

Department of Physics
University of Maryland, College Park

Assignment 10, Physics 374 — Due Thursday, May 6, 2010

Note: In solving math problems, you have to provide the details of intermediate steps. Without those steps, you cannot get full credit.

Problem 1 In calculating the Green's function for the Schrodinger equation in 3D, we encounter the following 3D integral,

$$I(\vec{r}) = \frac{1}{(2\pi)^3} \int d^3\vec{k} e^{i\vec{k}\cdot\vec{r}} e^{i\hbar\vec{k}^2 t/2m} \quad (1)$$

Evaluate the above integral as a product of three one-dimensional integrals.

Problem 2

Consider the one-dimensional Green's function equation for G ,

$$\frac{\partial G(t, t')}{\partial t} + \beta G(t, t') = \delta(t - t') \quad (2)$$

Consider solving G with two different boundary conditions. And show that the difference of the two Green's functions is a solution of the homogenous equation. [Hint: consider G vanishes before $t = t'$ and after $t = t'$ separately.]

Problem 3

Consider the Helmholtz equation in 2D

$$\frac{\partial^2 \psi}{\partial x^2} + \frac{\partial^2 \psi}{\partial y^2} + k^2 \psi = 0 \quad (3)$$

in a rectangular box with length L_x in the x-direction and L_y in the y-direction. Therefore, x and y coordinates are limited to $(0, L_x)$ and $(0, L_y)$, respectively. If ψ vanishes at the boundary of the box, calculate the normal modes for the system.

Problem 4

Consider the normal modes of a drum in Sec. 20.2. Show that the different normal modes are orthogonal to each other. Using the trick that I have shown you in the lecture.

Problem 5

Derive a completeness relation for the normal modes on a drum by expanding a function $f(r, \theta)$ in terms of the normal modes.