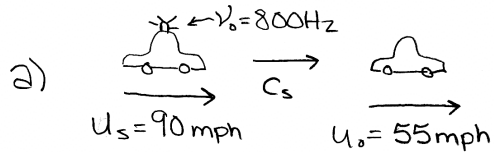


#4 Ch 8 #1



$$c_s = 90 \text{ mph} = 90 \left(\frac{1610 \text{ m}}{1 \text{ mile}} \right) \left(\frac{1 \text{ hour}}{3600 \text{ s}} \right) = 40.3 \text{ m/s}$$

$$u_o = 55 \text{ miles/hour} \left(\frac{1610 \text{ m}}{1 \text{ mile}} \right) \left(\frac{1 \text{ hour}}{3600 \text{ s}} \right) = 24.6 \text{ m/s}$$

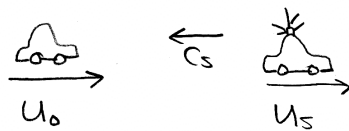
both source and observer are moving, use (8.7)

$$\nu' = \frac{c_s - u_o}{c_s - u_s} \nu_0$$

\leftarrow speed of observer
 \leftarrow unshifted frequency
 \uparrow speed of source
 \uparrow speed of sound

$$= \frac{340 \text{ m/s} - 24.6 \text{ m/s}}{340 \text{ m/s} - 40.3 \text{ m/s}} (800 \text{ Hz}) = 842 \text{ Hz}$$

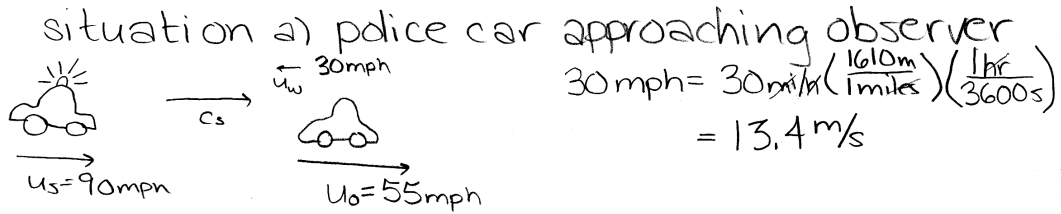
b)



now the source is getting further away instead of approaching. The velocity of the two cars is opposite the direction of the two cars. Thus the signs in Eq (8.7) must be flipped.

$$\nu' = \frac{c_s + u_o}{c_s + u_s} \nu_0 = \frac{340 \text{ m/s} + 24.6 \text{ m/s}}{340 \text{ m/s} + 40.3 \text{ m/s}} (800 \text{ Hz}) = 767 \text{ Hz}$$

#5 (ch 8 #2)



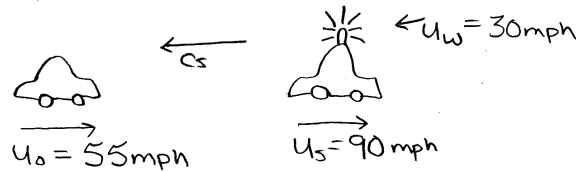
$$30 \text{ mph} = 30 \frac{\text{mi}}{\text{hr}} \left(\frac{1610 \text{ m}}{1 \text{ miles}} \right) \left(\frac{1 \text{ hr}}{3600 \text{ s}} \right) = 13.4 \text{ m/s}$$

In this case, the wind is opposing the direction of propagation of the sound, effectively decreasing the sound velocity

$$\nu' = \frac{c_s + (-u_w) - u_o}{c_s + (-u_w) + u_s} \nu_0 = \frac{340 \text{ m/s} - 13.4 \text{ m/s} - 24.6 \text{ m/s}}{340 \text{ m/s} - 13.4 \text{ m/s} - 40.3 \text{ m/s}} (800 \text{ Hz}) = 844 \text{ Hz}$$

negative because it opposes the sound velocity

situation b) police car moves away from observer



now, the wind is moving in the same direction as the sound, so the wind makes the sound carry faster because the wind velocities and the sound velocities add.

$$\nu' = \frac{c_s + u_s + u_o}{c_s + u_s + u_s} = \frac{340 \text{ m/s} + 13.4 \text{ m/s} + 24.6 \text{ m/s}}{340 \text{ m/s} + 13.4 \text{ m/s} + 40.3 \text{ m/s}} (800 \text{ Hz}) = 768 \text{ Hz}$$

$$8-4. \quad v = \frac{c_w + v}{c_w - v} v_0$$

$$\Delta v = v - v_0 = \frac{2v}{c_w - v} v_0$$

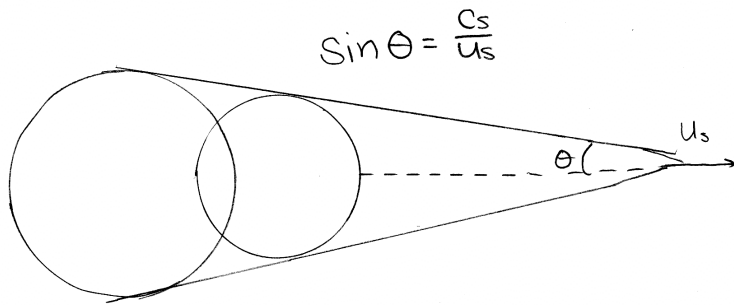
$$\Rightarrow v = \frac{\Delta v c_w}{2v_0 + \Delta v} = \frac{3 \times 340}{2 \times 800 + 3} \approx 0.64 \text{ (m/s)}$$

#6 Chap. 8 #5

$$u_s = 500 \text{ m/s}$$

$$c_s = 340 \text{ m/s}$$

$$\theta = \sin^{-1}\left(\frac{340}{500}\right) = 42.8^\circ$$



#7 Chap 8 #8

$$a) \nu' = \frac{1+\beta}{\sqrt{1-\beta^2}} \nu_0 \quad \beta = \frac{u}{c}$$

$$c = \lambda_0 \nu_0 \quad c = \lambda' \nu'$$

$$\frac{c}{\lambda'} = \frac{1+\beta}{\sqrt{1-\beta^2}} \frac{c}{\lambda_0} \quad \frac{\lambda_0}{\lambda'} = \frac{1+\beta}{\sqrt{1-\beta^2}} \quad \left(\frac{\lambda_0}{\lambda'}\right)^2 = \frac{(1+\beta)^2}{1-\beta^2} = \frac{(1+\beta)^2}{(1+\beta)(1-\beta)}$$

$$\left(\frac{\lambda_0}{\lambda'}\right)^2 (1-\beta) = 1+\beta \quad \left(\frac{\lambda_0}{\lambda'}\right)^2 - 1 = \beta \left[1 + \left(\frac{\lambda_0}{\lambda'}\right)^2\right]$$

$$\beta = \frac{\left(\frac{\lambda_0}{\lambda'}\right)^2 - 1}{\left(\frac{\lambda_0}{\lambda'}\right)^2 + 1} = \frac{\left(\frac{5500}{6500}\right)^2 - 1}{\left(\frac{5500}{6500}\right)^2 + 1} = \frac{-0.284}{1.716} = -0.166$$

$$u = \beta c \Rightarrow u = 0.166c$$

b) The negative sign tells us it's receding. Intuitively, if something is moving away, the peaks would appear to be moving apart to an observer, which means the frequency is getting lower. Looking at a diagram of the em spectrum lowering the frequency makes visible light more red.