

December 4, 2015

Physics 131

Prof. E. F. Redish

## ■ Theme Music: Peggy Lee

*Fever*

## ■ Cartoon: Jef Mallett

*Frazz*



12/4/15

Physics 131

1

# Outline

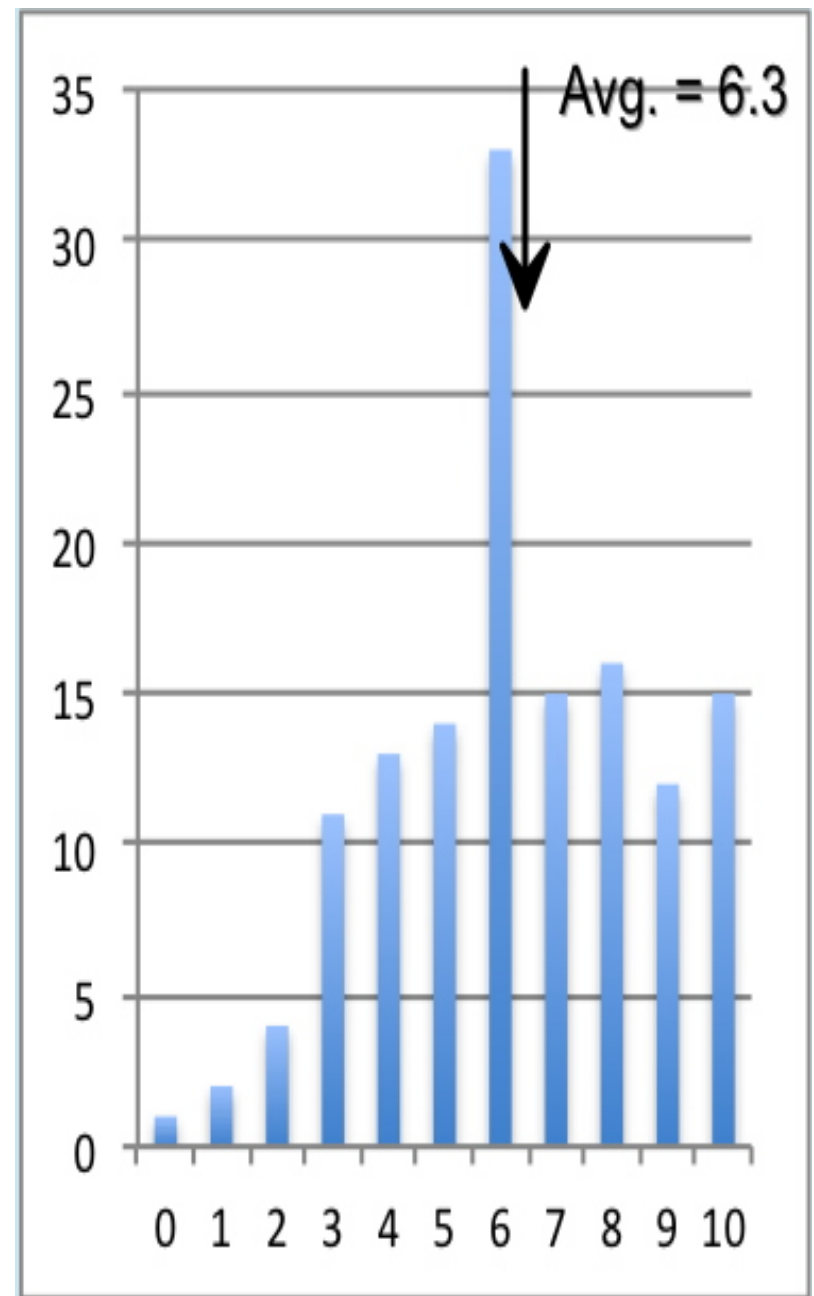
- Go over Quiz 10
- What do we mean by temperature?
- Heat capacity and specific heat

# Results from all Exams

	<b>#1</b>	<b>#2</b>	<b>#3</b>	<b>#4</b>	<b>#5</b>
<b>Exam 1</b>	91%	73%	58%	51%	66%
<b>Exam 1MU</b>	47%	37%	48%	54%	66%
<b>Exam 2</b>	72%	79%	37%	58%	74%
<b>Exam 2MU</b>	62%	50%	39%	59%	58%

# Quiz 10

	1.1	1.2	2.1	2.2
1	5%	9%	1%	18%
2	46%	10%	90%	8%
3	5%	21%	8%	65%
4	31%	41%	1%	4%
5	11%	16%		5%
6	1%	3%		0%
7	0%			





# *The Equation of the Day*

Heat and  
temperature

$$Q = mc\Delta T$$

# “The kind of motion we call heat”



- We have a natural sense of hot and cold.
- In the 19<sup>th</sup> century it was learned that the warmth of an object was a measure of a kind of random internal motion of the object's atoms.
- It was found that there was a surprisingly large amount of “hidden” energy that objects possessed as a result of their temperature – and that under the right conditions, this energy could be put to work.

# Real-World Intuition 1:



- If we have a cup of hot water and a cup of cold water and we put them aside for a while, what will happen to them?



## Real-World Intuition 2

### How do objects exchange hot and cold?



- When two amounts of water at different temperatures are combined, they come to a temperature somewhere in between.
- We expect that the amount of each kind of water determines the final temperature.
- Try it!
  - Case 1: Equal amounts of water
  - Case 2: Different amounts of water



# Two Objects of the Same Kind but Different Temperatures



Physical idea:  
The bigger mass changes  
its temp less in proportion.

$$\frac{m_1}{m_2} = \frac{\Delta T_2}{\Delta T_1}$$

$$m_1 \Delta T_1 = -m_2 \Delta T_2 \quad \longleftarrow$$

the changes in  
temp are opposite—  
one goes up  
the other goes down

$$m_1(T_f - T_1) = m_2(T_2 - T_f)$$

$$m_1 T_f - m_1 T_1 = m_2 T_2 - m_2 T_f$$

$$m_1 T_f + m_2 T_f = m_1 T_1 + m_2 T_2$$

$$T_f = \frac{m_1 T_1 + m_2 T_2}{m_1 + m_2} = \left( \frac{m_1}{M} \right) T_1 + \left( \frac{m_2}{M} \right) T_2$$

# Implications

- From the equation  $m_1\Delta T_1 = -m_2\Delta T_2$ 
  - it looks like something is being transferred from the hot object to the cold object
  - it looks like temperature is kind of a “density of hotness.” You have to multiply by the mass to get the “amount of hotness” transferred.
- We will call the thing being transferred “thermal energy.”

# What if we have different kinds of stuff?

- What happens if we have equal masses of water and something else — a copper cylinder, say?
- What's your intuition here?
  - Will the temperature settle down to halfway between?
  - Will it be closer to the water's temperature?
  - Will it be closer to the copper's temperature?
- Try it!

# Thermal Energy is NOT Temperature

- Even if the masses are the same, the temperature does not wind up halfway between.
- Each kind of material translates thermal energy into temperature in its own way.

$$m_1 c_1 \Delta T_1 = -m_2 c_2 \Delta T_2$$

# Specific Heat and Heat Capacity

- The amount of thermal energy needed to produce one degree of temperature change in an object is called its heat capacity.

$$Q = C\Delta T$$

- The amount of thermal energy per unit mass needed to produce one degree of temperature change in an object is called its specific heat.

$$C = mc$$

# Scales and Units

- 1 cal = the amount of thermal energy needed to change the temperature of 1 gm of water by 1 degree C (from 14.5° to 15.5°) (by definition)
- 1 Cal = 1000 cal
- 1 Cal = 4184 J

# Reinterpreting Our Results

When two objects at different temperature are put together, thermal energy flows from the hotter body to the colder body until their temperatures are the same. (0<sup>th</sup> Law)

$$Q = m_1 c_1 \Delta T_1 = m_1 c_1 (T_f - T_1^i)$$

$$-Q = m_2 c_2 \Delta T_2 = m_2 c_2 (T_f - T_2^i)$$

$$m_1 c_1 (T_f - T_1^i) = -m_2 c_2 (T_f - T_2^i)$$

$$m_1 c_1 (T_f - T_1) = m_2 c_2 (T_2 - T_f)$$

$$T_f = \left( \frac{m_1 c_1}{m_1 c_1 + m_2 c_2} \right) T_1 + \left( \frac{m_2 c_2}{m_1 c_1 + m_2 c_2} \right) T_2$$

$$T_f = \left( \frac{C_1}{C_1 + C_2} \right) T_1 + \left( \frac{C_2}{C_1 + C_2} \right) T_2$$

# Foothold ideas: 1



- Temperature is a measure of how hot or cold something is. (We have a natural physical sense of hot and cold.)
- When two objects are left in contact for long enough they come to the same temperature.
- When two objects of the same material but different temperatures are put together they reach an average, weighted by the fraction of the total mass.
- The mechanism responsible for the above rule is that the same thermal energy is transferred from one object to the other:  $Q$  proportional to  $m\Delta T$ .



## Foothold ideas: 2



- When two objects of different materials and different temperatures are put together they come to a common temperature, but it is not obtained by the simple rule.
- Each object translates thermal energy into temperature in its own way. This is specified by a density-like quantity,  $c$ , the specific heat.
- The heat capacity of an object is  $C = mc$ .
- When two objects of different material and different temperatures are put together they reach an average, weighted by the fraction of the total heat capacity.
- When heat is absorbed or emitted by an object  $Q = \pm mc\Delta T$

## Example:



A copper pot with a mass of 2 kg is sitting at room temperature ( $20^{\circ}\text{C}$ ). If 200 g of boiling water ( $100^{\circ}\text{C}$ ) are put in the pot, after a few minutes the water and the pot come to the same temperature. What temperature is this?

*We made a number of simplifying but unrealistic assumptions that could affect the final value of the temperature. Name three.*

# Real-World Intuition 1: Reconsidered



- If we have a cup of hot water and a cup of cold water and we put them aside for a while, what will happen to them?



- If you touch the cloth part of your chair and the metal part, which feels warmer?

