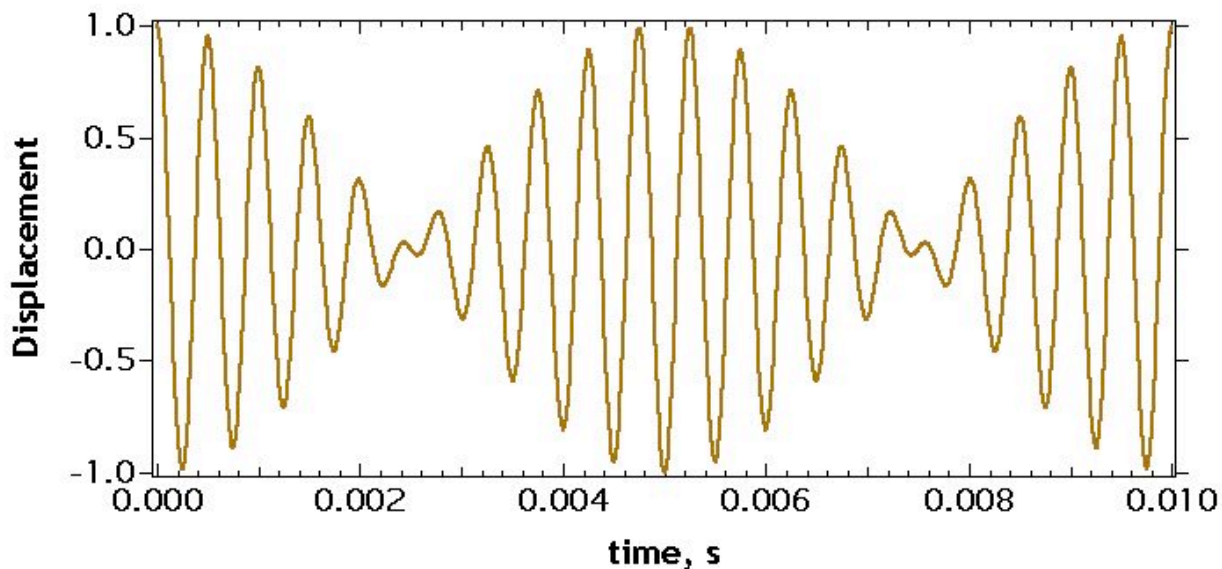


Closed-book examination. One pre-prepared 8 1/2" x 11" sheet of notes may be used. Calculator may be used. Show work for partial credit. Include UNITS on all answers.

EXAM ADVICE: If you don't immediately see what to do on one problem, go on to the next problem and come back to the unfinished problems later.

- (30 points) 1. Determine as quantitatively as possible the periods present in the sum wave shown, and use the estimates to find the frequencies,  $f_1$  and  $f_2$ , of the two cosine waves that were summed to produce the wave.



**(35 points)** 2. Consider a series RL circuit with a resistor R and an inductor L driven by an AC source of voltage  $V_0 \cos(\omega t)$ . You must show the reasoning and derivations completely and clearly to obtain credit. *Continue work on the blank sheet following this page if needed.*

- a) Draw the circuit and write the equation for the voltage drop across each component. What is the differential equation describing  $I(t)$ , the current in the circuit?
- b) Rewrite the differential equation from part a) using imaginary voltage and current functions,  $\hat{I}$  and  $\hat{V}$ , such that  $V = \text{Re}(\hat{V})$  and  $I = \text{Re}(\hat{I})$ , and  $\hat{V} = V_0 e^{i\omega t}$ ,  $\hat{I} = \hat{I}_0 e^{i\omega t}$ . Solve for  $\hat{I}_0$  and take the real part to find I. Give the expression for the phase difference between the current and the AC voltage source.
- c) Write expressions for the voltage drop across the resistor and the inductor. Given  $\omega = 130$  kHz,  $L = 0.50$  H,  $V_0 = 12$  V, and  $R = 65 \text{ k}\Omega$ , find the phase shift of the voltage drop across the resistor, and find the phase shift of the voltage drop across the inductor.



**(35 points)** 3. A transverse sinusoidal wave on a taut wire has an amplitude of 2 mm and a wavelength of 1.22 m. The wave speed is 180 m/s. The wave is traveling in the positive x direction, and the displacement is in the y direction. *Continue your work on the blank sheet following this one if needed.*

- a) Write the function  $y(x,t)$  describing the motion of the wave assuming that the displacement is  $y = 1\text{ mm}$  at  $x=0$  and  $t=0$ . Give numerical values with units for all the parameters in  $y(x,t)$ . Find the value of the tension in the wire given a linear density of  $2.45 \times 10^{-2} \text{ kg/m}$ .
- b) Find the maximum vertical speed of the wire. Consider the position  $x = 2.0 \text{ m}$  and find the first time after  $t=0$  at which the vertical speed of the wire is zero.
- c) Find the value of the maximum energy per unit length at any one position along the string. Carefully draw a graph of the displacement vs. time and the energy vs. time at  $x = 0.0 \text{ m}$ . Label your axes quantitatively.

