we have been studying systems which are governed by the classical wave equation.

Vp is the "phase velocity", which is the speed at which a point peak or trough in the ware will travel.

The normal modes are the harmonic solutions to this equation. They are

y(x) = Aeikx (when there are no boundary Conditions, Kij continuous)
with associated frequency

w= KVp

mode is

$$y_n(x,t) = (Ae^{ikx})e^{i\omega t} = Ae^{i(kx+\omega t)}$$

We can explicitly confirm that this satisfies the ernation of motion.

$$\frac{2^{3}}{2x^{2}} = -k^{2}Ae^{i(kx+\omega t)}$$

$$\frac{2^{2}}{2t^{2}} = -\omega^{2}Ae^{i(kx+\omega t)}$$

Substitute into Eq. of motion: - KAcilkx+wt) = 12 Allen Vi (-wAcilkx+w+) 4cp - K2 = - cs2 $V_p = \frac{\omega}{k}$ We see that the normal mode Ae i(kx+w+) is a solution, as long as the phase velocity is w/k. We can rewrite they condition. W= Vpk This equation describes all the physics of this system. We can think of this equation as telling us how the normal mode frequency (w) depends on the normal mode wan humber (k): $cw(k) = V_p k$ 1 linear dependence. normal mode Frequency depends on the war number. It mex year that there win K slope up

It may seem like there is no other possible relationship between cur and k, but this particular linear relationship only holds true for the classical wave equation. If any other equation of motion is used, then in general there will be some other relationship between cu and k.

An example is the loaded string. For that system, I'm normal mode Frequences are

We can re-write this as an w(k) function:

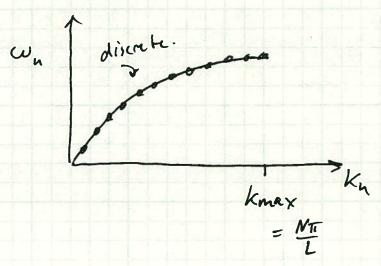
NE MOR

$$\omega_n = 2\omega_0 \sin\left(\frac{n\pi l}{2(N+1)l}\right) = 2\omega_0 \sin\left(\frac{m\pi l}{2L}\right)$$

nous Kn = NII , so we can re-unite as

when a goes from 1 to N.

This is a non-linear relationship between Kn and wn



The reason why this system does not have a linear relationship between co & k is because its equation of motion is not the simple classical wave Equation Its equation is

yp + Zwoyp - ω (γρ+1 + γρ-1) = 8

In general, the relationship between co 4 k is determined by the equation of motion, which is determined by the physics of the system

Notice that when MAN N -> 00, the loaded string becomes a continuous sex string woods.

This is equivalent to zooming-in on the linear part of the equation near $k_0 = \emptyset$.

For any the system, the relationship between co and k is called the "dispersion relation"
and and it is called the "disseries what and
co ach is to ever the dispersion relation
The classical wave equation has a <u>linear</u>
dispersion relation:
) (a) (k) = 1 k (lives diseases acted
(Classical wave equetton)
(Classical wave equation)
where, the loaded string has a non-linear dispersion
Melation:) w(kg) = Zwo Sin (knl) = non-linear despersion pelation
despersion pelation
(loaded string)
A system which has a linear dispersion relation
has a special propertie: A propagating pulse
will travel vithout changing its shape: pulse shape at +=0
pulse shape
Palse a top
at +=0
We can show this as follows. The pulse
can be described as a sum over normal modes.
But The normal modes are continuous, so the
Turn over normal modes is a Fourier Transform:
$y(x,t) = \begin{bmatrix} 1 \\ 12\pi \end{bmatrix} dK A(K) e e \\ 12\pi \end{bmatrix} Mormel its frequency sum over its conficient.$
12TT an ich e
normal Frequency
sum over
11 wast.

$$y(x_1+) = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} dk A(k) e^{i(kx-\omega +)}$$

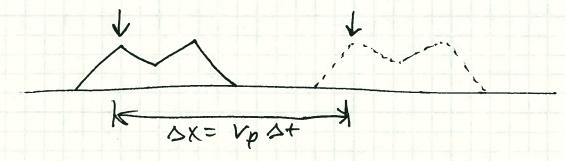
Now suppose that the system has a linear dispersion relations

w=VpK m

Then we have
$$y(x_1t) = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} dk \ A(k) e^{i(k(x-v_pt))}$$

$$= \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} dk \ A(k) e^{ik(x-v_pt)}$$

This says that as time goes forward, if we keep advancing X at spred Up, then the value of y will stay the same. So the shape of the pulse does not Change



Therefore, if w= VK for the system, then pulses do not disperse. They maintain their shape. A linear dispersion relation means that pulses of do not disperse.

This is a special case behavior for systems with linear dispersion relations. But suppose that un have a non-linear dispersion relation. For example, suppose

wantem mechanics who describing a free particle. In that case,

cu= tk2
2m.

How does a pulse propagate in a sy, ten like this? $y(x,t) = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} dk \ A(k) e^{ikx} -i(\frac{k}{\sqrt{2\pi}}) + \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} dk A(k) e^{ikx} -i(\frac$

Here, as time goes forward, we need to

advance X at a speed of $v_p = \frac{\pi k}{2m}$ to keep the argument of the exponential the summe.

But the speed vp = the is different for every Monash warmumber (k). That is, each normal mode as advances at its own velocity, they do not advance together. This means that the various normal modes will disperse; with some travelling slowly, and the pulse will disseppear

C	onside	a p	erfect	travel	ing w	ave j	wavelent period	5 7
5			\int	1	A	$-\int$	time 4	×
A+ on	e locati	dn, sqy	x=0,	jas T-	time.	goes	forward.	tin
							mod is	
13.	t a	speed	V=	$\frac{\lambda}{T} = -$	(天) (罢)	+ w w	ave ad W K efinition	au
T	ni) is						etinition ution	

Or, if the physical system is electromagnetic waves in bacuum, then

X = Mo Eo

Let's guess a travelling wave solution to the classical wave equation:

y(x,+) = A e i(kx-w+)

What requirements does this place on k & cu?

Let's substitute:

$$\frac{\partial^2 y}{\partial x^2} = -k^2 \left(A e^{i(kx-\omega t)} \right)$$

$$\frac{\partial^2 y}{\partial t^2} = -\omega^2 \left(A e^{i(kx-\omega t)} \right)$$

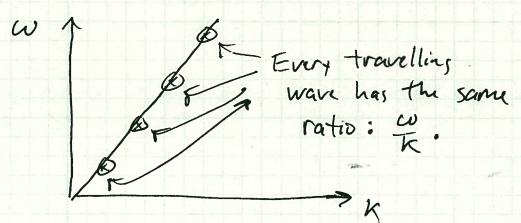
So the Classical Warn Equation says:
$$\left[-k^2 \left(Ae^{i(kx-\omega t)} \right) = \alpha \left[-\omega^2 \left(Ae^{i(kx-\omega t)} \right) \right) \right]$$

 $-k' = -\lambda \omega^2$ $\omega^2 = \frac{1}{\lambda} k^2$

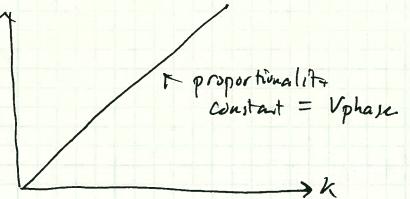
 $\frac{\omega}{K} = \frac{1}{\sqrt{\alpha}} = constant$

Now, by definition, w = phase velocity = Vp. So the classical wave equation requires that the phase velocity is a constant, independent of k, and independent of cv.

So if we plot w & K for a system described by the classical wave equation, every valid travelling wave will fall on a straight line that passes through the origin:



So what the classical man equation requires is that the frequency (w) they be directly proportine 1 to (k) (the man number).



Conversely, we could say that any system that has direct proportionality between we & K is described by the classical wave equation

So let β be some constant. If we find then a system for which $cw = \beta k$, then we can immediately conclude that the equation of motion of the system is the classical wave equation. Further, we can immediately infer that the phase relocate is

Vphase = $\frac{\omega}{\kappa}$ (by definition)

Vphase = $\frac{(\beta k)}{\kappa}$ For this particular $\frac{\beta}{\kappa}$ - 5xitem

Vphase = β = a constant

But in general me should not expect that the system is described by the classical wave equation. Then co is a more complicated function of k:

cu(k) = some complicated function of (k).

It will still be true that the vatio of cu & k
is still the phase velocity, because this is true
by definition.

Vphase = $\frac{\omega(\kappa)}{k}$ by definition. So for a more complicated system, the vatio $\frac{\omega(k)}{k}$ will not be a constant. MWAD"

Another important case is free particles in quantum muchanics. There particles have the Following dispersion relation:

co(k)= At the quatum free particle

and their phase velocity is

$$V_{phan} = \frac{cu(k)}{k} = \frac{t_1k^2}{t_1m} = \frac{t_1k}{z_m} = \frac{t_1k}{constant}$$

$$\frac{t_1k^2}{k} = \frac{t_1k^2}{z_m} = \frac{t_1k}{constant}$$

Combination.

For some A(k) which describes the pulse in k-space

Now the cv = cv(k), so

pulse = $y(x_3+) = \frac{1}{\sqrt{2\pi}} \int dk \, A(k) e^{-ik(x-\frac{cv(k)}{k}+)}$

Now suppose the system is has a simple dispusion relation: ew(k) = (some constant) k = Vohase k

The

 $y(x)t) = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} dk A(k) e^{ik(x-v_{phase}t)}$

Or suppose that the system is a quarter free particles

(pearting $(x,t) = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} dk A(k) e^{ik(x-(\frac{\pi k}{nn})+)}$

For Ysimple, we can surfalong at a constant value of y, if we advance x and at the constant value of Vphase. In other words, the cotter pulse advances without cleanging its shape at a speed of Vphase:

at +9

--- at +>0

SX= Vphaset

But what about the quantum free particle?

To keep the phase constant, we have to advance at a different rate for every wavenumber K which makes up the pulse.

Yquartra = of Jdk Alk) e ik (x - tak +)

there is no way to hold this constant for all k at the same time.

The problem is that all the component travelling waves which make up the pulse con travelling at different velocities. In other words, the are dispersing. And the pulse will dissuppee as it goes forward in tom:

at +>9
+>>0.

so the simple dispersion relation really means "no dispersion"

The w(k) = (some constant) k, the then will be no dispersion. Pulses will travel forever with the same shope. Therefore the classical war equation describes systems which have no dispersion.

In these systems, a pulse can travel forever.

Therefore example of this in nature is electromagnetic wares in vacuum, (or waves on an ideal string.)

Information * Bussositet transmission and group velocity

A perfect perfect travelling wave count be used to communicate. Because it is a perfect wave, it extends in time to (flowd (-) intinity, and to in space to (+) and (-) infinity. To the communicate a message, I would need to alter the wave in some ways two it off, make it larger, change its frequency, etc. But doing and of these things would mean that the wave is no longer perfect, because it the would then have multiple frequency compound.

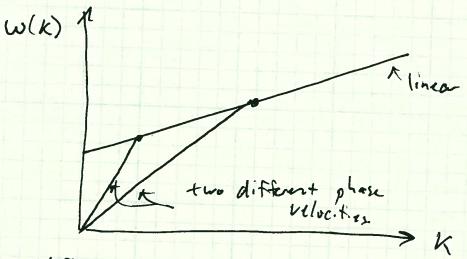
So to send a message, I will need multiple frequency at my disposal.

But if the medium is dispersive, then the various frequency components will all travel at different velocities, and my message will disperse so there will be some limit to how for I can communicate.

However, to there is a clear way to send information a much longer distance by using a small range of frequencies to create a pulse.

A, long as the dispersion relation is linear over that range of Frequeies, une can mare a public which travels foreur.

To illustrate, imagin that our dispersion relation is linear, but not directly proportional:



Since distant waves have different phon velocities, This system is dispersive.

Non I create a pulse-like envelope function "

composed of a range of varioumbers. $F(x) = \text{a pulse-like function} = \frac{1}{12\pi} \int_{-\infty}^{\infty} F(k) e^{ikx} dk$

Fourier Transform

f(x) could be a gaussian pulse, for example, F(x) a possible pulse-like f(x) Went Franklipty My claim is that I can make this pulse propagate in time Forener by multiplying f(x) by a high trequency perfect travelly wave. The high frequency wan is known as the "carrier wave" so let $Z(x) = (pulse) x (carrier) = f(x) e^{ikc}$ Whene Ke = wave number of the high frequency carrier wave Now Z(X) looks like 2(x) high frequency correr were multiplied by the pulse tunction

HMPAD"

Claimi Pulse propagates with an essent envelope function which does not dissipate:

at t=6

same envelope
function, ho
dissipation.

Tugo

"The speed at which the envelope propagates".

IF this claim is true, then the pulse propagation will be described mathematically as

we would like to provethis

$$\frac{Z(x) = F(x)e^{ikx} \text{ at } t = \emptyset}{Z(x, t) = F(x - v_0 t) e^{i(kx - w_0 t)}} \text{ at } t > \emptyset.$$

$$\frac{Z(x) + \lambda}{\sqrt{2}} = \frac{1}{2} \frac$$

relouty

f(x-vgt) describes the envelope moving at the group velocity without changing its shape

Now we prove this:

Z(x) = Jui Sak F(k) eikx dh eikex = I ok F(k) ei (k+ke)x

Trick 1: Let Alla Mar K'= K+ Ke.

Then K= K'- Ke, and we have

Z(x)= I Jok F(K'-Ke) e'kx

integrate over k' now.

This equation says that the Fourier Transform of Z(X) is F(K-Ke).

But k' is just a variable of integration. We can re-name it k if we wish .

Z(x) = \frac{1}{4\infty} \int dk F(k-Ke)e = The Fourier Transform
expression for Z(x).

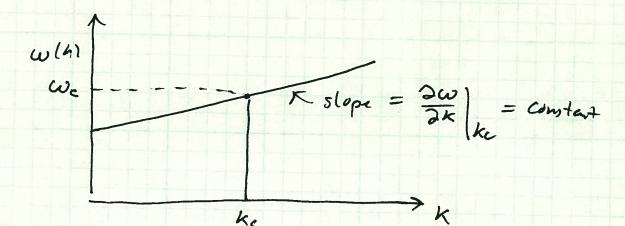
Now we see that the Foure Transform of Z(x) is F(k-ke).

Let's make Z(x) more alla formerd in time. To dottent we multiply each travelling wave component by i willis.

$$Z(x,+) = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} dk \ F(k-kc) e^{ikx} e^{-i\omega(k)+}$$

$$= \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} dk \ F(k-kc) e^{ik(x-\frac{\omega(k)}{k}+)}$$

Now we use our basic assumption: culkling linear



We call $\frac{2\omega}{2k}\Big|_{k_{L}} = V_{g} = \frac{u}{group}$ velocity.

The our travelling wave is

$$Z(x,+) = \frac{1}{\sqrt{k}} \int_{-\infty}^{\infty} dk \ F(k-kc) \ e^{ik \left(x - \left(\frac{\omega_c}{k} + \frac{kv_s}{k} - \frac{kev_s}{k}\right) + \right)}$$

todas

Trick 2: Let K" = K-ke. The K= K"+Ke. Theroan

$$Z(x_1+) = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} dk'' F(k'') e^{i(k'+k_c)x} - i\omega_c t - i(k'+k_c)v_g t$$

$$= e^{ik_c v_g t}$$

Apris mat deand . KV

$$Z(x,t) = e^{i(k_{c}X - \omega_{c}t)} \left[\frac{1}{4\pi} \right] dk'' F(k'') e^{ik''(x - V_{3}t)}$$

This is the Fourte Transfer of the envelope function $f(x-v_5+)$

 $z(x)+) = f(x-y+) e^{i(kex-\omega_c+)}$

This is what we set out to prove the envelope function f(x) propagate, without changing its shape: $f(x) \rightarrow f(x-v_3t)$. The speed of envelope progagation, known as the group velocity, has been determined to be

Vg = group velocity = $\frac{2\omega}{2\kappa} (\kappa = \kappa_c)$

This result is important because any dispersion relation will be approximately linear over a small range of k. So pulses can be sent through any dispersion medium, as long as we use a sufficiently small range of k to make our pulses.

Example: Quantum free particle co(k) AMPAD" tangent Slope = group velocity

Two Deam Interference

$$E_{p} = E_{1} + E_{2} = ZA \underbrace{i(kx - \omega t)}_{\text{wave fauthr}} \underbrace{Css\left(\frac{k\delta}{2}\right)}_{\text{amplitude factor}}$$

$$\delta = X_{2} - X_{1}$$

$$\overline{X} = \underbrace{X_{2} + X_{1}}_{7}$$

Usually we don't care about the wave factor (foscillaxing too Fast to see).

If we only want the amplitude Factor, then

For a single beam, the result would be $E_p E_p^{**} = A^2$

maximum is 4 times what it would be for our beam.

To observe interterence we need:

More generally,

EpEp*

= 4ACOS 20

a difference

SD = phase

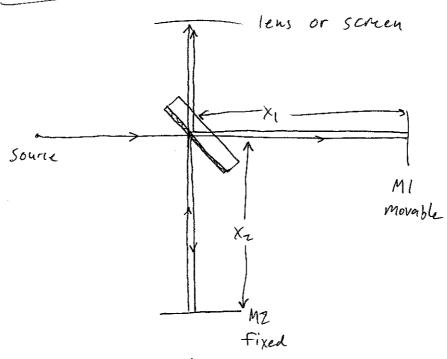
- · same polarization (usually get this automatically by using the same source to creek the two beams.)
- real light waves are not perfect cos functions.
 Coherence time is amount of time light wave remains predictable. Coherence lengths is distance light wave predictable.

Beams overlap

here.

He-Ne lasers have coherence lengthy of a 20 cm = 10m) for white light, wherene length inabout our wowelength (2/m)

Michelson Interferometer



I < 4A2 C152 40

path difference = $Z(x_1-x_2) = \delta$ - phase due to path difference = $k\delta = Zk(x_1-k_2)$ - phase due to internal reflection = $\frac{k}{2} \pm 11$ of beam along M_1

total phase difference = $ZK(x_2-x_1) + ZT = mTT$ for light frings $kA = \frac{Z}{K} = mT - 0,1,2,3$

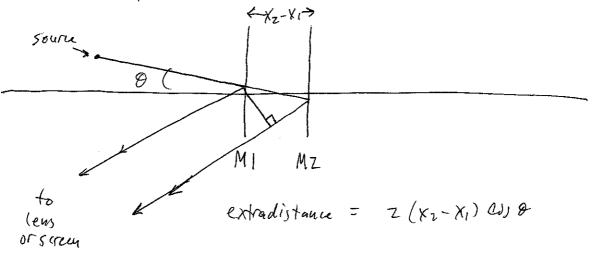
 $K = \frac{2\pi}{\lambda}$ $\frac{1}{\lambda}$ $\frac{1}{\lambda}$

constructive interference.

In practice you don't see one spot, you see rings:



This is because off-axis points have additional phase differences hum to the path length difference:



If $X_2 = X_1$, then only one fringe will be seen (no off-axis phase difference)

A TOO A

Otherwise many rings will be seen.

In some cases

Applically we don't care about which order of tringe we are observing. Instead, we more MZ and count the number of fringes that pass by. Then

 $\Delta M = \frac{7(X_2-X_1)}{\lambda}$ Can up this to measure the braveley to of the light.

Sodium Lamp

Two closely spaced wavelengths: 1, 1

Each makes its own fringe pattern.

Suppose the Michelson interferometer gives a

For both wavelents:



Fringe order Fringe order

 $\frac{Zd_1}{\lambda} = \frac{Zd_2}{\lambda'} + N, \quad \lambda_1 = \chi_2 - \chi_1$

Now increase X2 (nove mirror). I After while, the tringe pattern dissapples:



Then keep movins, and tringes

Now Xz-X1 = dz

 $\frac{zdz}{\lambda} = \frac{zdz}{\lambda'} + \frac{N+1}{\sqrt{N+1}}$

m and m' differ by on more unit now

 $\frac{Z(dz-d_1)}{\lambda} = \frac{Z(dz-d_1)}{\lambda'} + 1$

 $\frac{2dd}{\lambda} - \frac{2dd}{\lambda'} = 1$

 $\lambda - \lambda' = \frac{\lambda \lambda'}{7 \cdot \Delta \lambda} \Rightarrow \Delta \lambda =$

Lecture 9- Single Slit Diffraction

Review From last week

I & 4A Cos 2 DO Two Bean interference

Dot = all phase difference between two beans.

Michelson interferometer: total phase difference = ZK(X1-X2)+II.

Constructive interference: $2k(x_1-x_2)$ = (x_1-x_2) = $m+\frac{1}{2}$, n=0,1,2.

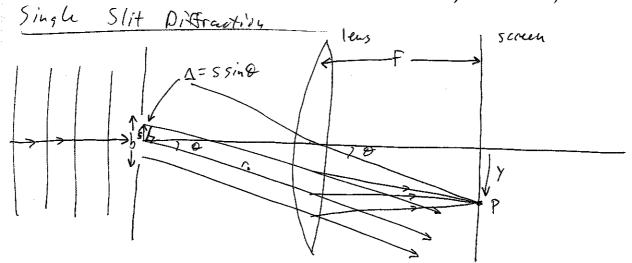
distructive interference: $\frac{7(x_1-x_2)}{\lambda} = m$, m = 0, 1, 2, ...

Measuring the wavelength: keep MI fixed, move Mij count fringes: $\Delta m = \frac{Z\Delta X_{Z}}{\lambda}$

Sodium Lang: Two closely spaced wavelengths & and 1'

 $\Delta \lambda = \lambda^2 - \lambda' \approx \frac{\lambda^2}{7 \Delta d}$

I the distance MZ roves between to case of maximum fringe visibility.



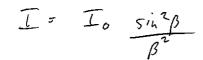
Framhofer Diffrantion (Four Field Diffrantism): Observe interference pattern at infinity as a function of D. L73 3/2 Four Field Condition.
Use a lens to move diffrantism pattern from infinity to a screen

Each point in the aperture is a source of spherical waves.

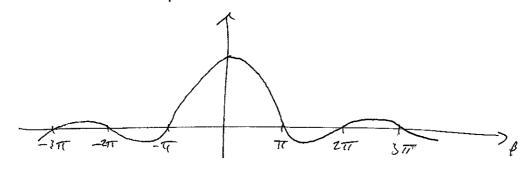
Field at P due to a single point on the aperture: $dE_{r} = \left(\frac{E_{1}ds}{r}\right)e^{i(kr-\omega+1)}$ Amplitude Factor tor spherical (IXT), so EXT Let so be the distance travelled by the wavelet originating at the center of the aperture. $dE_p = \left(\frac{E_L d_S}{r_o + \Delta}\right) e^{i(K(r_o + \Delta) - \omega t)} \approx \frac{E_L d_S}{r_o} e^{i(Kr_o - \omega t)ik\Delta}$ I can ignore & compared to r.

Integrate over the aperture to get the total field at Point P: $\Delta = 55$ ind Ep = JdEp = & EL i(kro-wt) polz iks sind ds $= \frac{EL}{r_0} e^{i(kr_0-\omega t)} \left(\frac{e^{ikssin0}}{e^{ikssin0}}\right)^{-b/2}$ $= \frac{EL}{r_0} e^{i(ksr_0-\omega t)} \left(\frac{e^{ikssin0}}{e^{ikssin0/2}}\right)^{-ikbsin0/2}$ $= \frac{e^{i(ksr_0-\omega t)}}{e^{ikssin0}} \left(\frac{e^{ikssin0}}{e^{ikssin0}}\right)^{-ikbsin0/2}$ B = tkbsino Ep = ELB i(kro-wt) Zising = | ELB i(kro-wt) (sing)

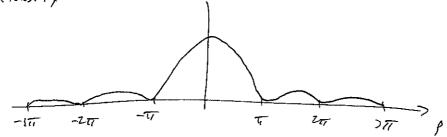
 $\overline{I} = \frac{\xi_0 \zeta}{Z} E_p E_p^* = \frac{\xi_1 \zeta}{Z} \left(\frac{E_L b}{r_0} \right)^2 \frac{\sin^2 \beta}{R^2} /, \quad p = \frac{1}{2} k b \sin \theta$



Electric Field amplitude:



Intensity:



Zeros occur when

$$\beta = \pm m\pi$$
, $m = \pm 1, 2, 3,$
but not $m = \beta!$

thosing = MTT

Which using a lens, we can write & in terms of the position on the screen:

$$\frac{y}{f} = \tan \theta \approx \sin \theta$$

$$\sin \theta \approx \frac{y}{f}$$

width of the central maximum:

DO = ZA

Linversely proportional to to
aperture width.

Lecture 10 - Double and Multiple 5/17 Diffraction 11/7/04 Recap 0 = 5 sin0 Fraunhofer (Far-Field) diffraction: L>> 5 $E_p = \frac{E_1b}{r_0} e^{i(kr_0 - \omega t)} \frac{sin\beta}{R}$, $\beta = \frac{1}{2}kbsin\theta$ $I = \frac{2iC}{7} EEp = \frac{2iC}{7} \left(\frac{E_1b}{r_0}\right)^2 \frac{\sin^2 \beta}{R^2} = I_0 \frac{\sin^2 \beta}{B^2}$ Zeros at $\beta = m\pi$, $m = \pm 1, \pm 7, ..., but nut <math>m = \emptyset$! m/ = bsino / Zeros 11 24 34 417 If we use a lens, and put the screen in the Focal plane, then the zeros are located of yn = mat / zeros , f = tocal lengths yn = position on the screen

Reunite

Double Slit Diffrackin

$$dE_{p} = \underbrace{ELS}_{r} e^{i(kr-\omega+)}$$

$$r = r_{0} + \Delta = r_{0} + S \sin \theta$$

$$E_{p} = \int dE_{p} = \underbrace{EL}_{r_{0}} e^{i(kr_{0} - \omega+)} \int e^{ik\Delta} ds$$

$$Slits = \int e^{i(kr_{0} - \omega+)} \int e^{ik\Delta} ds$$

$$E_{p} = \int dE_{p} = \frac{EL}{r_{o}} \left[\frac{(kr_{o}-\omega t)}{\sqrt{2}} \right] \frac{e^{ik\Delta}}{e^{ikssin\theta}} ds$$

$$= \frac{EL}{r_{o}} e^{i(kr_{o}-\omega t)} \left[\frac{1}{2} \frac{(a+b)}{e^{ikssin\theta}} \right] \frac{1}{2} \frac{(a+b)}{e^{ikssin\theta}} ds$$

$$= \frac{EL}{r_{o}} e^{i(kr_{o}-\omega t)} \left[\frac{1}{2} \frac{(a+b)}{e^{ikssin\theta}} \right] \frac{1}{2} \frac{1}{2} \frac{(a+b)}{e^{ikssin\theta}} ds$$

$$= \frac{EL}{r_{o}} e^{i(kr_{o}-\omega t)} \left[\frac{1}{2} \frac{(a+b)}{e^{ikssin\theta}} \right] \frac{1}{2} \frac{1}{2} \frac{(a+b)}{e^{ikssin\theta}} ds$$

$$= \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{(a+b)}{e^{ikssin\theta}} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{(a+b)}{e^{ikssin\theta}} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{(a+b)}{e^{ikssin\theta}} \frac{1}{2} \frac{1}{$$

B = Zkbsino

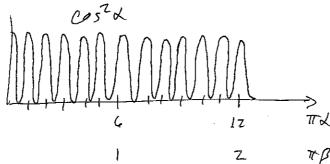
$$= \frac{E_{L}}{r_{o}} \frac{(kr_{o}-\omega t)}{ik\sin \theta} \left[\begin{array}{c} -i\varkappa & i\beta & -i\varkappa & i\beta \\ e & e & -e & e & +e & e & +e \\ \hline r_{o} & e & (kr_{o}-\omega t) \end{array} \right] \left(\begin{array}{c} -i\varkappa & i\varkappa \\ (-i\varkappa & i\varkappa) \end{array} \right) \left(\begin{array}{c} -i\beta & -i\beta \\ (-i\varkappa & -e) \end{array} \right)$$

$$= \frac{E_{L}(ib)}{r_{o}} \frac{i(kr_{o}-\omega t)}{ik\sin \theta} \left[\begin{array}{c} (-i\varkappa & -i\varkappa) \\ (-i\varkappa & -e) \end{array} \right] \left(\begin{array}{c} -i\beta & -i\beta \\ (-i\varkappa & -e) \end{array} \right)$$

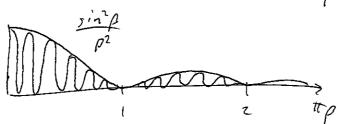
$$= \frac{E_{L}(ib)}{r_{o}} \frac{i(kr_{o}-\omega t)}{ik\sin \theta} \left[\begin{array}{c} (-i\varkappa & -i\varkappa) \\ (-i\varkappa & -e) \end{array} \right] \left(\begin{array}{c} (-i\varkappa - -i\beta) \\ (-i\varkappa - e) \end{array} \right)$$

$$I = \frac{\epsilon_0 C}{z} \frac{4E_1^2 b^2}{b^2} \frac{5ih^2 \beta}{\beta^2} \cos^2 \alpha$$

$$= 4 I_{ss} \frac{\sin^2 \beta}{\beta^2} \cos^2 \lambda$$
single



" Interference term"



" Differetion term"

Who slit spacing is an integral number of slit midtles, we always get missing maxima.

Diffraction minima: mx = bsing, m= ±1, ±2,

Interference maxima: nh = asind, u=0, 1/12,...

Number of peaks in central diffraction fringe = Z(a)-1.

N slits:

$$T = T_0 \frac{\sin^2 \beta}{\beta^2} \left(\frac{\sin N \lambda}{\sin \alpha} \right)^2$$

Interference Factor: SINNA

indeterminate whenever d = 0, IT).

Theoetire interference maxima are No more intense than they would have been for 1 slit. I= NZ Ioss SinZB when d = MII, n=0,±1,±2,... Sin2 L: Suppose N=4 Interfern N-1 zeros between principle maxima, and N-2 secondary maxima between principle maxima. Suppose third principle maxima is mining. Therefor $\beta = \frac{2}{3}$ Babinet's Principle Complementary obstruction produce the same diffractions pattern, except for the bean spot: Use this to measure the width of gr obstruction, like a hour hour.