

Solution to Quiz 11(a)

We use eq 41.53 from the book.

$$P_{\text{tunnel}} = e^{-2W/\eta}$$

where w is the width of the forbidden region
and

$$\eta = \frac{\hbar}{\sqrt{2m(U_0 - E)}} \quad \begin{array}{l} \text{----- } U_0 \\ \text{----- } E \end{array}$$

Here, $w = 15 \text{ fm}$

Since the electron's energy is 1.5 MeV below the top,
we are actually already given

$$U_0 - E = 1.5 \text{ MeV}$$

Plugging values

$$\begin{aligned} \eta &= \frac{\hbar}{\sqrt{2m(U_0 - E)}} \\ &= 1.05 \times 10^{-34} \text{ J}\cdot\text{s} \left/ \sqrt{2 \times 1.67 \times 10^{-27} \times 1.5 \times 10^6 \times 1.6 \times 10^{-19}} \right. \\ &= 3.70 \times 10^{-15} \text{ m} = 3.70 \text{ fm} \end{aligned}$$

$$\begin{aligned} \Rightarrow P &= e^{-(2 \times 15 / 3.70)} = 3.2 \times 10^{-4} \\ &= 3.2 \times 10^{-4} \times 100 \% = 0.032 \% \end{aligned}$$