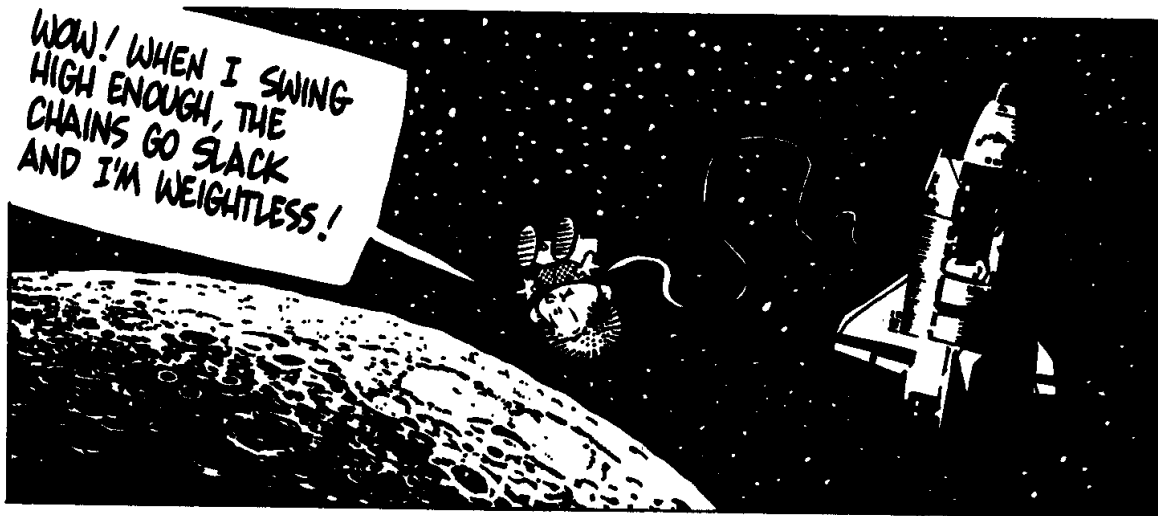


# ■ Theme Music: Fleetwood Mac

## *Silver Springs*

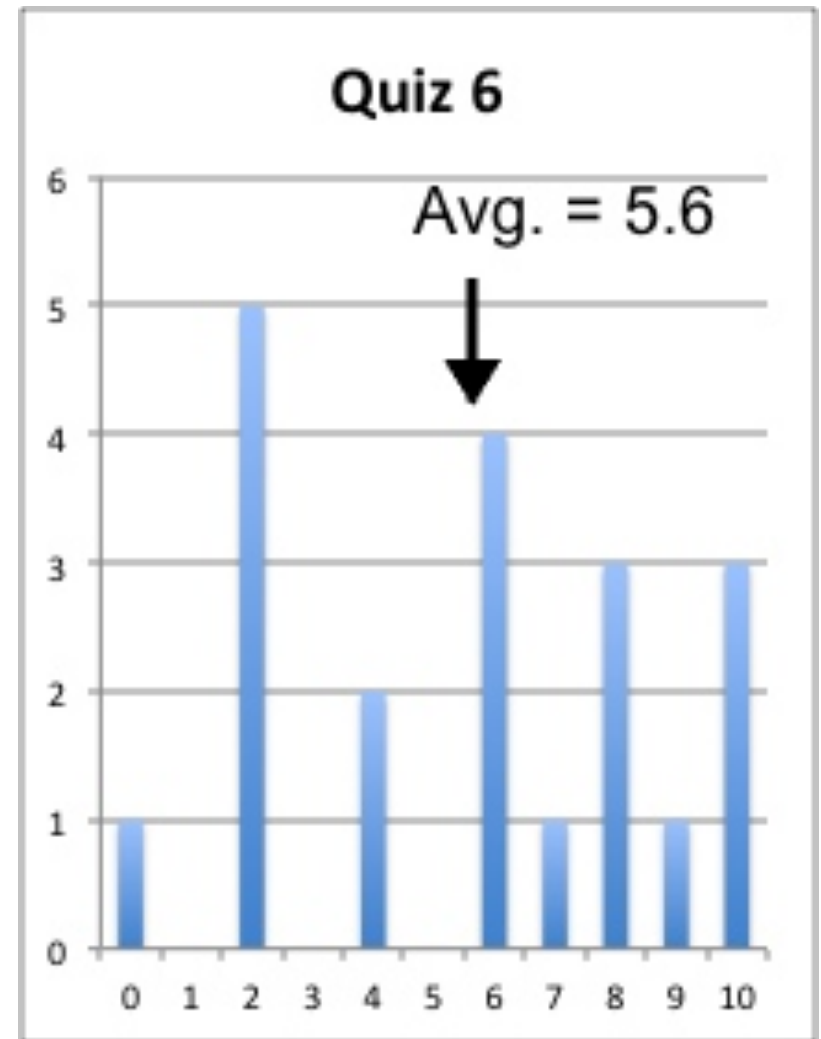
### Cartoon: Pat Brady

## *Rose is Rose*



# Quiz 6

	6.1	6.2.1	6.2.2	6.2.3
A	0%	0%	10%	0%
B	5%	70%	25%	55%
C	45%	5%	45%	15%
D	10%	20%	15%	25%
E	45%	5%	5%	5%
F	65%			
G	5%			



# Foothold ideas: Kirchhoff's principles



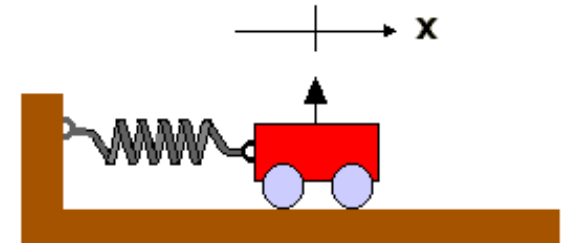
1. ***Flow rule***: The total amount of current flowing into any volume in an electrical network equals the amount flowing out.
  2. ***Ohm's law***: in a resistor,  $\Delta V = IR$
  3. ***Loop rule***: Following around any loop in an electrical network the potential has to come back to the same value (sum of drops = sum of rises).
- ***The Constant Potential Corollary***: Along any part of a circuit with 0 resistance,  $\Delta V = 0$ , i.e.,  $V$  is constant.

# Foothold ideas: Harmonic oscillation



- There is an equilibrium (balance) point where the mass can stay without moving.
- Whichever way the mass moves, the force is in the direction of pushing it back to its equilibrium position.
- When it gets back to its equilibrium, it's still moving so it overshoots.

# Model system: Mass on a Spring

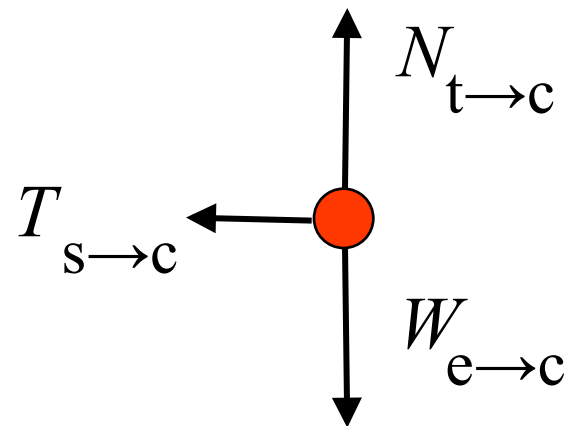
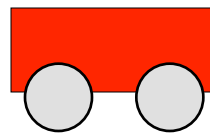
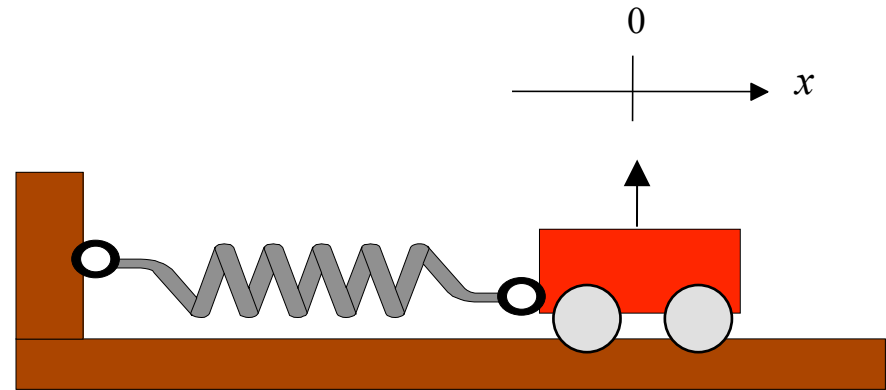


- Consider a cart of mass  $m$  attached to a light (mass of spring  $\ll m$ ) spring.
- Choose the coordinate system so that when the cart is at 0 the spring is at its rest length
- Recall the properties of a (nice) spring.
  - When it is pulled or pushed on both ends it changes its length.

$$T = k\Delta l$$

# Analyzing the forces: cart & spring

- FBD:  
What are  
the forces  
acting on the cart?



# Doing the Math: The Equation of Motion

- The N2 equation for the cart is

$$a = \frac{F_{net}}{m} = -\frac{kx}{m} = -\left(\frac{k}{m}\right)x$$

- What kind of a quantity is  $k/m$ ?

$$\left[\frac{k}{m}\right] =$$

# Mathematical structure

- Express  $a = F^{\text{net}}/m$  in terms of derivatives.

$$\frac{d^2 x}{dt^2} = -\omega_0^2 x$$

- Except for the constant, this is like having a functions that is its own second derivative.

$$\frac{d^2 f}{dt^2} = -f$$

- In calculus, we learn that  $\sin(t)$  and  $\cos(t)$  work like this. How about:  $x = \cos t$  ?