TRIG IDEN TITY

=
$$Sm(A+B)$$
 $Cos(A-B)$ + $Cos(A+B)$ $Sm(A-B)$

Now
$$\operatorname{Cos}\left(B-A\right) = \operatorname{Cos}\left(A-B\right)$$

But
$$Sui \left(B-A \right) = -Sui \left(A-B \right)$$

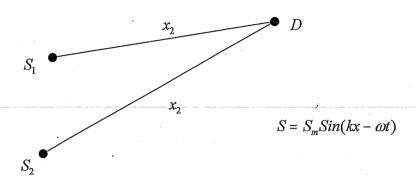
Hence

Similarly

That is, a wave whose amplitude is controlled by (x1-x2) leading to INTERFERENCE.

SOUND WAVES-INTERFERENCE

What happens if two sound waves start in phase but have traveled different distances before they arrive at the detector? S_1, S_2 are two sources of sound, which emit waves in phase.



Let us put both phases equal to zero at the starting points. Note: when a wave travels a distance λ its phase must change by 2π . Hence, the wave from S_1 is when it arrives at D will have the phase $\Phi_1 = \frac{2\pi}{\lambda} x_1$.

When this wave arrives at D there is nothing there. However, when the wave from S_2 arrives at D its phase will be $\Phi_2 = \frac{2\pi}{\lambda} x_2$ and since wave from S_1 already there, the two waves superpose. If $(\Phi_1 - \Phi_2) = 0.2\pi, 4\pi, 6\pi$ the two waves will be in phase at D and will combine to produce a maximum at D.

We call this constructive interference.



CONDITION FOR MAXIMUM AT D:

$$(\Phi_{1} - \Phi_{2}) = 2M\pi \quad M = 0,1,2...$$

$$\frac{2\pi}{\lambda}(x_{1} - x_{2}) = 2M\pi$$

$$or (x_{1} - x_{2}) = M\lambda \quad M = 0,1,2...$$
(I)

In other words, if the path DIFFERENCE is a whole # of λ 's, the waves which started in phase will again be in phase at D and produce a maximum there.

However, if

$$(\Phi_1 - \Phi_2) = \pi, 3\pi, 5\pi...$$
or equivalently
$$(x_1 - x_2) = (2m+1)\frac{\lambda}{2}$$
(II)

with m=0, 1, 2, ...

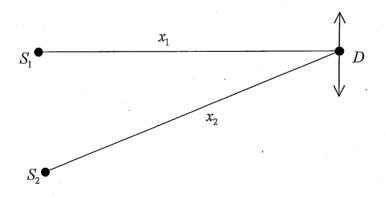
When the waves meet at *D*, they will be exactly out of phase And cancel each other.

DESTRUCTIVE INERFERENCE

CONDITION FOR MINIMUM

$$(x_1 - x_2) = (2m+1)\frac{\lambda}{2}, m = 0,1,2,...$$
 (II)

If you keep S_1 and S_2 fixed and move D up and down as shown, $(x_1 - x_2)$ will vary and you will encounter a series of maxima (loud sound) and minima (no sound) as you go alternately from Eq I to Eq II and vice versa.



INTERESTING CASE

 S_1 and S_2 are separated by $M\lambda$ and D (your ear) moves along line joining S_1 and S_2 .

$${}^{x}S_{1}$$
 ${}^{x}D$

a) When D is at S_1 :

$$x_1 = 0$$

$$x_2 = M\lambda$$

$$(x_1 - x_2) = -M\lambda$$

b) When D is at Mid-point:

$$x_1 = x_2 = \frac{M\lambda}{2}$$

$$(x_1 - x_2) = 0$$

MAX

c) When D is at S_2 :

$$x_1 = M\lambda$$

$$x_2 = 0$$

$$(x_1 - x_2) = M\lambda$$

MAX

In all you hear (2*M*+1) Maxima In between where will be 2*M* minima

N.B. CRUCIAL QUANTITY IS PATH DIFFERENCE!!!