

6.3 Exotic contributions to $g - 2$. Any particle that couples to the electron can produce a correction to the electron-photon form factors and, in particular, a correction to $g - 2$. Because the electron $g - 2$ agrees with QED to high accuracy, these corrections allow us to constrain the properties of hypothetical new particles.

- (a) The unified theory of weak and electromagnetic interactions contains a scalar particle h called the *Higgs boson*, which couples to the electron according to

$$H_{\text{int}} = \int d^3x \frac{\lambda}{\sqrt{2}} h \bar{\psi} \psi.$$

Compute the contribution of a virtual Higgs boson to the electron ($g - 2$), in terms of λ and the mass m_h of the Higgs boson.

- (b) QED accounts extremely well for the electron's anomalous magnetic moment. If $a = (g - 2)/2$,

$$|a_{\text{expt.}} - a_{\text{QED}}| < 1 \times 10^{-10}.$$

What limits does this place on λ and m_h ? In the simplest version of the electroweak theory, $\lambda = 3 \times 10^{-6}$ and $m_h > 60$ GeV. Show that these values are not excluded. The coupling of the Higgs boson to the muon is larger by a factor (m_μ/m_e): $\lambda = 6 \times 10^{-4}$. Thus, although our experimental knowledge of the muon anomalous magnetic moment is not as precise,

$$|a_{\text{expt.}} - a_{\text{QED}}| < 3 \times 10^{-8},$$

one can still obtain a stronger limit on m_h . Is it strong enough?

- (c) Some more complex versions of this theory contain a pseudoscalar particle called the *axion*, which couples to the electron according to

$$H_{\text{int}} = \int d^3x \frac{i\lambda}{\sqrt{2}} a \bar{\psi} \gamma^5 \psi.$$

The axion may be as light as the electron, or lighter, and may couple more strongly than the Higgs boson. Compute the contribution of a virtual axion to the $g - 2$ of the electron, and work out the excluded values of λ and m_a .