

**PHYS 373 (Spring 2015): Mathematical Methods for
Physics II**
Final exam: Monday, May 18, 10.30 am.-12.30 pm.

Read the instructions below and do *not* flip to next page till you are told to do so.

Name:

Student ID:

Useful formulae:

$f(x) = \frac{a_0}{2} + \sum_1^\infty \left(a_n \cos \frac{n\pi x}{l} + b_n \sin \frac{n\pi x}{l} \right)$	$f(x) = \sum_{l=0}^\infty c_l P_l(x)$	$f(x) = \sum_{-\infty}^\infty c_n e^{in\pi x/l}$
$P_l^m(x) = (1-x^2)^{m/2} \frac{d^m}{dx^m} P_l(x)$	$a_n = \frac{1}{l} \int_{-l}^l f(x) \cos \frac{n\pi x}{l} dx$	$P_3(x) = \frac{1}{2} (5x^3 - 3x)$
$\int_0^1 x J_p(\alpha x) J_p(\beta x) dx = 0 \quad (\alpha \neq \beta)$	$b_n = \frac{1}{l} \int_{-l}^l f(x) \sin \frac{n\pi x}{l} dx$	$P_1(x) = x$
$c_m = \frac{2m+1}{2} \int_{-1}^1 f(x) P_m(x) dx$	$\frac{\partial u}{\partial x} = \frac{\partial v}{\partial y}, \quad \frac{\partial v}{\partial x} = -\frac{\partial u}{\partial y}$	$P_0(x) = 1$
$f(z) = f(x+iy) = u(x,y) + iv(x,y)$	$J_{p-1}(x) - J_{p+1}(x) = 2J'_p(x)$	$J_0(0) = 1$
$\frac{d}{dx} \left[x^{-p} J_p(x) \right] = -x^{-p} J_{p+1}(x)$	$N_n(0) = \infty$	$J_{n \neq 0}(0) = 0$
$\frac{\partial^2}{\partial x^2} T(x,y) + \frac{\partial^2}{\partial y^2} T(x,y) = 0$	$T = \left\{ \begin{matrix} e^{kx} \\ e^{-kx} \end{matrix} \right\} \left\{ \begin{matrix} \sin ky \\ \cos ky \end{matrix} \right\}$	$\text{or } \left\{ \begin{matrix} \sin kx \\ \cos kx \end{matrix} \right\} \left\{ \begin{matrix} e^{ky} \\ e^{-ky} \end{matrix} \right\}$
$R(z_0) = z \lim_{z \rightarrow z_0} (z - z_0) f(z)$	$g(\alpha) = \frac{1}{2\pi} \int_{-\infty}^\infty f(x) e^{-i\alpha x} dx$	$J_n(\infty) = 0$
$\frac{d^2}{dt^2} G(t,t') + \omega^2 G(t,t') = \delta(t-t')$ for (residue of $f(Z)$ at $Z = \infty$) =	$y'' + \omega^2 y = f(t)$ - (residue of $\frac{1}{z^2} f\left(\frac{1}{z}\right)$ at $z = 0$)	$y_0 = y'_0 = 0$ $\int_{t_0-\epsilon}^{t_0+\epsilon} \delta(t-t_0) dt = 1$
$\int_{-\infty}^\infty \frac{P(x)}{Q(x)} e^{imx} \text{ (around } C, \text{ with } m > 0) =$	$2\pi i \cdot \text{sum of residues of } \frac{P}{Q} e^{imz}$	$\text{in upper half-plane}$
$\delta(t-t_0) = 0, \text{ for } t \neq t_0$	$P_l(x) = \frac{1}{2^{l l }} \frac{d^l}{dx^l} (x^2 - 1)^l$	$\int f(z) dz = 0, \text{ around } C$
$ax^2 + bx + c = 0 \rightarrow$	$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$	$R(z_0) = \frac{g(z_0)}{h'(z_0)}, \text{ if } f = \frac{g}{h}$

It is necessary to show the details of the derivation and not just the final answer for *all* problems.

This is a closed book exam: crib sheets are not allowed.

In case they are needed, more blank paper and staples are provided.

Please write clearly and if you use the backside of a page, then please indicate so.

Check that there are total of 8 *pages* (2 cover pages + 6 problems).

Note that some problems have *multiple* parts; so, please read the statement of each problem carefully.

Remember the honor pledge that you signed at the start of the semester.

Problem #	Points scored	Maximum points
1		8
2		15
3		10
4		10
5		11
6		11
Total		65