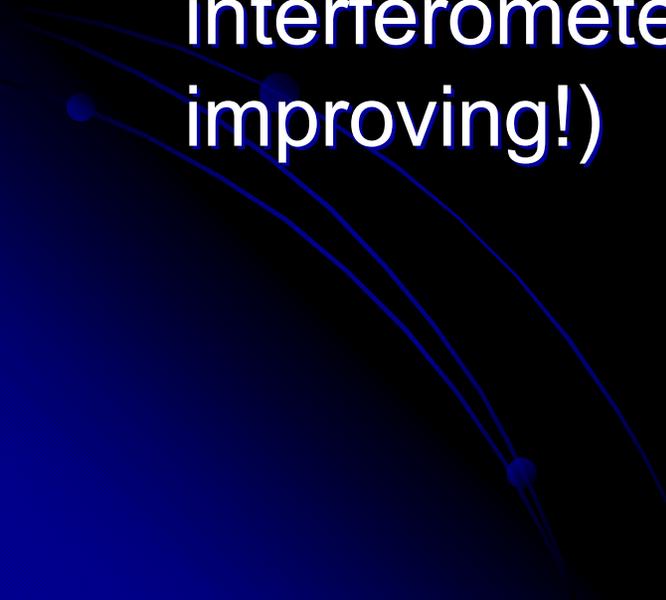


# Astrophysical Stochastic Gravitational Waves

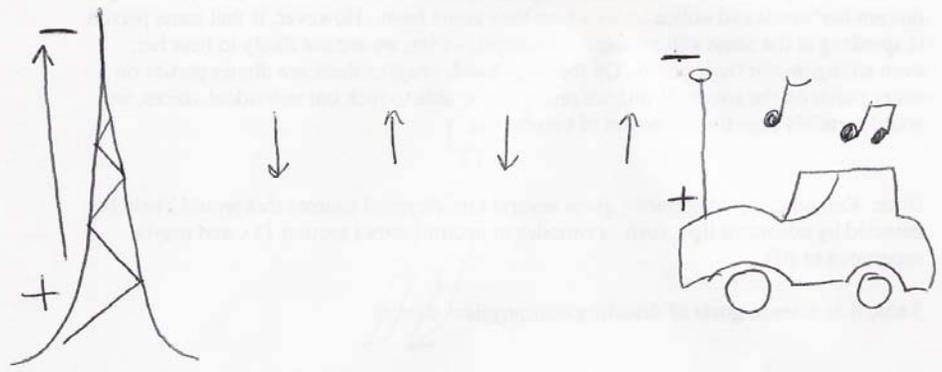
Jonah Kanner – PHYS 798G – March 27, 2007



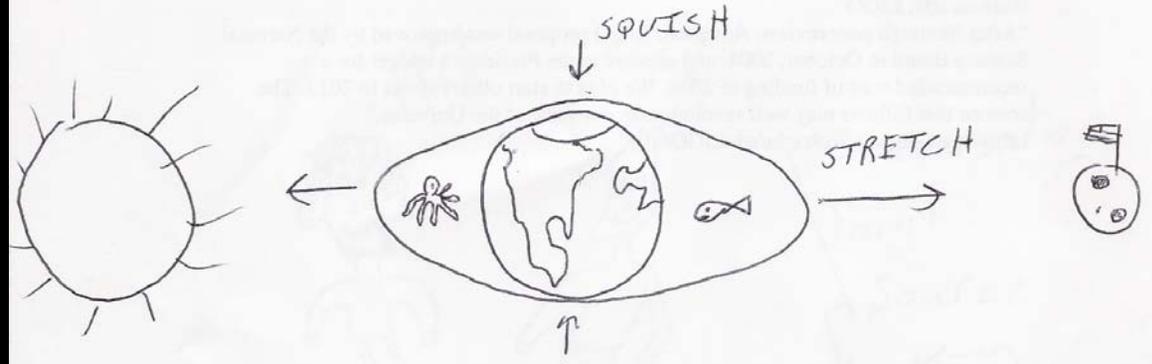
# Introduction

- Gravitational Waves come from space
  - Require acceleration of dense mass  
(Think black holes and neutron stars!)
  - Will be detected with resonant bars and interferometers (both exist and are improving!)
- 

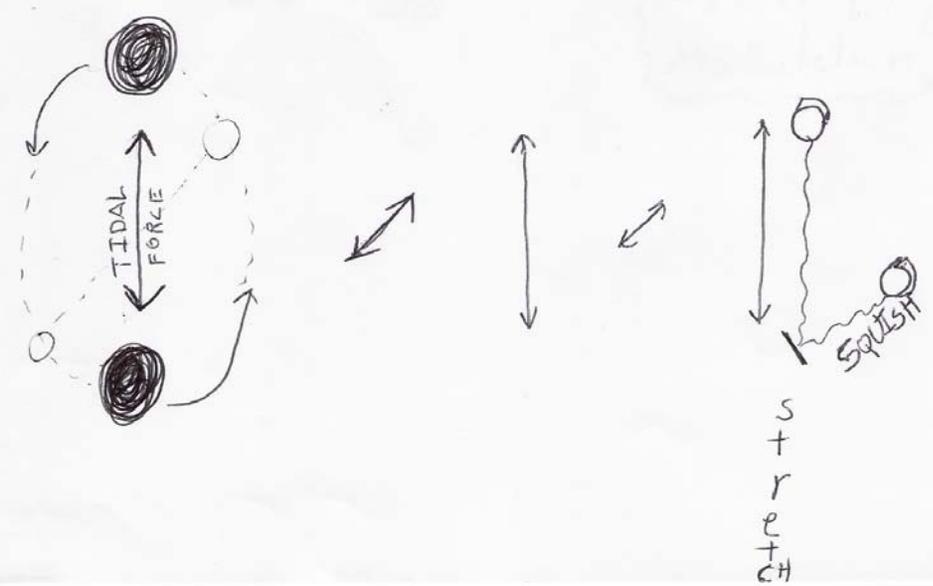
E-M Waves come from moving charges, flipping field lines back and forth.



Gravitational quadra-pole fields lead to tidal forces. The "tidal forces" describe the field – ocean not required!



GWs come from moving masses, flipping a tidal stretch back and forth across 2 orientations.



Bang!

GW WAVES

wa-wa-wa-  
wa-wa

Fizzzzzzzzzzzzzz

Bursts

Periodic

Stochastic

Supernova  
Coalescing  
Compact  
Binaries

Rotating  
NS  
Stable  
Orbiting  
Binaries

Astrophysical

Cosmological

Collection  
of many  
distant,  
unresolvable  
periodic and  
burst  
sources

GW signal  
from  
the very early  
universe -  
analogue of  
CMB in E&M  
radiation

# Introduction

- Current detectors measure mainly  
~50-3000 Hz  
(In band of human hearing!)

Merger (burst)



Inspiral  
(~periodic)



SN  
Stochastic  
(popcorn)



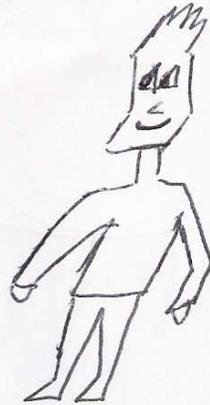
<http://www.ligo.caltech.edu/~mours/bh-no-noise.au>

<http://www.physics.uwa.edu.au/~coward/SIMULATION.htm>

<http://gmunu.mit.edu/sounds.html>

Hi!

Hi!



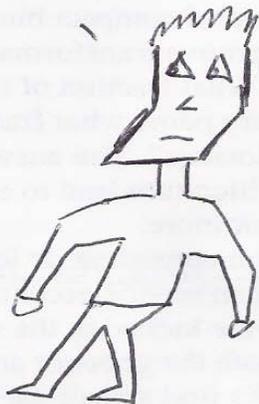
Conversation  
Point

Source

Amp, Freq,  
Modulation

o Blah  
/

Hello ???



Point  
Source  
Too Far  
Away



# What is the Astrophysical Background???

- What: Many point sources overlapping in time
- Quick Math: Imagine a spherical shell
  - Number of sources/shell  $N \sim r^2$
  - Amplitude per source  $A \sim 1/r$
  - Net Amp  $\sim$  Random Walk  $\sim A \cdot \sqrt{N} \sim$  CONSTANT!

Result: A background fuzz from redshift  $z \sim 1-5$

# Characterization

- Omega!!!!!!

$\Omega(f)$  is roughly the normalized energy density in a given frequency band of the stochastic background

$$\int \Omega(f) d(\ln(f)) = \rho_{\text{GW}}/\rho_c$$

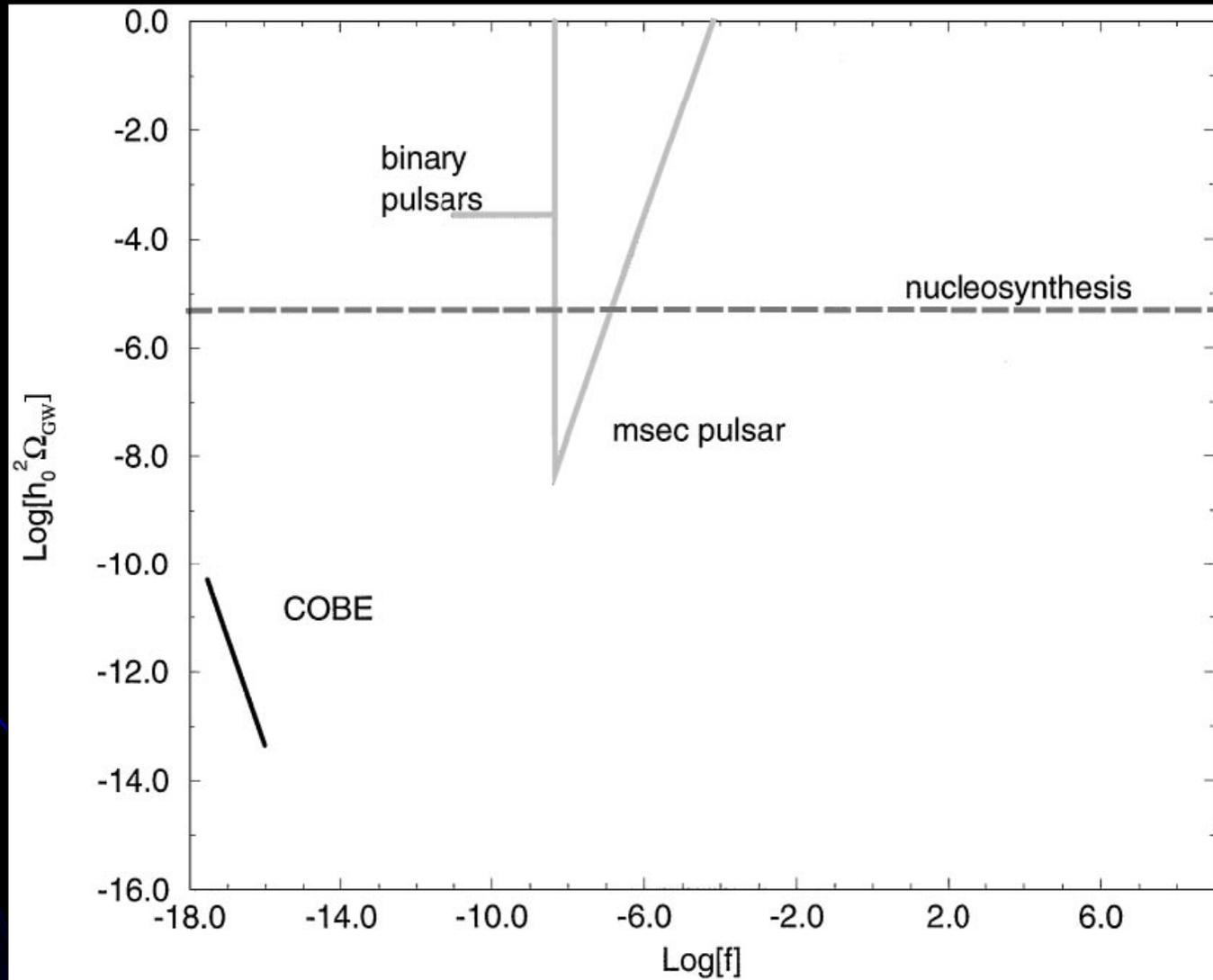
In the same sense that a single temperature (2.7 K) completely describes the CMB, omega completely describes the GW background if it's stationary, Gaussian, and isotropic

Convention: Bound  $\Omega_0$

# Measurement - Indirect

The nucleosynthesis bound applies only to Cosmological signals

For high freq, it's a wide open field!



# Measurement – IFO's & Bars

- LIGO, TAMA, GEO, VIRGO
- Bar Detectors
- Advanced Detectors (LIGO, VIRGO) ~ 2013



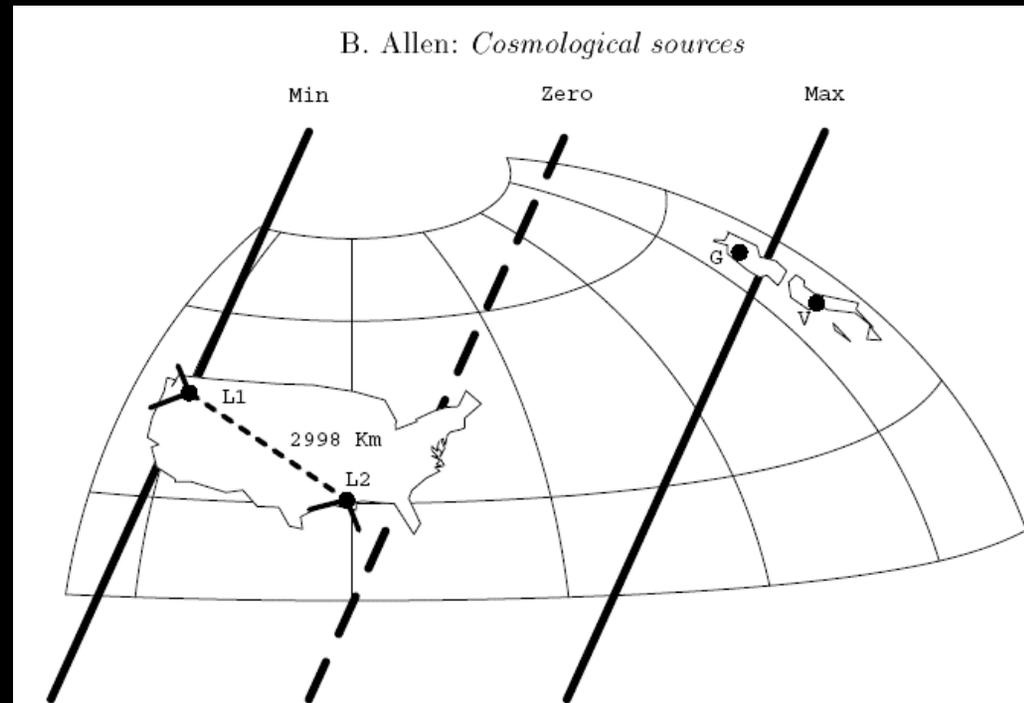
Current bound on  $\Omega$  of about  $10^{-5}$  at 50-150 Hz  
Bounds around  $10^{-9}$  from “adv” IFOs (50-150Hz)  
Bars + IFOs for higher frequency bounds

# Measurement

- Cross Correlation

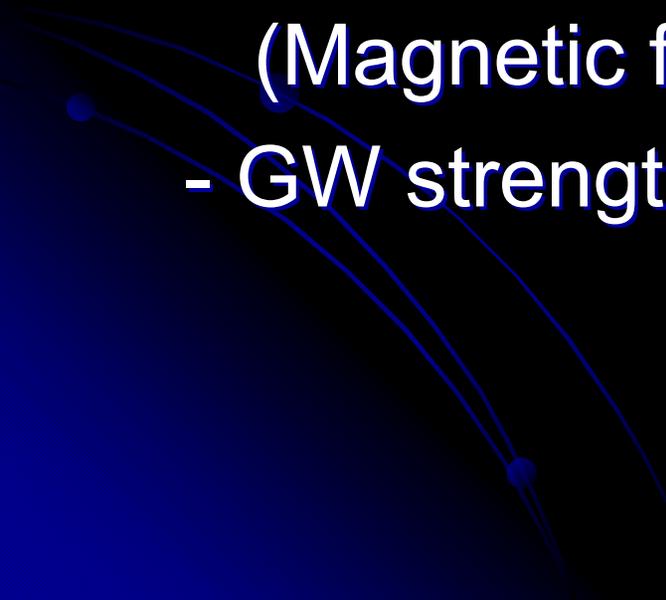
Idealization (IFOs at same place):  $\int s_1(t) s_2(t) dt$

Limitation: IFOs are usually not in the same place!! Wavelengths much shorter than 3000 km (100 Hz) will get “washed out” of cross correlation for L1-H1 pair



# Sources

## Estimation

- Star Formation Rate (SFR)
  - Galactic Population Properties  
(Magnetic fields, freq, masses, etc...)
  - GW strength per source
- 

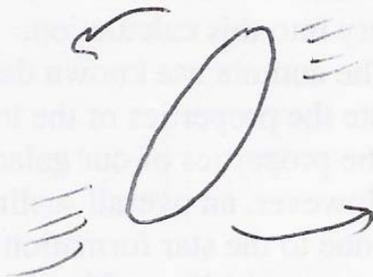
# Eccentric Neutron Stars



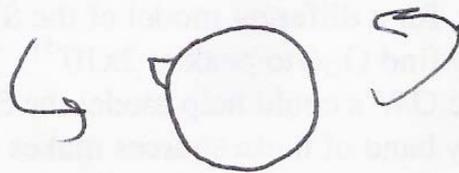
- Eccentricity may be any asymmetry with respect to axis of rotation (potato or mt.)
- Use pulsar data to make estimates on the properties of the spinning neutron star population (also LMXB's and HMXB's)
- $\epsilon$  is difficult to estimate – existing upper bounds, but hard to get a good value

Spinning Potato

NS



NS



with  
Mountain

# Eccentric Neutron Stars



- T. Regimbau and J. A. de Freitas Pacheco estimate  $\Omega$  between  $10^{-9}$  and  $10^{-11}$
- Assume  $\varepsilon = 10^{-6}$  (?)
  - Wide range of  $\Omega_0$  comes from different models of SFR (corresponding to different models of cosmic dust)
  - Freq  $\sim 1$ -1.5 kHz (from pulsar freq.)

# Eccentric Neutron Stars



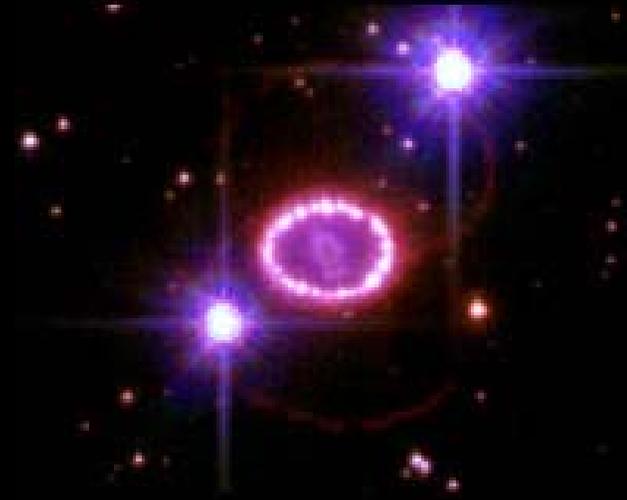
Not promising for IFO alone (high freq!)

--Bars + IFO might do it

R-modes might do better

Tough estimate! Measurement probes SFR

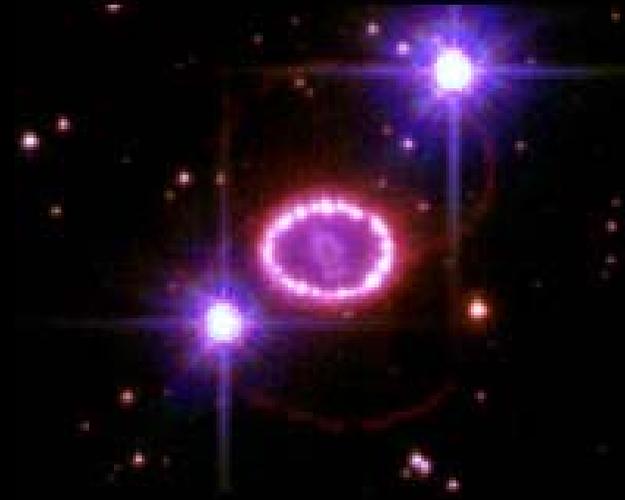
# Supernovas (ka-pow!)



David M. Coward, P Ronald R. Burman and David G. Blair consider NS forming SN

SN still not well understood – authors consider a mix of three different models – GW production depends on asymmetry of simulation

# Supernovas (ka-pow!)



- Popcorn noise
- Get  $\Omega$  about  $10^{-12}$  peaked at 200-300 Hz
- With BH forming SN, could be closer to  $10^{-10}$

# Neutron Star Coalescence



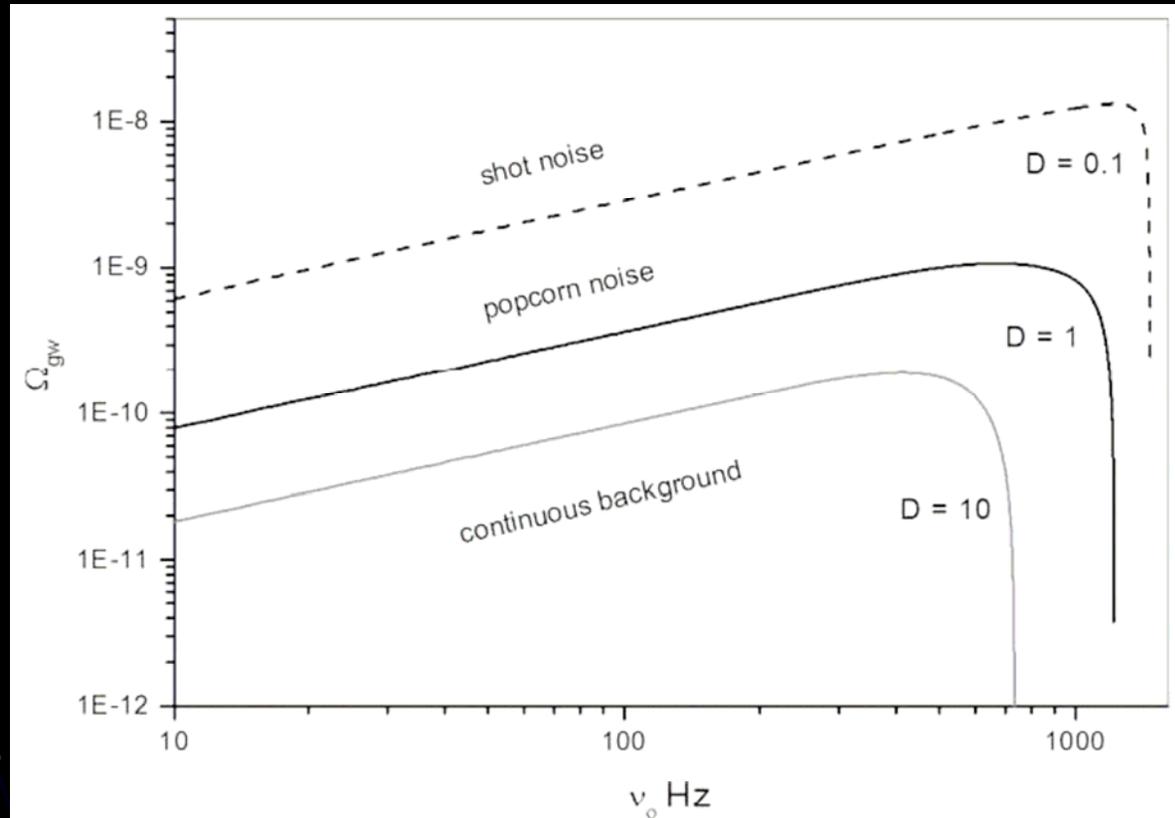
- Hard things to estimate: What fraction of massive stars exist as binaries??
- Of those, what fraction are binaries after 2 SN's ??
- Can use eccentricity of pulsar orbits to estimate “kick” from SN

# Neutron Star Coalescence



T. Regimbau and J. A. de Freitas Pacheco

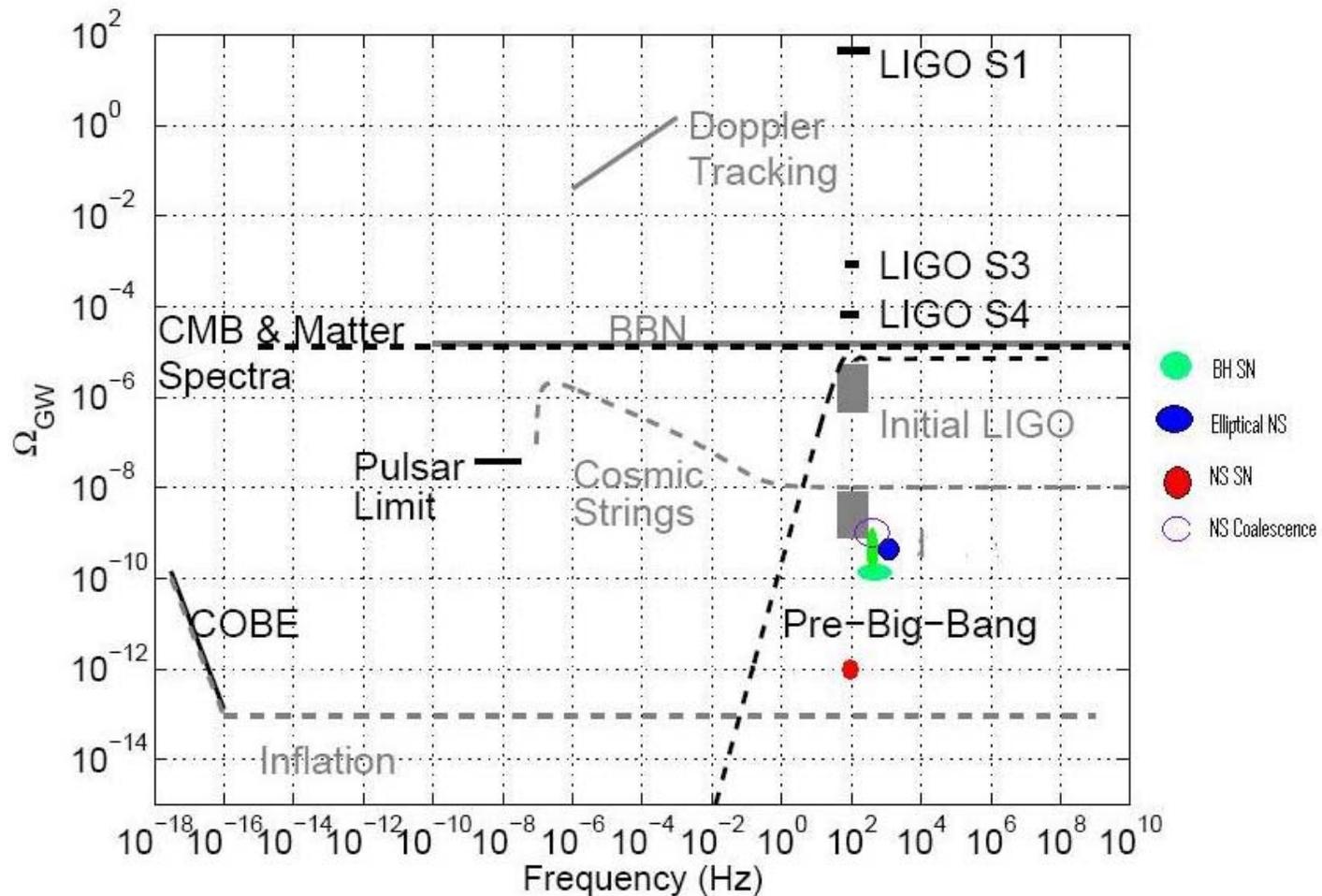
Should be visible by  
Advanced IFOs



# Science

- Probe the SFR (clear up the dust issue)
- Snapshot of universe,  $z \sim 1-5$
- Rates of supernovas, mass and angular momentum distributions of compact objects, and ratios between formation of black holes and neutron stars, etc.
- Astrophysical Stochastic signal may have to be understood and removed to see Cosmological signal

# A Rough Sketch



# References

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- Binary NS image  
<http://chandra.harvard.edu/photo/2005/grb050709/animations.html>
- Ns image  
<http://www.astro.cf.ac.uk/groups/relativity/research/part13.html>

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