creating magnetic flux Φ_B through it: $L = N\frac{\Phi_B}{I}$ so that induced ("back/opposing") emf: $\mathcal{E} = -L\frac{dI}{dt}$
3. Energy stored in inductance L carrying current I : $U = \frac{1}{2}LI^2$, which can be thought of as being stored in the magnetic field, with energy density $u = \frac{1}{2}\frac{B^2}{\mu_0}$
4. Combination of inductance and resistance (LR circuit): when connected to a battery of emf V_0 , the current rises as $I = I_0(1 - e^{-t/\tau})$, where $I_0 = V_0/R$ is the steady-state current and $\tau = L/R$ is the time constant. Whereas, if the battery is removed, then the current drops as $I = I_0e^{-t/\tau}$
5. Combination of inductance and capacitance (LC circuit): capacitor discharging through an inductor exhibits oscillation (of charge on capacitor, current through inductor and energies stored in the two) with angular frequency $\omega = 1/\sqrt{LC}$, i.e., $Q = Q_0 \cos \omega t$ (where Q_0 is initial charge on capacitor) etc.

Chapter 31 of Giancoli

1. Changing electric field produces magnetic field (Maxwell's modification of Ampere's law): $\oint \mathbf{B} \cdot d\mathbf{l} = \mu_0 I_{\text{encl}} + \mu_0 \epsilon_0 \frac{d\Phi_E}{dt}$, where Φ_E is the electric flux ($\epsilon_0 \frac{d\Phi_E}{dt}$ being called the displacement current)
2. Maxwell's equations: $\oint \mathbf{E} \cdot d\mathbf{A} = \frac{Q_{\text{encl}}}{\epsilon_0}$ (Gauss's law); $\oint \mathbf{B} \cdot d\mathbf{A} = 0$ (Gauss's law for magnetism); $\oint \mathbf{E} \cdot d\mathbf{l} = -\frac{d\Phi_B}{dt}$ (Faraday's law) and $\oint \mathbf{B} \cdot d\mathbf{l} = \mu_0 I_{\text{encl}} + \mu_0 \epsilon_0 \frac{d\Phi_E}{dt}$ (Ampere-Maxwell's law)
3. Plane sinusoidal electromagnetic (EM) wave traveling in x -direction: $E_y = E_0 \sin(kx - \omega t)$ and $B_z = B_0 \sin(kx - \omega t)$, where k (wave-number) = $2\pi/\lambda$ in terms of wavelength (λ); $v = \lambda f$ is speed of the wave and f (ω) is (angular) frequency: Maxwell's equations give $\frac{E_0}{B_0} = v$, with $v = 1/\sqrt{\mu_0 \epsilon_0}$, which is (numerically) equal to the speed of light in vacuum, $c = 3 \times 10^8$ m/s
4. Energy carried by EM wave across unit area in unit time (Poynting vector):

$$\mathbf{S} = \frac{1}{\mu_0} \mathbf{E} \times \mathbf{B}$$