

angular equation

$$\hat{L}^2 Y(\theta, \phi) = \hbar^2 l(l+1) Y(\theta, \phi) \Rightarrow Y_l^m(\theta, \phi) = \text{spherical harmonics}$$

$$l = 0, 1, 2, \dots$$

$$m = -l, -l+1, \dots, l-1, l$$

radial equation

$$\left[\frac{\hat{p}_r^2}{2M} + V(r) + \frac{\hbar^2 l(l+1)}{2Mr^2} \right] R(r) = E R(r)$$

change of variables: $R(r) = \frac{u(r)}{r}$

$$\left[\frac{\hbar^2}{2M} \left(\frac{1}{r} \frac{d}{dr} r \right) \left(\frac{1}{r} \frac{d}{dr} r \right) \frac{u}{r} + V(r) \frac{u}{r} + \frac{\hbar^2 l(l+1)}{2Mr^2} \frac{u}{r} \right] = E \frac{u}{r}$$

$$\frac{1}{r} \frac{d^2}{dr^2} u$$



$$\left[-\frac{\hbar^2}{2M} \frac{d^2}{dr^2} + V(r) + \frac{\hbar^2 l(l+1)}{2Mr^2} \right] u(r) = E u(r)$$

↑
centrifugal barrier

$V_{\text{eff}}(r)$