

HW# 3 -Phys273-Spring 2003  
Due Tuesday, Feb. 25, 2003, by 9am

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**Problem 1.** [10 points]

- a) Solve the differential equation  $y'' + 4y = 0$  for the following initial conditions
- $y(0) = 0, y(\pi/4) = 1$
  - $y(\pi/2) = -1, y'(\pi/2) = 1$
  - $y(0) = 0, y'(0) = 1$
  - $y(\pi/4) = a, y''(0) = b$
- b) Solve the differential equation  $y'' + y = 2y'$  with the boundary conditions  $y(0) = 1, y(1) = 1$

**Problem 2.** [10 points]

Solve the following homogeneous differential equations with an exponential ansatz and determine the most general solution. In case that the solution is complex, determine the corresponding real solution

- $2y'' - 12y' + 10y = 0$
- $4y'' - 12y' + 9y = 0$
- $y'' + 2y' + 5y = 0$

**Problem 3.** [10 points]

A mass  $m$  is subject to a resistive force  $F = -bv$ , where  $b$  is a constant and  $v$  is the velocity but no restoring force.

- a) Show, that the displacement as a function of time takes the form  $x = C - \frac{v_0}{\gamma} e^{-\gamma t}$ , where  $\gamma = \frac{b}{m}$ . To show this, use the method used in class to solve the damped oscillator. That is, assume the displacement as a function of time takes the form  $x(t) = e^{\alpha t}$ , plug into the equation of motion and solve for possible values of  $\alpha$ . Check, if you have the right number of free constants in your solution.
- b) At  $t = 0$  the mass is at rest at  $x = 0$ . At this instant a driving force  $F = F_0 \cos(\omega t)$  is switched on. Find the values of  $A$  and  $\delta$  in the steady state solution  $x(t) = A \cos(\omega t - \delta)$ .
- c) Write down the general solution (the sum of parts (a) and (b) of this problem) and find the values of  $C$  and  $v_0$  from the initial conditions that  $x = 0$  and  $x' = 0$  at  $t = 0$ . Sketch  $x$  as a function of  $t$ .

[10 points]