

February 24, 2016

Physics 132

Prof. ~~F. F. Redish~~

B. Dreyfus

■ Theme Music: Joni Mitchell

*Electricity*

■ Cartoon: Bill Watterson

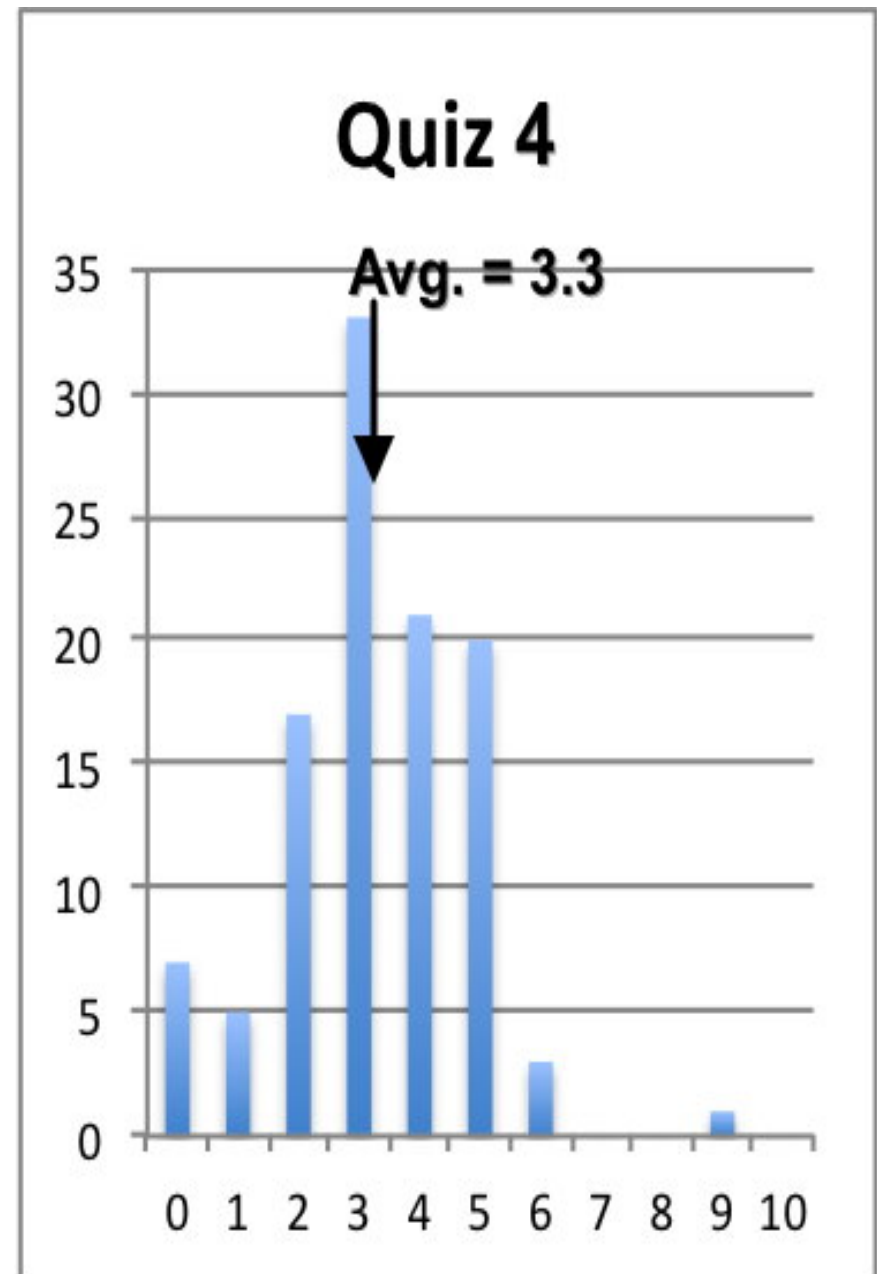
*Calvin & Hobbes*



# Quiz 4

	<b>1</b>
a	7%
b	<b>67%</b>
c	3%
d	<b>41%</b>
e	3%
f	2%
g	<b>31%</b>
h	9%

	<b>2</b>		<b>3.1</b>		<b>3.2</b>
a	<b>75%</b>	a	<b>60%</b>	a	3%
b	<b>20%</b>	b	<b>19%</b>	b	18%
c	5%	c	<b>16%</b>	c	<b>45%</b>
d	0%	ac	0%	d	<b>29%</b>
		bc	<b>2%</b>	e	<b>2%</b>
				f	2%



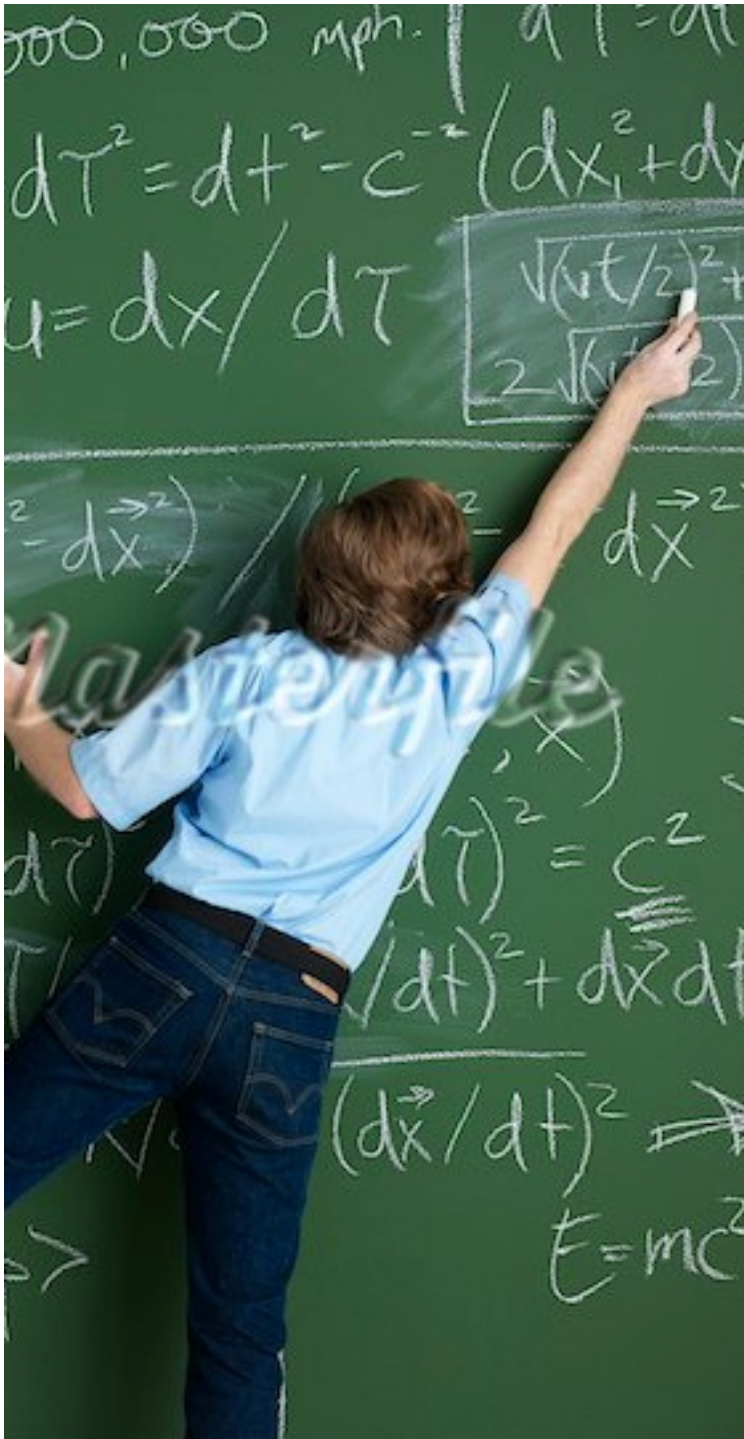
# The Equation of the Day

The Electric Field  
in simple  
model systems

$$E(\vec{r}) = k_c q / r^2$$

$$E(\vec{r}) = 2k_c \lambda / d$$

$$E(\vec{r}) = 4\pi k_c \sigma$$



# Recap: Vector Fields

- A *field* is a concept we use to describe anything that varies in space. It is a set of values assigned to each point in space (e.g., temperature or wind speed).
- A *force field* is an idea we use for non-touching forces. It puts a force vector at each point in space, summarizing the effect of all objects that would exert a force on a particular object placed at that point.
- A *gravitational, electric, or magnetic field* is a force field with something (a “coupling strength”) divided out so the field no longer depends on which test object is used.

$$\vec{g} = \frac{\vec{F}_{\text{acting on } m}}{m} \quad \vec{E} = \frac{\vec{F}_{\text{acting on } q}}{q}$$

Field is the value at a position in space “ $r$ ” assuming that the force is measured by placing the object at  $r$ .

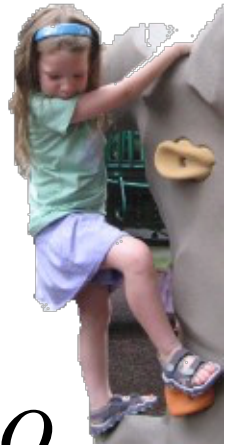
# Recap: Scalar Fields

- A *field* is a concept we use to describe anything that varies in space. It is a set of values assigned to each point in space (e.g., temperature or wind speed).
- An *potential energy field* is the assignment of a potential energy that a test charge would feel (add to the system) if placed at each point in space.
- A *gravitational, electric potential* is a potential energy field with something (a “coupling strength”) divided out so the field no longer depends on what test object is used.

$$gh = \frac{\Delta U_m^{\text{grav}}}{m} \quad V = \frac{\Delta U_q^{\text{electric}}}{q} \quad V(\vec{r}) = - \int_{\text{ref. pt.}}^{\vec{r}} \vec{E}(\vec{r}') \cdot d\vec{r}'$$

# Foothold ideas:

## Electric potential energy and potential



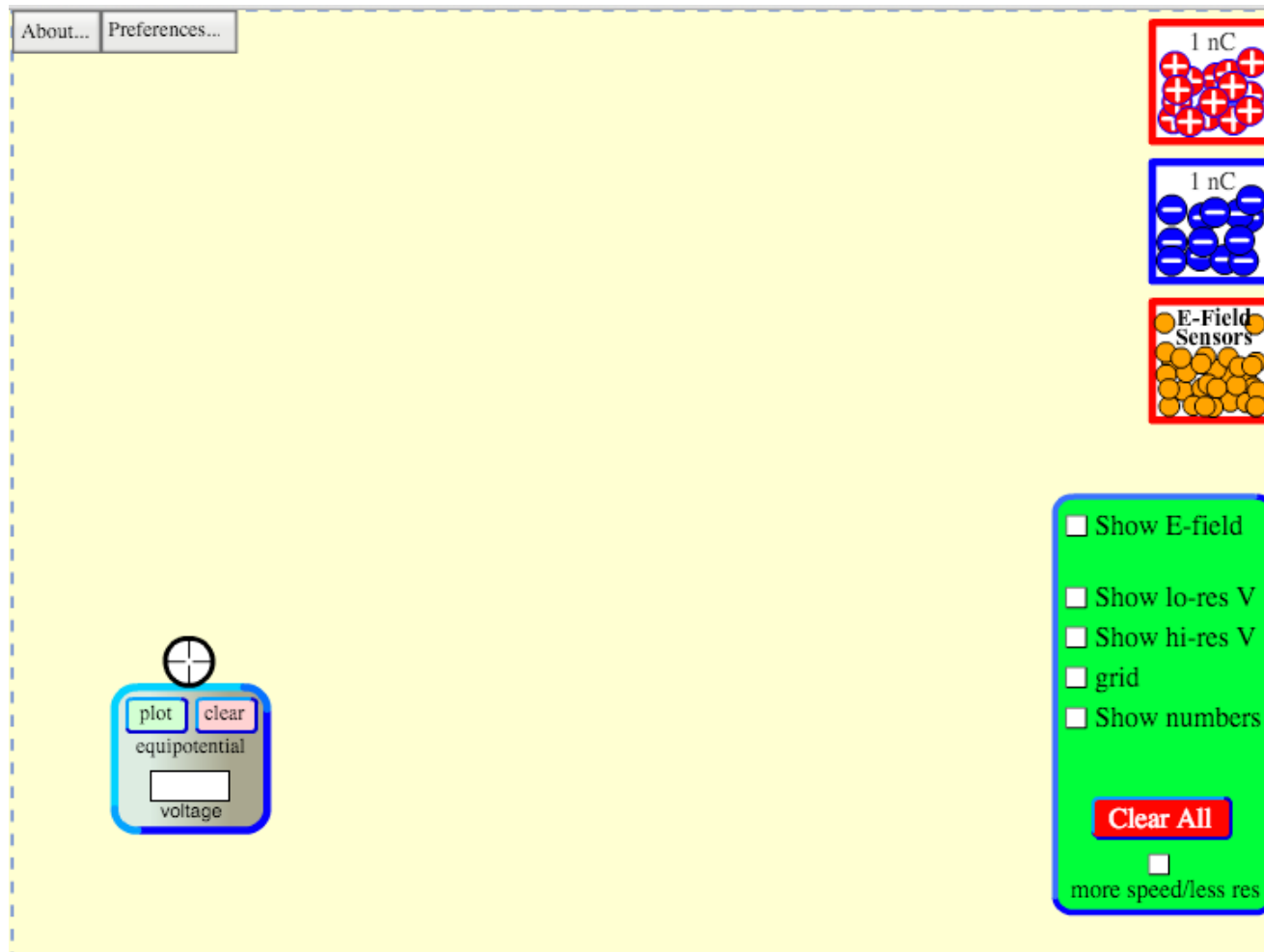
- The potential energy between two charges is
- The potential energy of many charges is
- The potential energy added by adding a test charge  $q$  is

$$U_{12}^{elec} = \frac{k_C Q_1 Q_2}{r_{12}}$$

$$U_{12\dots N}^{elec} = \sum_{i < j = 1}^N \frac{k_C Q_i Q_j}{r_{ij}}$$

$$\Delta U_q^{elec} = \sum_{i=1}^N \frac{k_C q Q_i}{r_{iq}} = qV$$

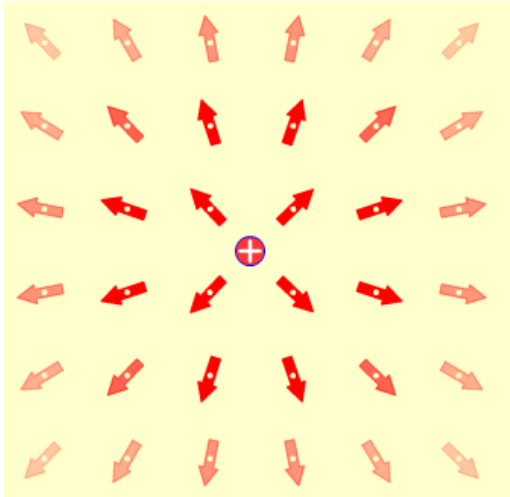
# Explore the potential near a point charge



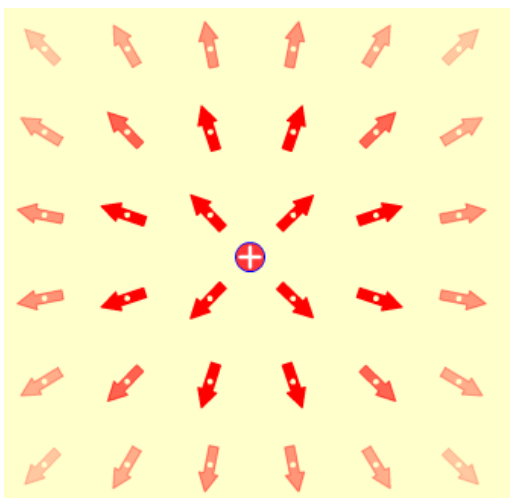
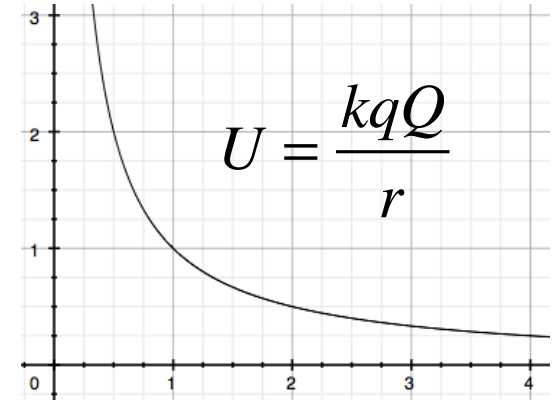
[https://phet.colorado.edu/sims/charges-and-fields/charges-and-fields\\_en.html](https://phet.colorado.edu/sims/charges-and-fields/charges-and-fields_en.html)



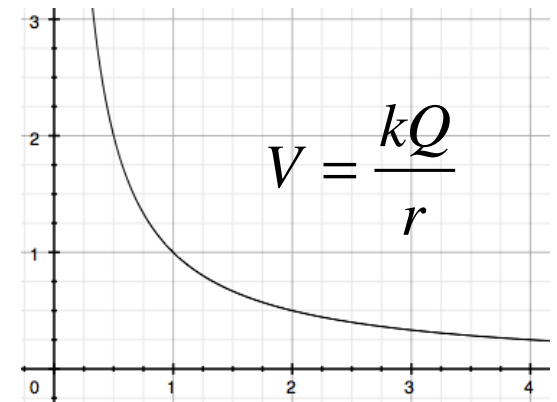
# Positive test charge near a single (+) source charge



Potential energy  
of a positive test charge  
near a positive source.

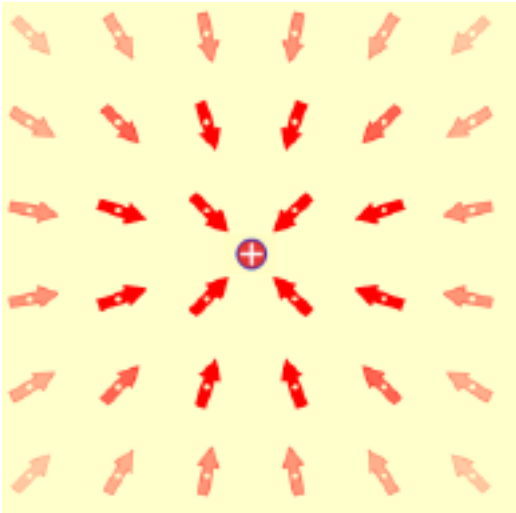


Electric Potential  
of a positive test charge  
near a positive source.

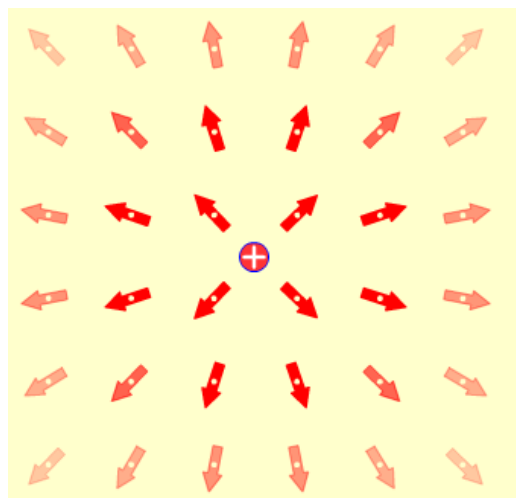
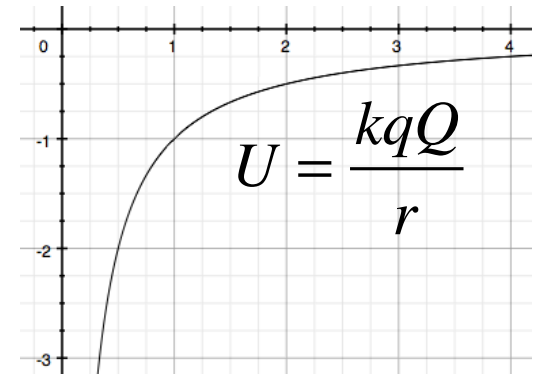




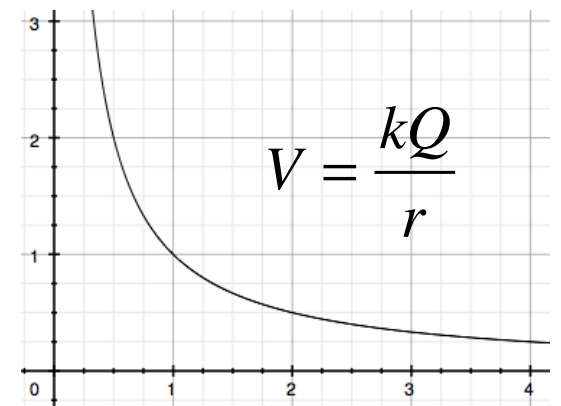
# Negative test charge near a single (+) source charge



Potential energy  
of a negative test charge  
near a positive source.



Electric Potential  
of a negative test charge  
near a positive source.



# Representations

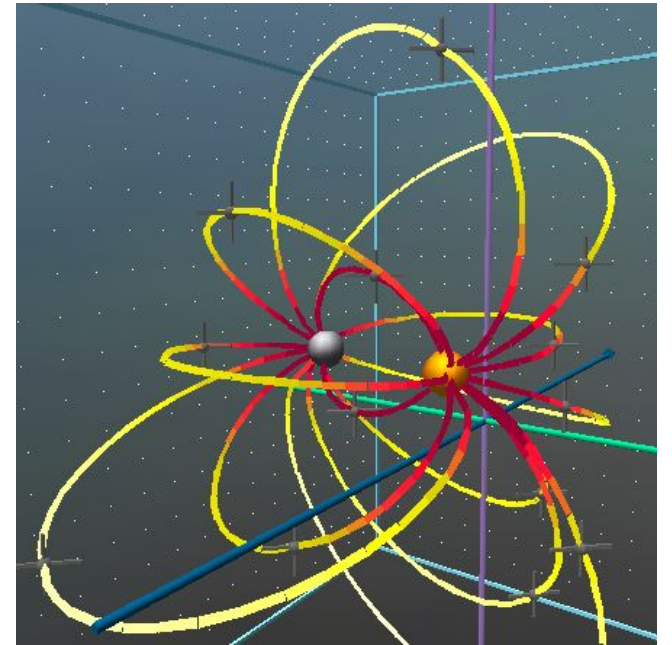
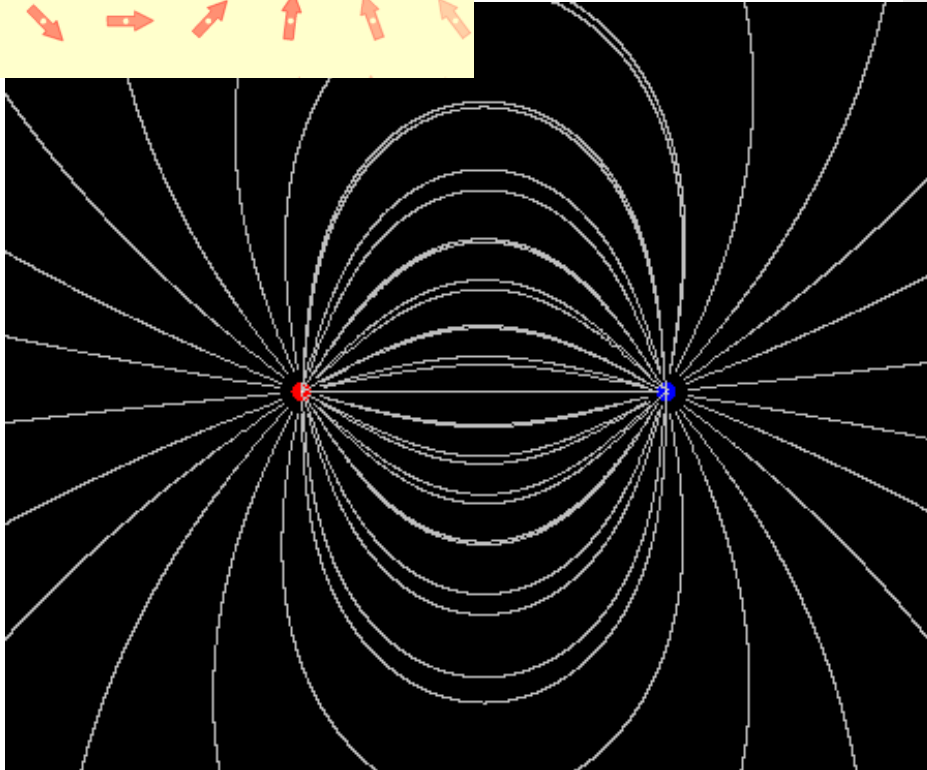
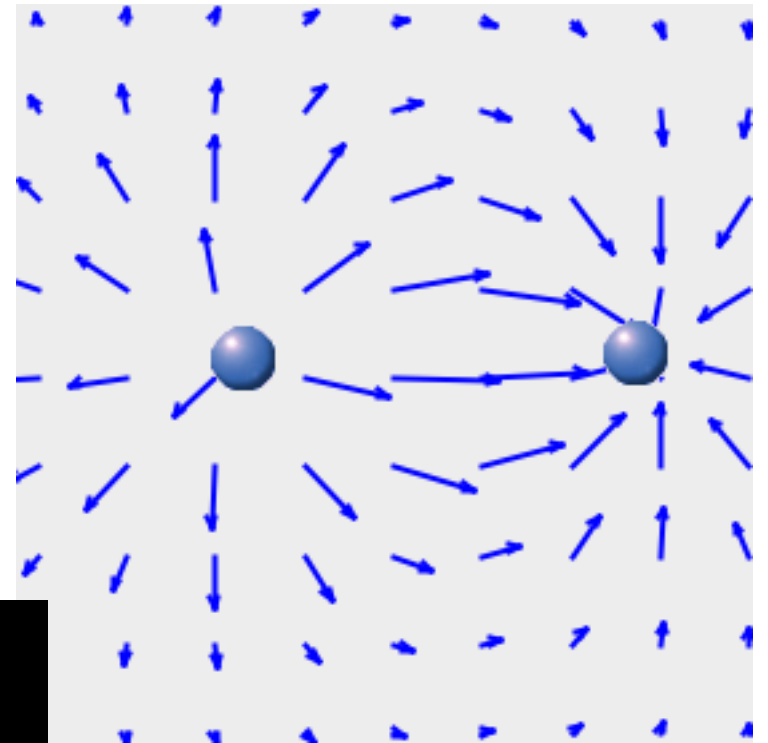
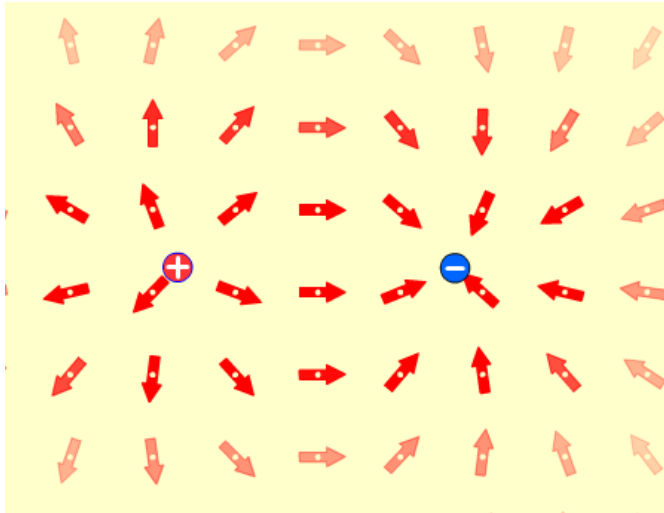
## ■ Representing $E$

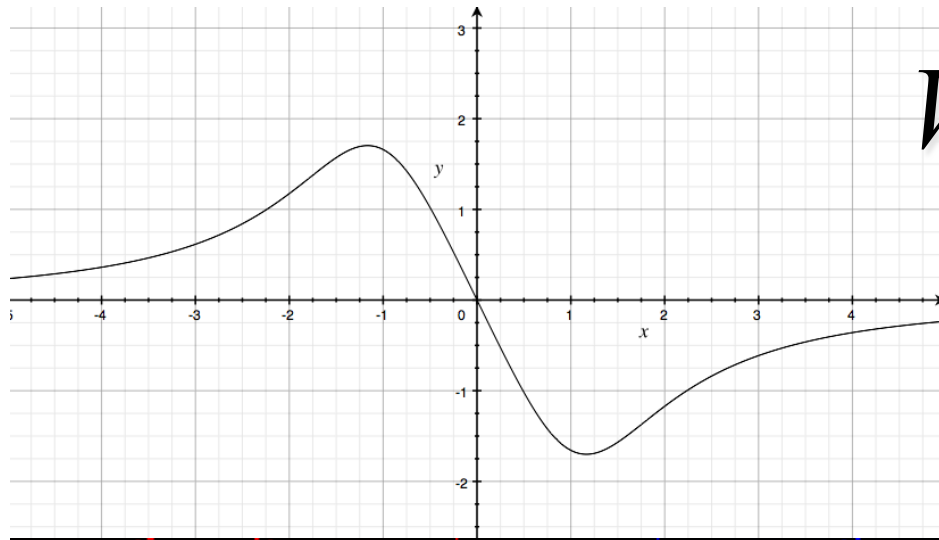
- Arrows (length shows  $|E|$ )
- Arrows (fixed length, color or width shows  $|E|$ )
- Field lines (show direction only)
- Field lines (color shows  $|E|$ )

## ■ Representing $V$

- 1D: Graph
- 2D: Isoclines (lines of equal value)
- 3D: Equipotential surfaces (surfaces of = value)

# $E$ field





$V$

