September 7, $2016 \quad$ Physics $131 \quad$ Prof. E. F. Redish
■ Theme Music: Wynton Marsalis Where or When?
■ Cartoon: Randall Munroe XKCD


9/7/16


Physics 131


1

## The Equation of the Day

## Functions



## Foothold Ideas: <br> Estimation - Quantifying experience

- Don't look up data online or get it from friends!*
- Don't use your calculator! Use 1-digit arithmetic
- Do figure out your estimations by starting with something you can plausibly know and scale up or down
- Do check your answer to see if it's reasonable
- Do learn a small number of Useful numbers
- Measure your body parts
* Sometimes on exams or homework we will give you or tell you to look up some numbers that you might in principle be able to estimate but that would take too much time.


## Reading questions: Estimation

- When would we need to use estimation techniques like this outside of physics?
- If we make an assumption, can that assumption be considered wrong on an exam? for example, if you wanted us to estimate how much one's hair grows in a year, and I assume it grows an inch/minute. This is clearly wrong, but its my assumption for the problem.
- When we guess something to start an estimation, it might vary from person to person. How can we know who is right when sometimes the value can be somehow abstract or hard to specifically calculate?


## My personal scales

| inches |
| :--- |
| First digit of <br> thumb |
| Open handspan |
| Forearm (cubit) |
| Full height |
|  |

## Useful numbers (people)

| Numbers |  |
| :--- | :--- |
| Number of people on the earth | $\sim 7$ billion $\left(7 \times 10^{9}\right)$ |
| Number of people in the USA | $\sim 300$ million $\left(3 \times 10^{8}\right)$ |
| Number of people <br> in the state of Maryland | $\sim 5$ million $\left(5 \times 10^{6}\right)$ |
| Number of students <br> in a large state university | $\sim 30-40$ thousand $\left(3 \times 10^{4}\right)$ |

## Useful numbers (distances)

| Macro Distances |  |
| :--- | :--- |
| Circumference of the earth | $\sim 24,000$ miles (1000 miles/ <br> time zone at the equator) |
| Radius of the earth* | $2 / \pi \times 10^{7} \mathrm{~m}$ |
| Distance across the USA | $\sim 3000$ miles |
| Distance across DC | $\sim 10$ miles |
| $9 / 2 / 16$ | Physics 131 |

## Useful numbers (bio)

| Bio Scales |  |
| :--- | :--- |
| Size of a typical animal cell | $\sim 10-20$ microns $\left(10^{-5} \mathrm{~m}\right)$ |
| Size of a bacterium, <br> chloroplast, or mitochondrion | $\sim 1$ micron $\left(10^{-6} \mathrm{~m}\right)$ |
| Size of a medium-sized virus | $\sim 0.1$ micron $\left(10^{-7} \mathrm{~m}\right)$ |
| Thickness of a cell membrane | $\sim 5-10 \mathrm{~nm}\left(10^{-8} \mathrm{~m}\right)$ |



## Cat television

- When we do science, we don't try to solve the entire universe at once.


■ We restrict our considerations to a limited set of data and try to understand it. Only when we get it do we try to expand further to more situations.

- This is like looking out a window onto a small segment of the world. Since cats like to do this, I call the process "choosing a channel on cat television."


## The Main Question

(for this term, at least)

- Start by choosing a big question and then refining it:


## How do things move?

Why choose this?
-concepts of measurement, rate of change, and force are basic - set frame for what are appropriate terms to use to think about motion.
-ties to everyday experience so can use and learn to build/refine intuition

## Foothold ideas: Measuring "where"

- In order to specify where something is we need a coordinate system. This includes:

1. Picking an origin
2. Picking perpendicular directions
3. Choosing a measurement scale


Can position
be negative?
What would that mean?

- Each point in space is specified by three numbers: ( $x, y, z$ ), and a position vector- an arrow showing the displacement from the origin to that position.
- Vectors add like successive displacements or algebraically by

$$
\vec{A}=A_{x} \hat{i}+A_{y} \hat{j} \quad \vec{B}=B_{x} \hat{i}+B_{y} \hat{j}
$$

$$
\vec{A}+\vec{B}=\left(A_{x}+B_{x}\right) \hat{i}+\left(A_{y}+B_{y}\right) \hat{j}
$$

## Notation

- We specify the directions we are talking about by drawing two little arrows of unit length in two perpendicular directions.
- " $x$ " and " $y$ " are called the coordinates and can be positive or negative.

- Note that if $x$ is negative, it means $x \hat{i}$ is a vector pointing in the direction opposite to $\hat{i}$
https://phet.colorado.edu/sims/vector-addition/vector-addition_en.html


## Foothold ideas: Vectors (2-D coordinates)

- We have 2 directions to specify. We must
- Choose a reference point (origin)
- Pick 2 perpendicular axes ( $x$ and $y$ )

- Choose a scale
- We specify our $x$ and $y$ directions by drawing little arrows of unit length in their positive direction. $\hat{i}, \hat{j}$
- A position vector (displacement from the origin) is written

$$
\vec{r}=x \hat{i}+y \hat{j}=(x, y)
$$

- $x$ and $y$ have units, $\hat{i}, \hat{j}$ do not.


## Foothold ideas: Measuring "when"

- Time is a coordinate just like position
- We need an origin (when we choose $t=0$ )
- a direction (usually times later than 0 are + )
- a scale (seconds, years, millennia)

■ Note the difference between

- clock reading, $t$
- a time interval, $\Delta t$

This is like the difference between position and length!

- Positions can now be specified as functions of time: $x(t)$ and $y(t)$

