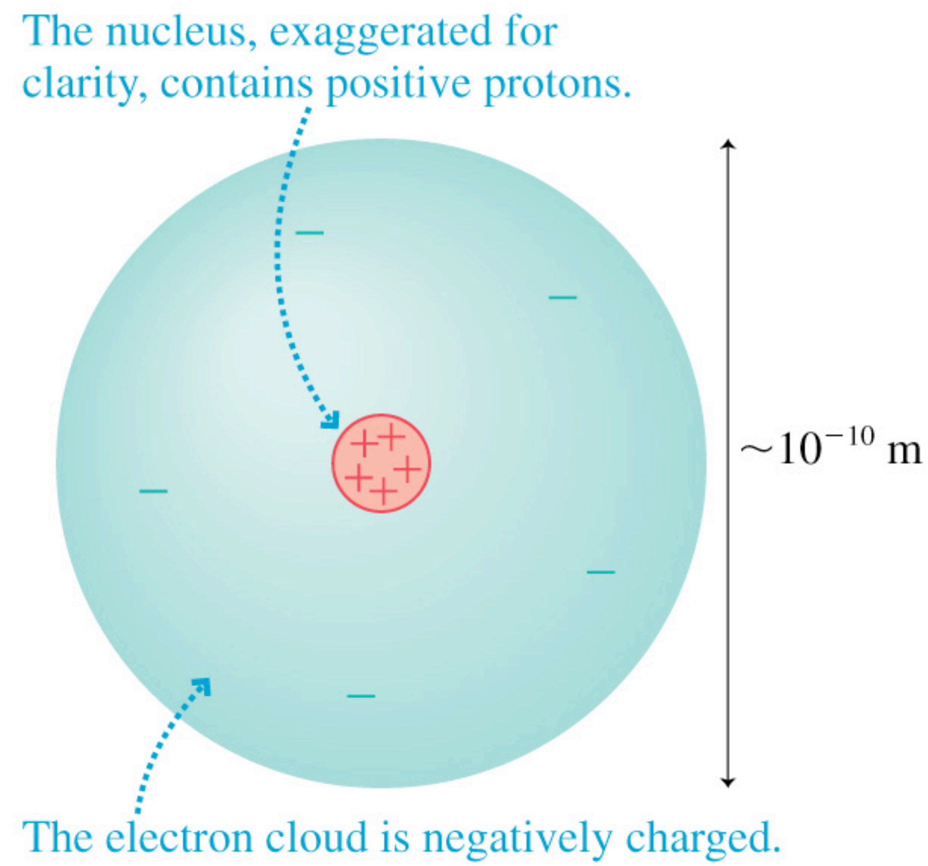
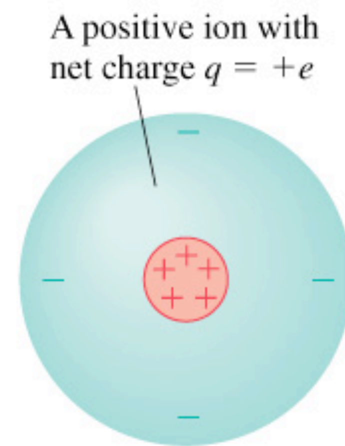
Lecture 17

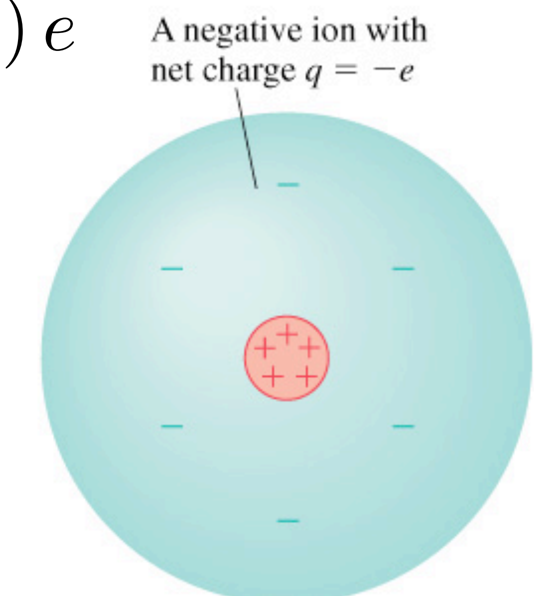
- Charges at microscopic level
- understand insulators, conductors...
- Quantify force: Coulomb's law
- Concept of electric field
- Electric field due to point charge

Charge at microscopic level I

- 2 types of charges behave like positive and negative numbers, e.g. metal sphere is neutral after receiving equal amounts of 2...
- which is positive is <u>convention</u> (Franklin): glass rod positive, electron attracted to it electron negative
- Atomic-level/<u>fundamental unit of charge</u>: +e for proton, -e for electron (inherent property)
- no other sources of charge: $q = N_p e - N_e e = (N_p - N_e)\, e$ (charge quantization)
- acquire positive charge by losing electron (<u>ionization</u>); negative ion (extra electron)

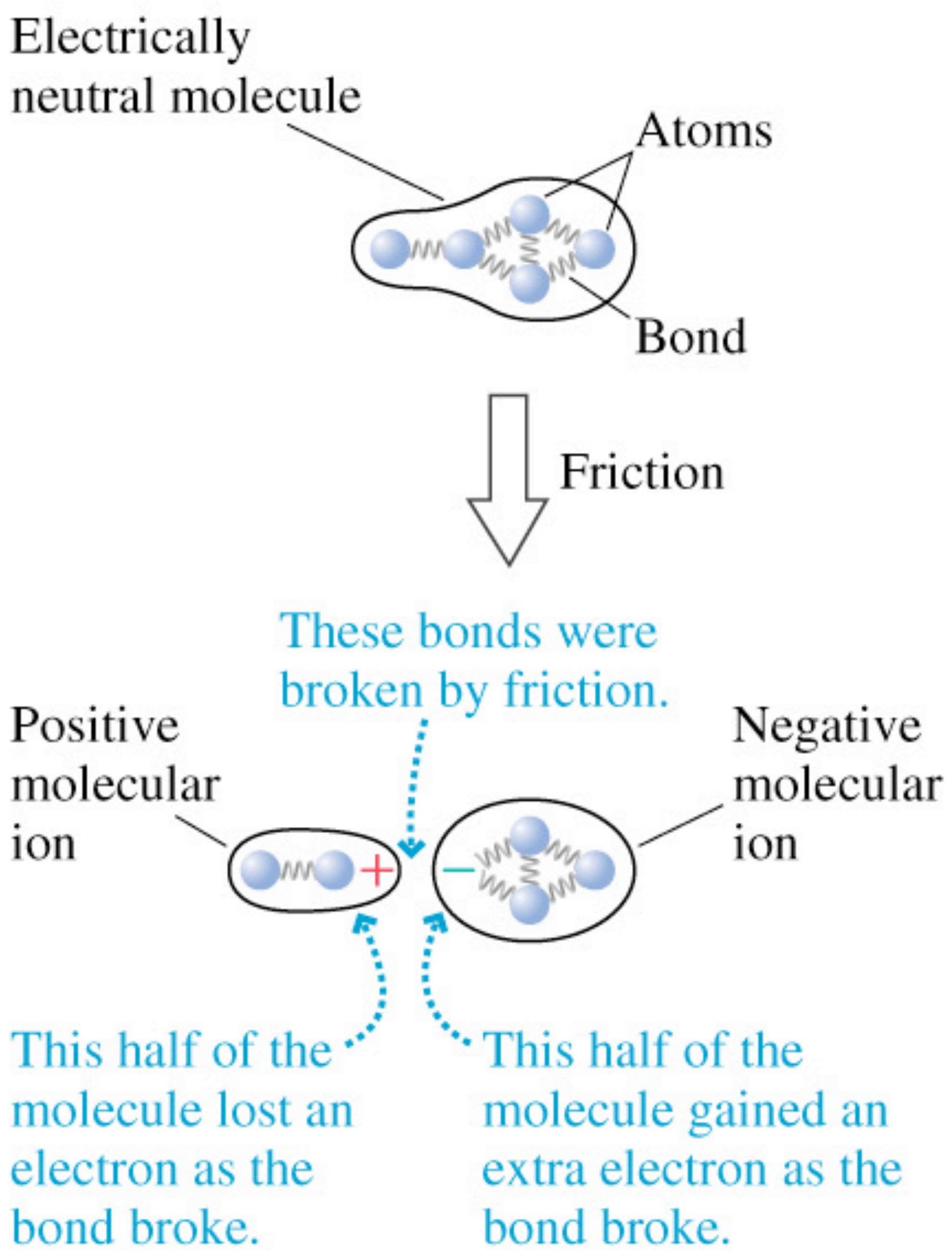


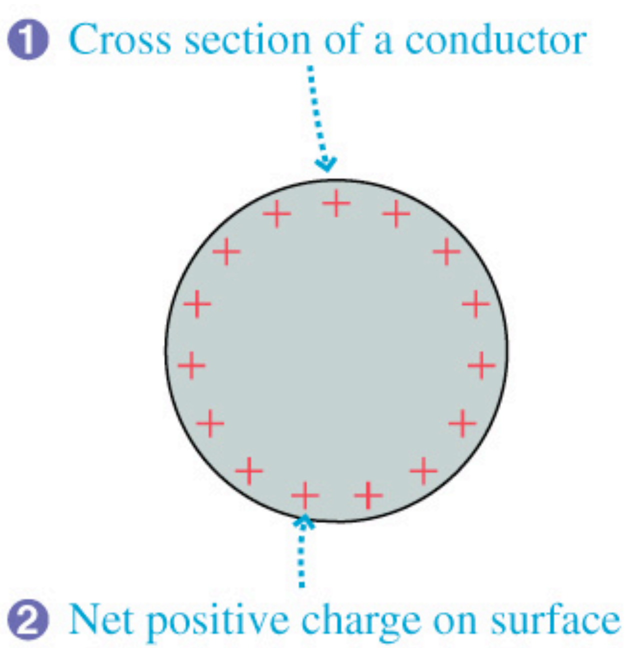


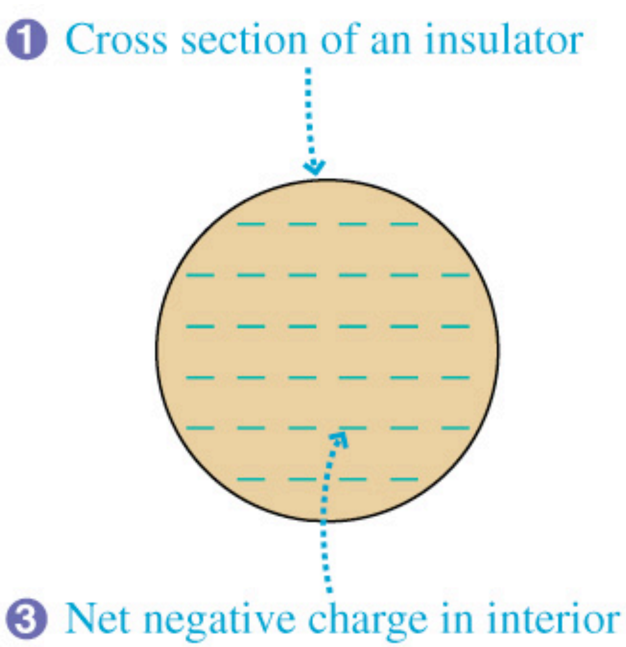


Charge at microscopic level II

- charging by rubbing: molecular ions from breaking of bonds
- <u>charge conservation</u> (transferred by electrons/ions): $q_{wool} = -q_{plastic}$
- <u>charge diagrams</u>: show net charge; conserve charge in next diagram

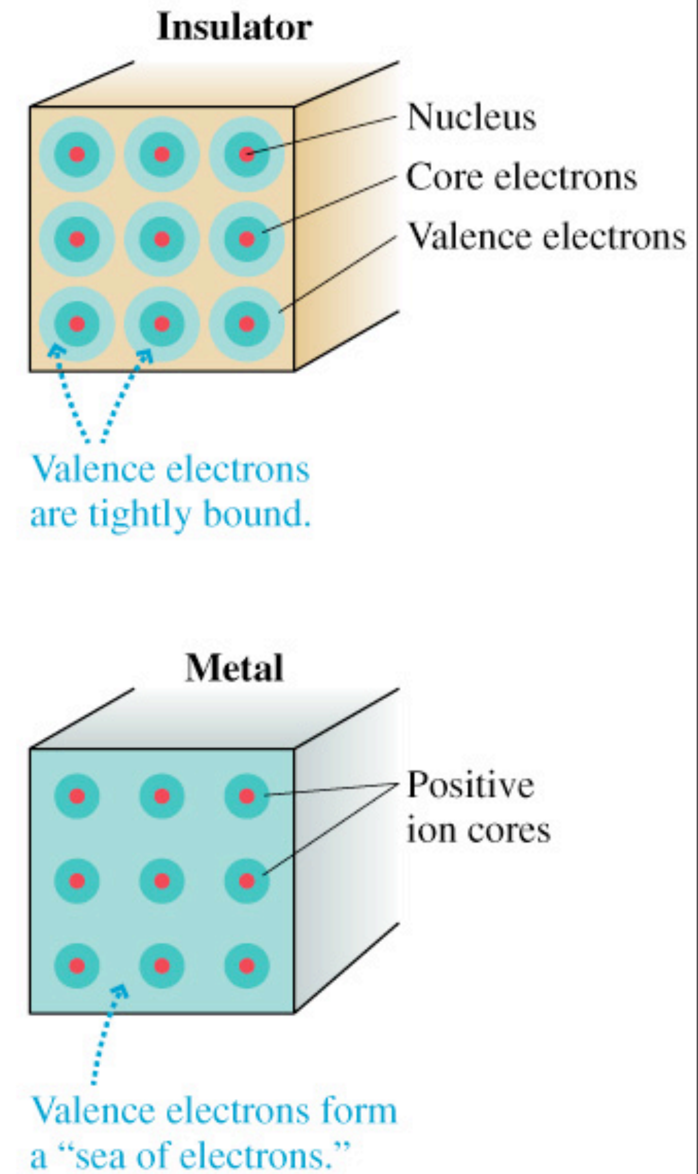






Insulators and Conductors

- insulators: charges immobile
- Conductors, e.g., <u>metals</u>: valence electrons weakly bound, respond to electric forces; salt water: ions...



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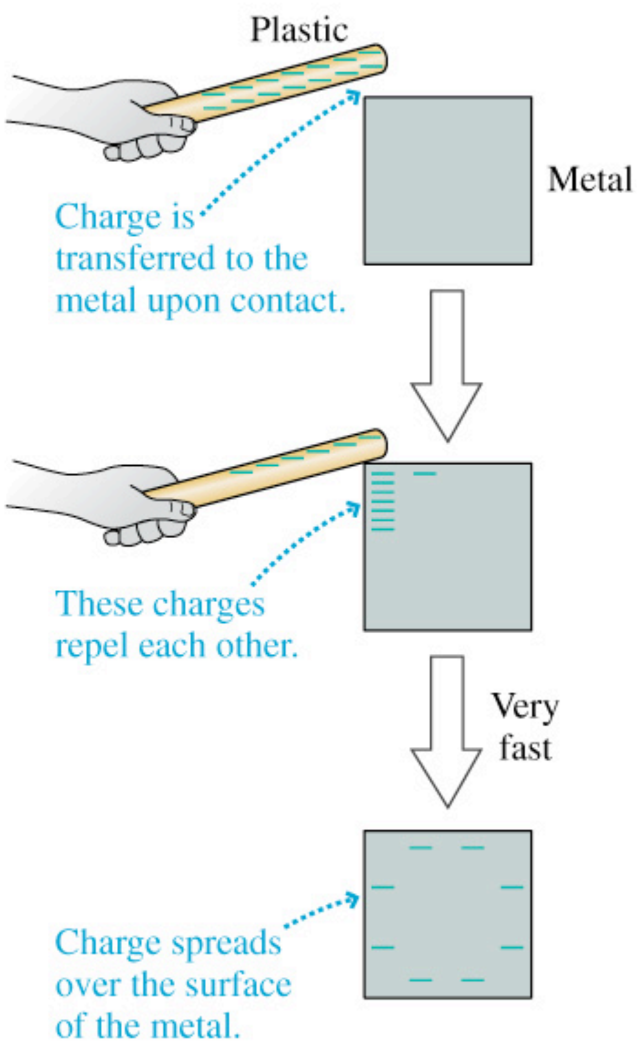
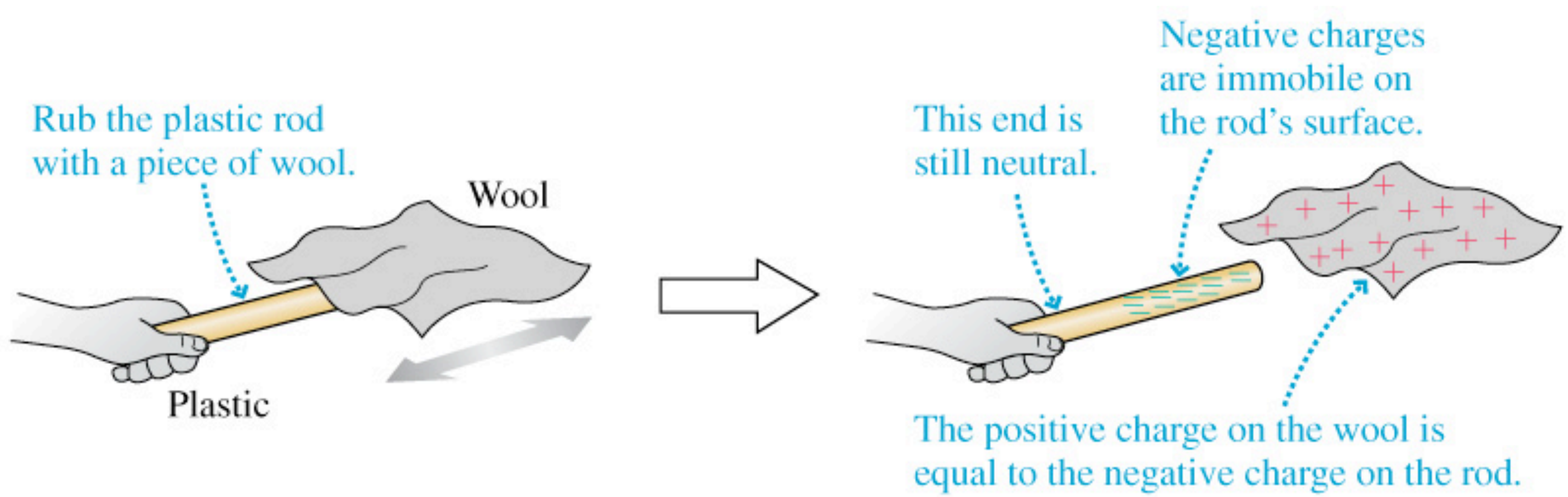
Charging

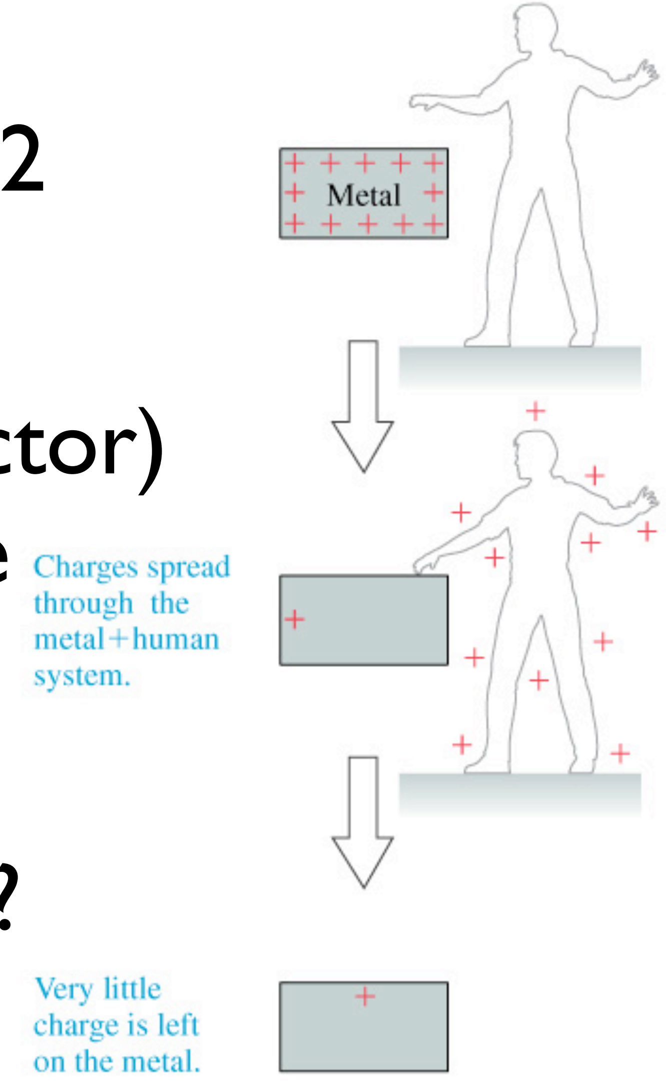
- conductors in electrostatic equilibrium: excess charge located on surface (if in interior, forces exerted causing move...)





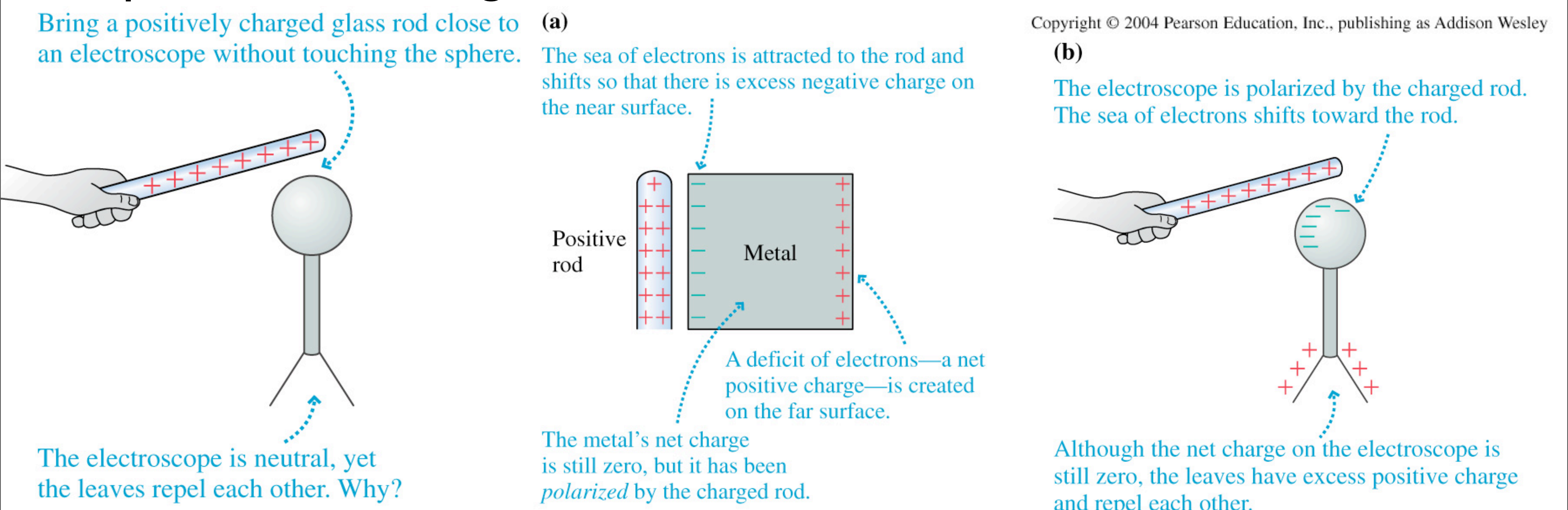
Discharging

- human body (salt water) is (large) conductor:2 conductors in contact "share" charge
- grounding: object connected to earth (conductor) thru' conductor to prevent build-up of charge



Charge polarization

- charged objects (either sign) force on <u>neutral</u>?
- <u>separation</u> of charges in neutral



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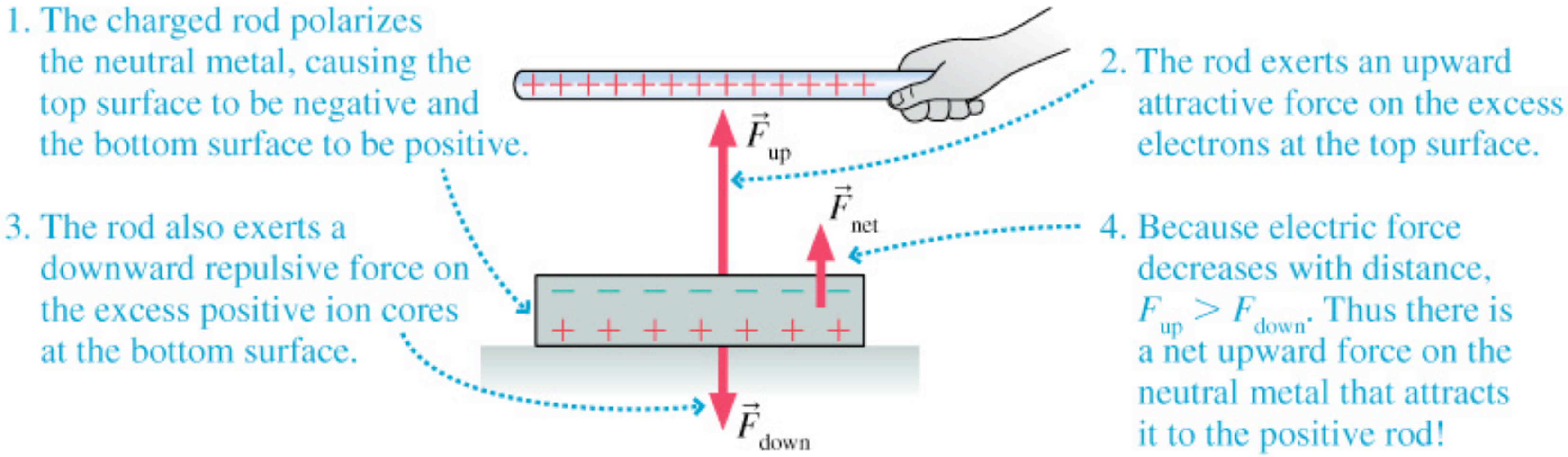
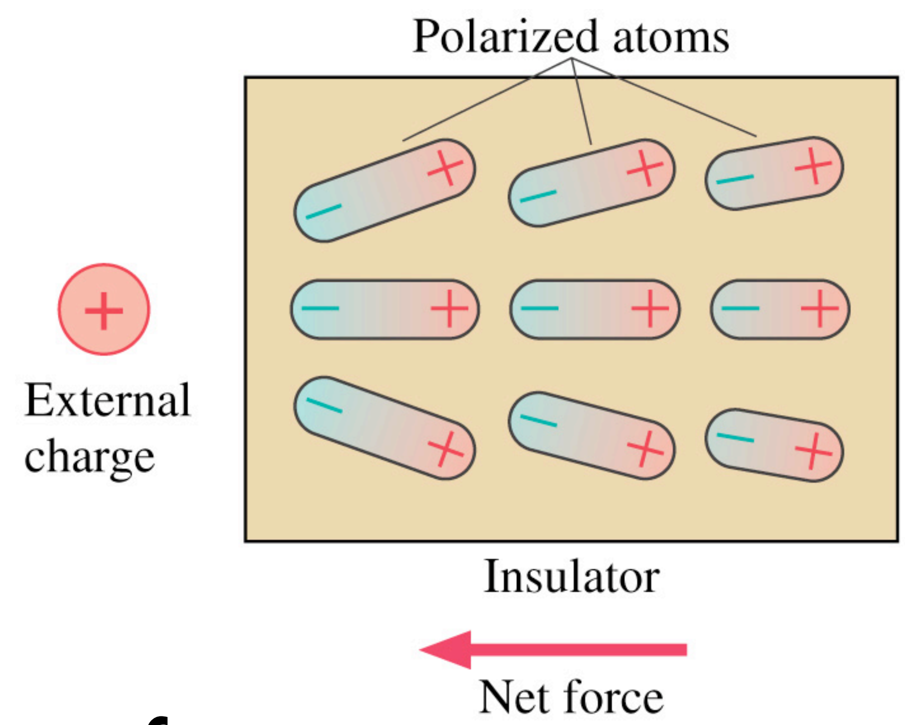
Electric Dipole

- Polarization force <u>attractive</u> (both signs of charged rods)





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- charged rod picks up paper (<u>insulator</u>)?
- atoms polarized (electrons still bound)...net force...
  <u>electric dipole</u>: two charges with separation

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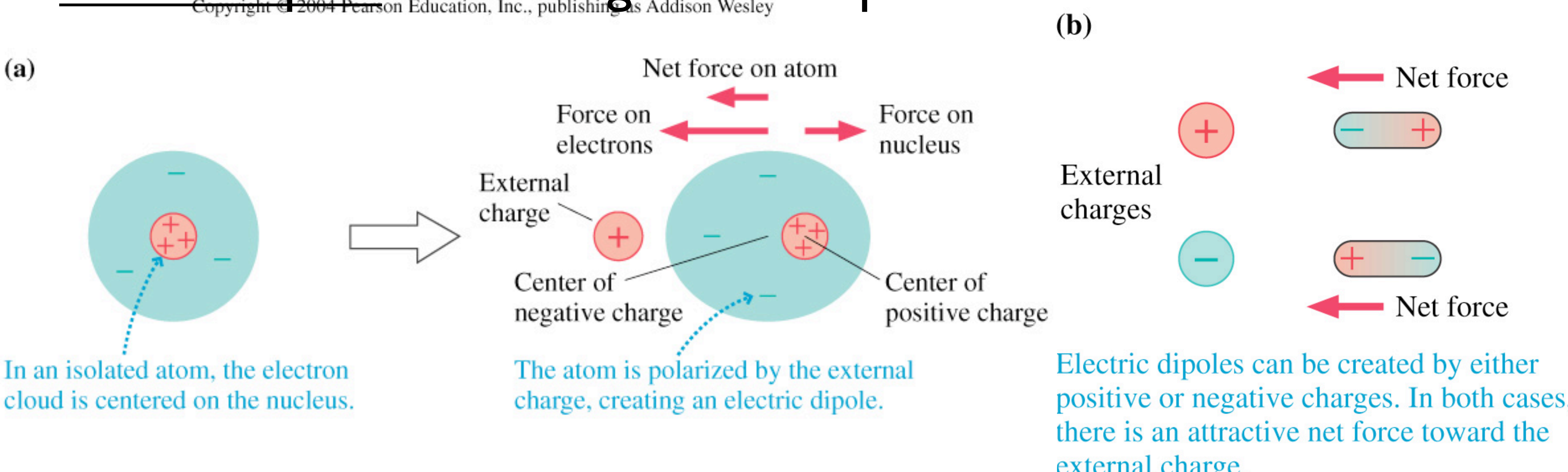
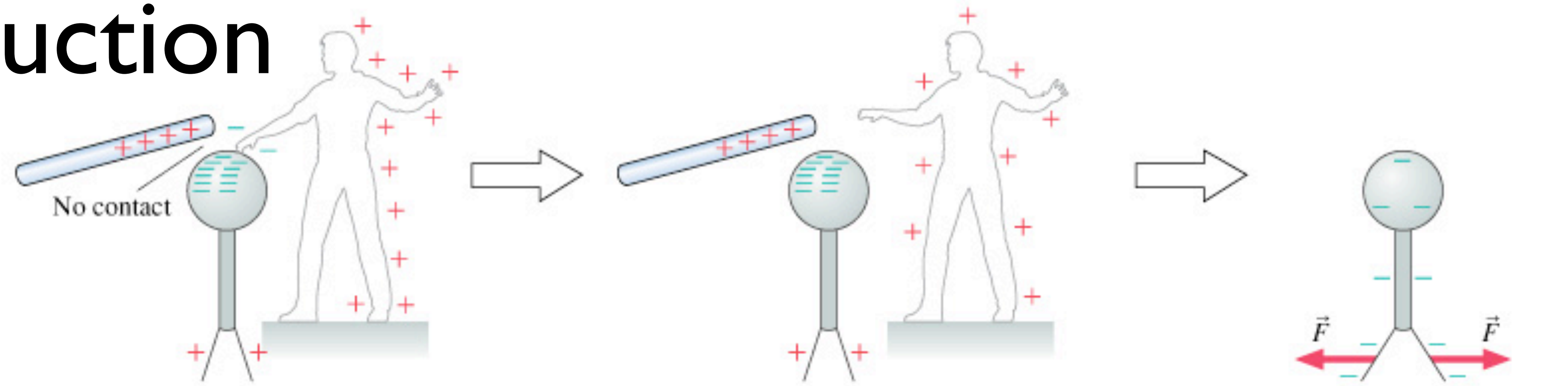


Charging by Induction



1. The charged rod polarizes the electroscope+person conductor. The leaves repel slightly, due to polarization within the electroscope, but overall the electroscope has an excess of electrons and the person has a deficit of electrons.

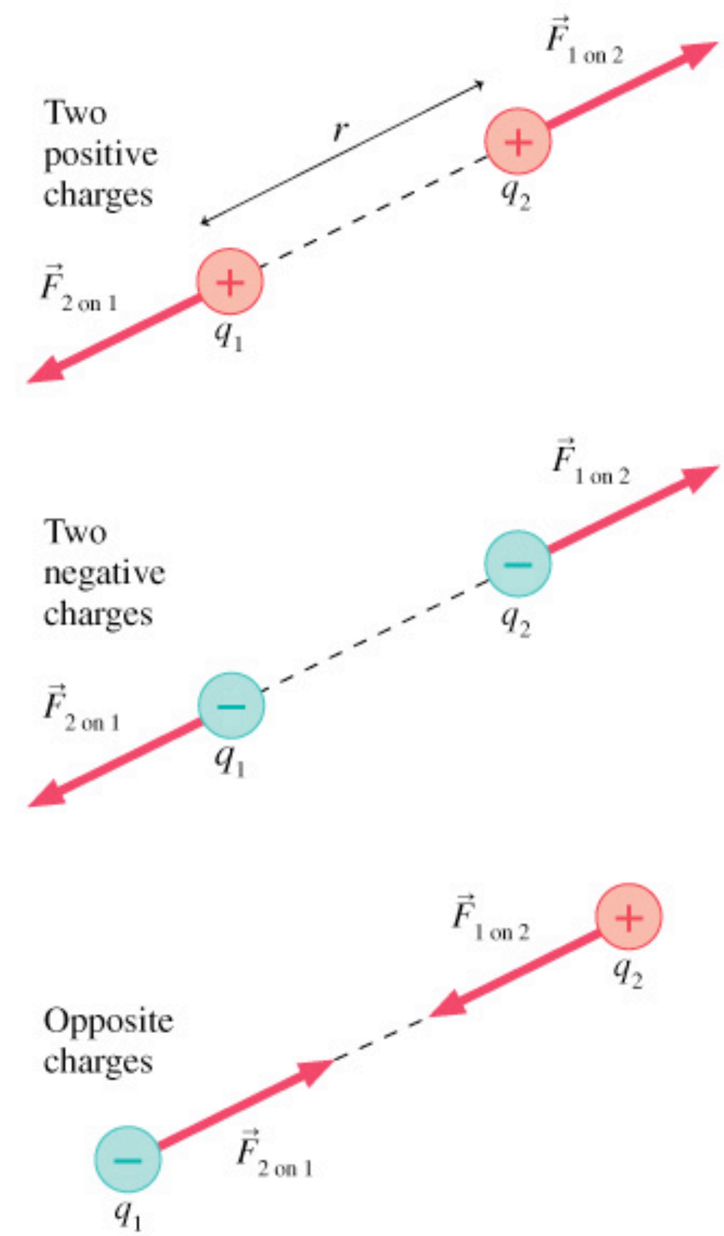
2. The negative charge on the electroscope is isolated when contact is broken.

3. When the rod is removed, the leaves first collapse, as the polarization vanishes, then repel as the excess negative charge spreads out. The electroscope has been *negatively* charged.

Coulomb's law

$$F_{1\text{ on }2} = F_{2\text{ on }1} = \frac{K|q_1||q_2|}{r^2}$$

- equal in magnitude, opposite in direction, along line joining
- attractive for opposite, repulsive for like (vectors)
- point charges: size $\ll$ separation between..
- static charges ($\ll$ speed of light)



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Using Coulomb's law

- Units of charge (derived from current):

$$e = 1.6 \times 10^{-19}\ \mathrm{C} \quad \Rightarrow \quad K = 9 \times 10^{9}\ \mathrm{N\ m^2/C^2}$$

- Rewrite in terms of $\epsilon_0 = \frac{1}{4\pi K} = 8.85 \times 10^{-12}\ \mathrm{C^2/N\ m^2}$

$$F = \frac{1}{4\pi\epsilon_0}\frac{|q_1|q_2|}{r^2}$$

- Superposition: multiple charges 1,2, 3...

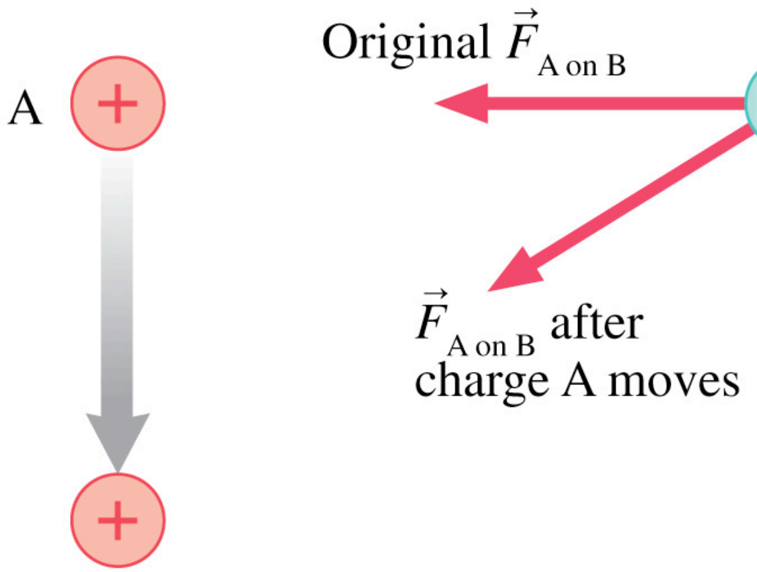
$$\bar{F}_{net}\,\mathrm{on}\,_j = \bar{F}_1\,\mathrm{on}\,_j + \bar{F}_2\,\mathrm{on}\,_j + \ldots$$

- Strategy: pictorial representation (show charges, forces vectors...); graphical vector addition; x-and y-components

Example

- Two 1.0 g spheres are charged equally and placed 2.0 cm. apart. When released, they begin to accelerate at 150 meter per second squared. What is the magnitude of the charge on each sphere?

Concept of a Field



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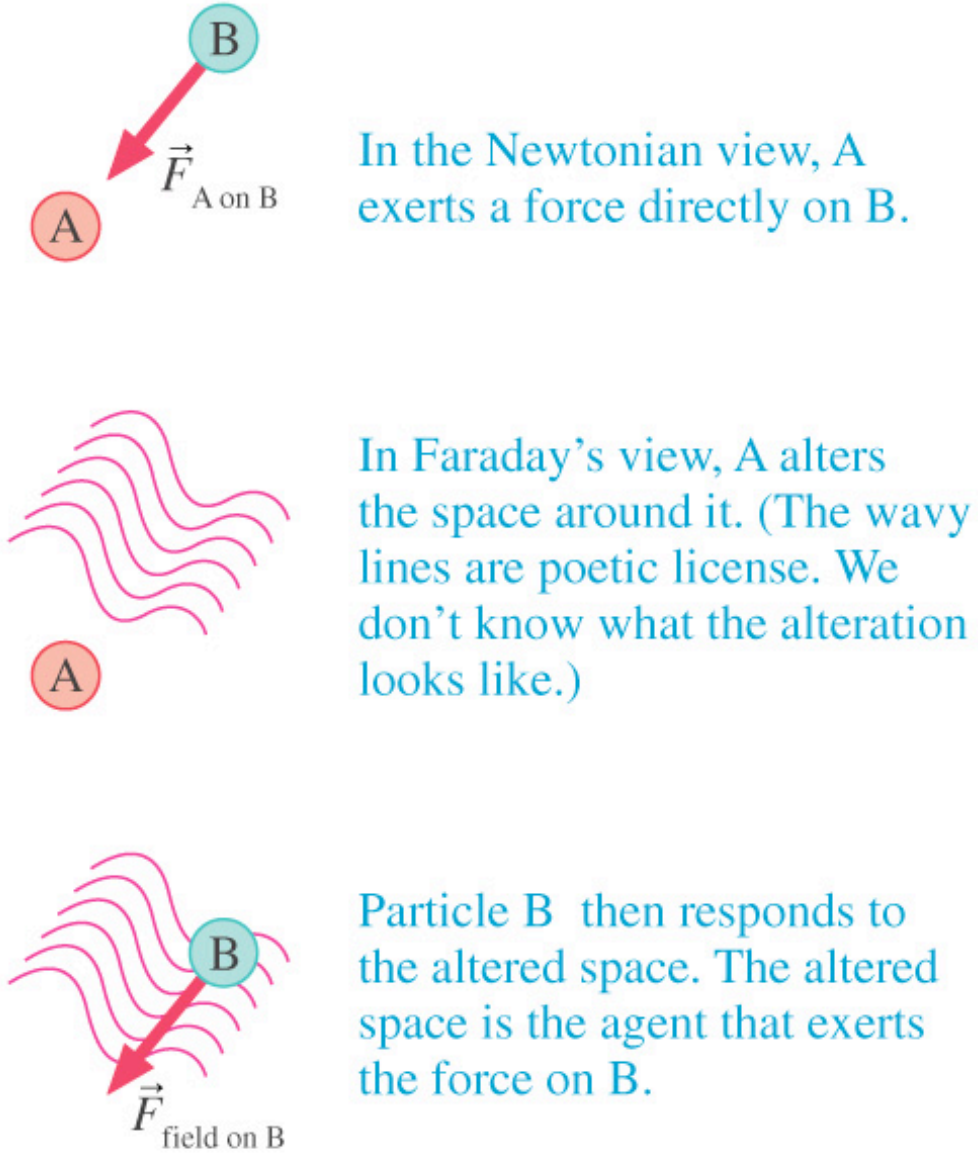

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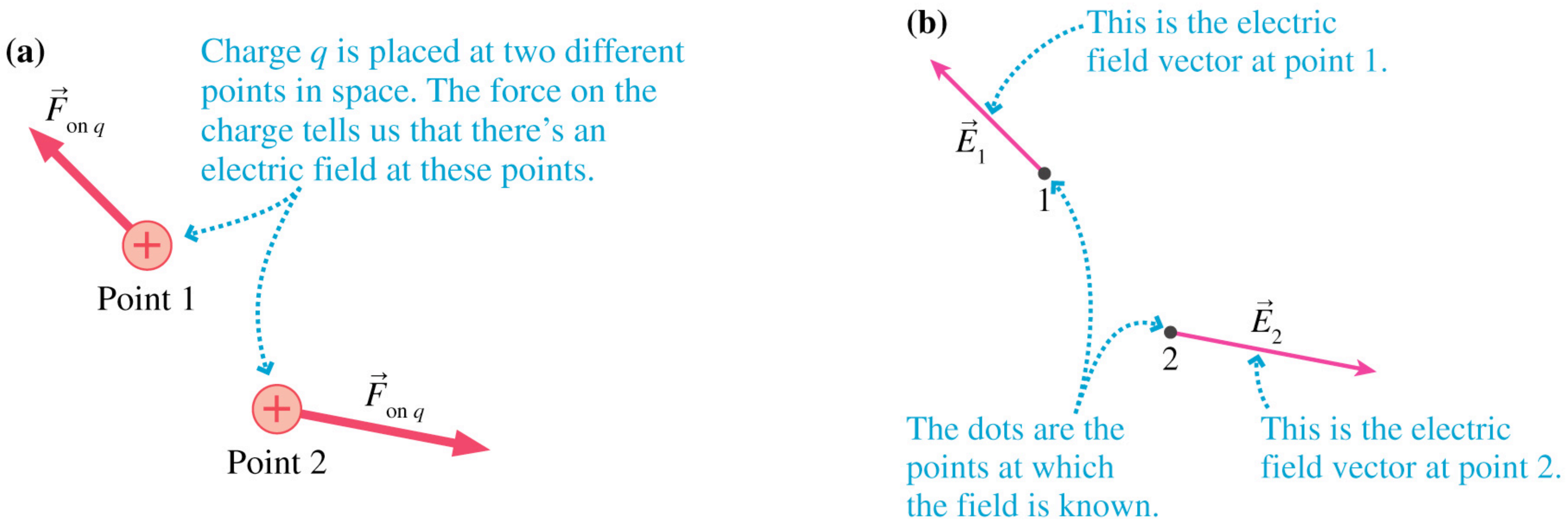
- gravity, electric forces long range (action at a distance): mechanism?
- force changes instantly?
- Faraday (and Maxwell): other masses/charges respond to field, f(x, y, z) cf. particle exits at 1 point
- alteration of space around a mass/charge: gravitational/electric field

Electric Field Model



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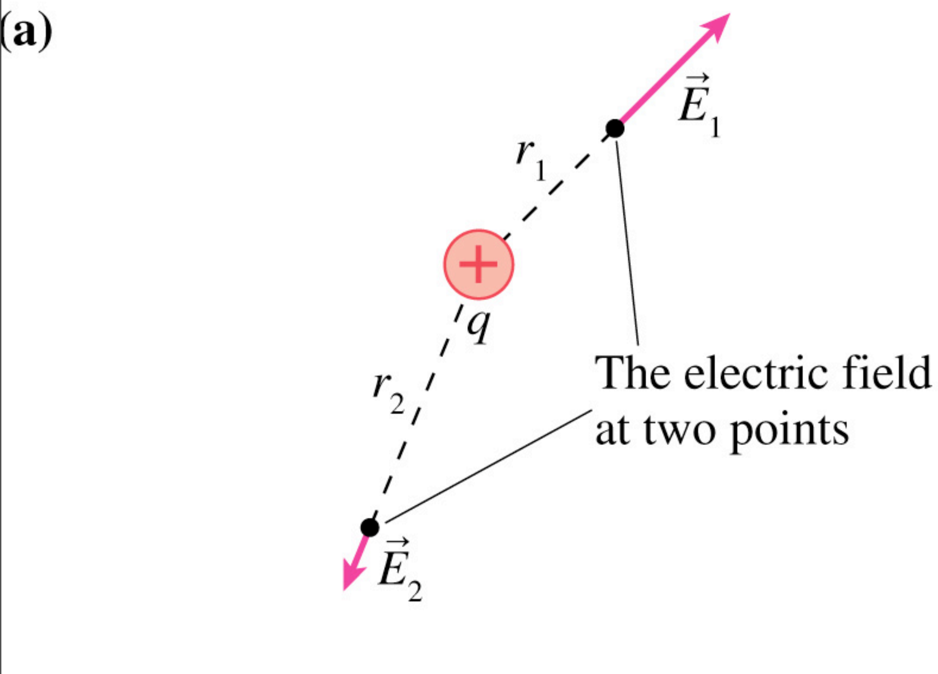
- more complex: 2 types of charges, forces, materials...
- source charge create electric field $\bar{E}$, probe charge experiences $\bar{F}$ exerted by $\bar{E}$

$$\vec{E}(x, y, z) = \frac{\vec{F}_{\text{on } q} \text{ at } (x, y, z)}{q}$$

- field is agent exerting force ($\bar{F} = q\bar{E}$): vector at every point; same direction as $\bar{F}$ for q > 0; independent of q (since $\bar{F}_{\text{on } q} \propto q$)

Electric Field of Point Charge



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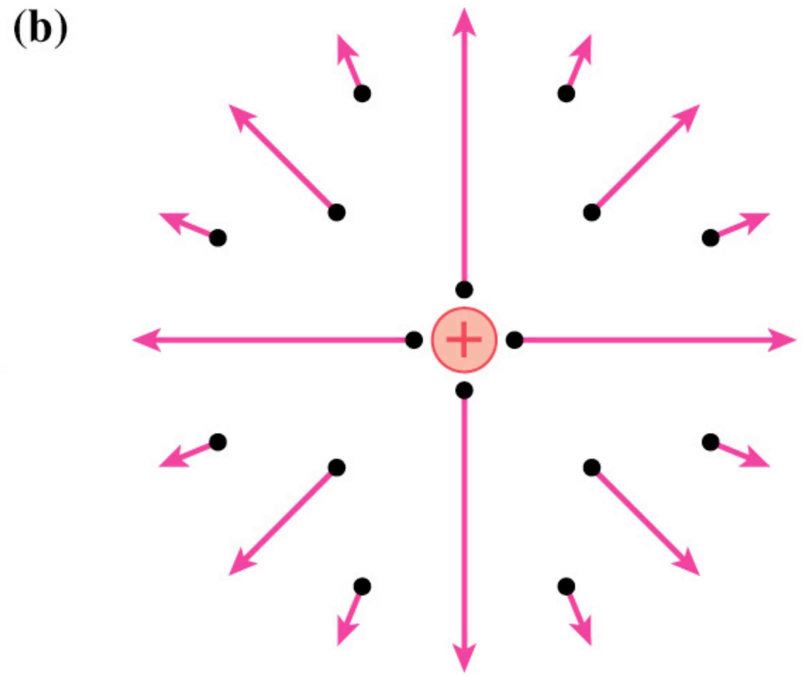

The electric field diagram of a positive point charge

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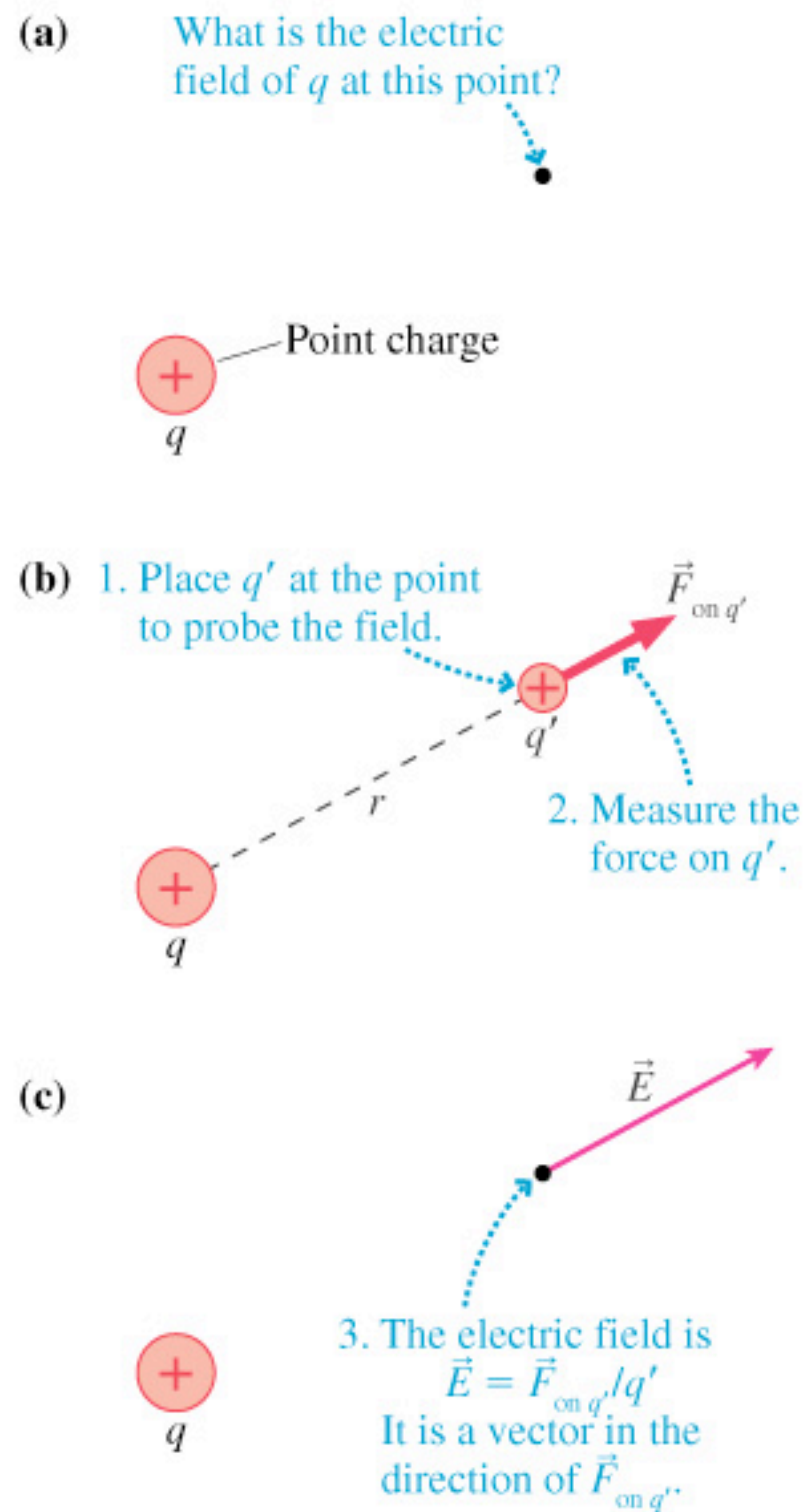
- Use Coulomb's law:

$$\bar{E} = \frac{\bar{F}\text{on}_{\,q'}}{q'} = \left(\frac{1}{4\pi\epsilon_0}\frac{q}{r^2}, \text{away from } q\right)$$

- field diagram (sample vectors): at tail of vector; does not stretch...



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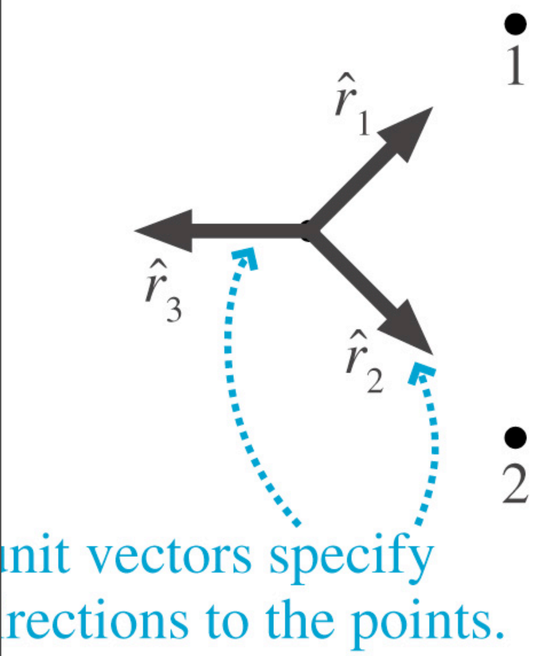
Unit Vector Notation



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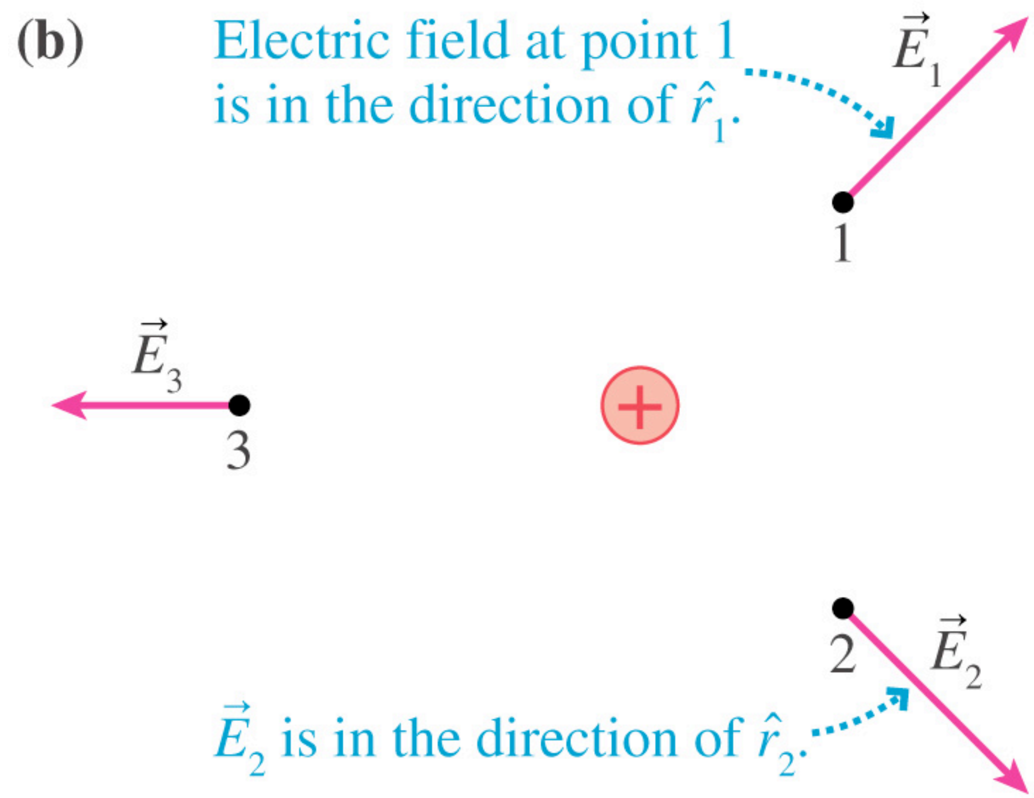

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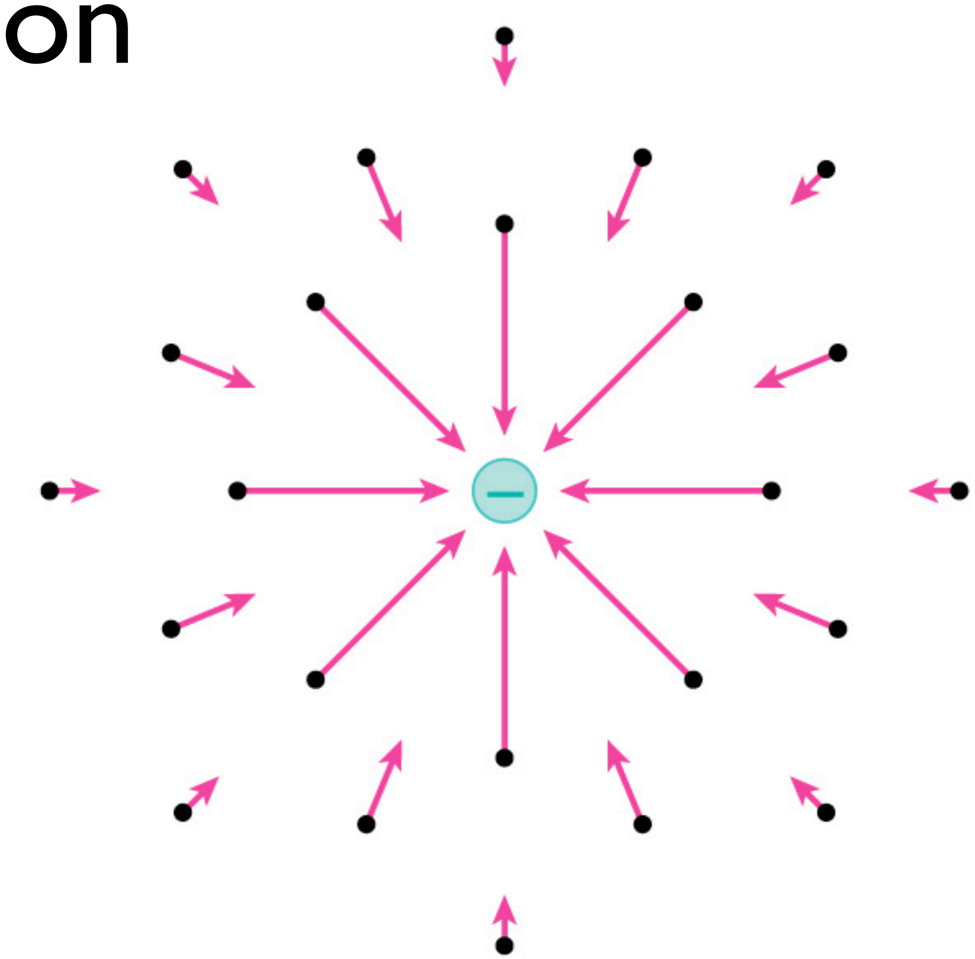

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- mathematical notation for "away from q"
- $\hat{i},\ \hat{j},\ \hat{k}$: magnitude 1 (no units), purely directional information
- $\hat{r}$: unit vector pointing from origin to point ("straight outward from point" like $\bar{E}$)

$$\vec{E} = \frac{1}{4\pi\epsilon_0}\frac{q}{r^2}\hat{r} \qquad \text{(electric field of a point charge)}$$

- applies to q < 0 ($-\hat{r}$ points towards charge)