

March 1, 2013

Physics 132

Prof. E. F. Redish

- **Theme Music: Duke Ellington**  
*Take the A Train*
- **Cartoon: Lynn Johnson**  
*For Better or for Worse*



## Foothold principles: Newton's Laws

- Newton 0:
  - An object responds **only** to the forces it feels and only at the instant it feels them.
- Newton 1:
  - An object that feels a net force of 0 keeps moving with the same velocity (which may = 0).
- Newton 2:
  - An object that is acted upon by other objects changes its velocity according to the rule  $\vec{a}_A = \vec{F}_A^{net} / m_A$
- Newton 3:
  - When two objects interact the forces they exert on each other are equal and opposite.  $\vec{F}_{A \rightarrow B}^{type} = -\vec{F}_{B \rightarrow A}^{type}$



## Foothold ideas: Kinetic Energy and Work



- Newton's laws tell us how velocity changes. The Work-Energy theorem tells us how speed (independent of direction) changes.
- Kinetic energy =  $\frac{1}{2}mv^2$
- Work done by a force =  $F_x\Delta x$  or  $F_{\parallel}\Delta r$  (part of force  $\parallel$  to displacement)
- Work-energy theorem:  $\Delta(\frac{1}{2}mv^2) = F_{\parallel}^{net} \Delta r$  (small step)  
 $\Delta(\frac{1}{2}mv^2) = \int_i^f F_{\parallel}^{net} dr$  (any size step)

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## Foothold ideas: Potential Energy



- The work done by some forces only depends on the change in position. Then it can be written  

$$\vec{F} \cdot \Delta\vec{r} = -\Delta U$$
*U* is called a *potential energy*.
- For gravity,  $U_{gravity} = mgh$   
 For a spring,  $U_{spring} = \frac{1}{2}kx^2$   
 For electric force,  $U_{electric} = k_c Q_1 Q_2 / r_{12}$
- Potential to force:  $\vec{F} = -\frac{\Delta U}{\Delta\vec{r}} = -\left(\frac{\partial U}{\partial x}\hat{i} + \frac{\partial U}{\partial y}\hat{j} + \frac{\partial U}{\partial z}\hat{k}\right) = -\vec{\nabla}U$

*The force associated with a PE at a given place points  
 "downhill" – in the direction where the PE falls the fastest.*

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## Foothold ideas: Energy



- Kinds of energy (macro)
  - Kinetic
  - Potential
  - Thermal
  - Chemical
- Kinds of energy (micro)?
- First law of thermodynamics
  - Conservation of total energy

Energy needed to add internal energy at constant pressure (Enthalpy)

Internal energy

Thermal energy entering

Work done on the rest of the world

$$\Delta U = Q - W$$

$$\Delta H = \Delta U + p\Delta V$$

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## Foothold ideas: Inter-atomic interactions



- The interaction between atoms arises from the combination of the electrical forces of its components (electrons and nuclei).
  - It can be quite complex and involve electron sharing and chemical bonds.
  - The complexity arises from the quantum character of electrons.
- Despite this complexity, a simple potential model summarizes many features of a two-atom interaction.

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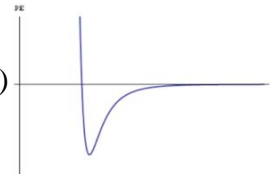
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## Foothold ideas: Inter-atomic potentials



- The interaction between neutral atoms includes an attraction at long-range that arises from the fluctuating charge distribution in each atom; the PE behaves like  $1/r^6$ .
- When the atoms are pressed close, they repel each other strongly; both because the +nuclei repel and because of the Pauli principle (two electrons cannot be in the same state).
- Two commonly used models are:
  - The Lennard-Jones potential ( $A/r^{12}-B/r^6$ )
  - The Morse potential (exponentials)



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## Foothold principles: Randomness



- Matter is made of molecules in constant motion and interaction. This motion moves stuff around.
- If the distribution of a chemical is non-uniform, the randomness of molecular motion will tend to result in molecules moving from more dense regions to less.
- This is not directed but is an emergent phenomenon arising from the combination of random motion and non-uniform concentration.

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## Foothold ideas: Thermal Equilibrium & Equipartition



- Degrees of freedom – where energy can reside in a system.
- Thermodynamic equilibrium is dynamic. Changes keep happening, but equal amounts in both directions.
- Equipartition – At equilibrium, the same energy density in all space and in all DoFs.

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## Foothold ideas: Microstate and macrostates



- A *microstate* is a specific distribution of energy telling how much is in each DoF.
- A *macrostate* is a statement about some average properties of a state (pressure, temperature, density,...).
  - A given macrostate corresponds to many microstates.
- If the system is sufficiently random, each microstate is equally probable. As a result, the probability of seeing a given macrostate depends on how many microstates it corresponds to.

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Foothold ideas:  
Thermal Equilibrium & Equipartition



- ***Degrees of freedom*** – where energy can reside in a system.
- ***Thermodynamic equilibrium is dynamic*** – Changes keep happening, but equal amounts in both directions.
- ***Equipartition*** – At equilibrium, the same energy density in all space and in all DoFs.

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Foothold ideas:  
Entropy




- ***Entropy*** – an extensive measure of how well energy is spread in an object.
- ***Entropy measures*** –
  - The number of microstates in a given macrostate  $S = k_B \ln(W)$
  - The amount that the energy of a system is spread among the various degrees of freedom
- ***Change in entropy*** upon heat flow  $\Delta S = \frac{Q}{T}$

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## Foothold ideas: The Second Law of Thermodynamics



- Systems composed of a large number of particles spontaneously move toward the thermodynamic (macro) state that correspond to the largest possible number of particle arrangements (microstates).
  - The 2<sup>nd</sup> law is probabilistic. Systems show fluctuations – violations that get proportionately smaller as  $N$  gets large.
- Systems that are not in thermodynamic equilibrium will spontaneously transform so as to increase the entropy.
  - The entropy of any particular system can decrease as long as the entropy of the rest of the universe increases more.
- The universe tends towards states of increasing chaos and uniformity. (Is this contradictory?)

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## Foothold ideas: Transforming energy



- Internal energy:  $\Delta U$   
thermal plus chemical
- Enthalpy:  $\Delta H = \Delta U + p\Delta V$   
internal plus amount needed  
to make space at constant  $p$
- Gibbs free energy:  $\Delta G = \Delta H - T\Delta S$   
enthalpy minus amount associated with raising  
entropy of the rest of the universe due to energy  
dumped
- A process will go spontaneously if  $\Delta G < 0$ .

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Spontaneity...

$$\Delta G = \Delta H - T\Delta S$$

$\uparrow$                        $\uparrow$                        $\uparrow$   
 $-T\Delta S_{\text{total}}$                $-T\Delta S_{\text{surroundings}}$                $T\Delta S_{\text{system}}$

The sign of the Gibbs Free Energy change indicates spontaneity!

$$\Delta G < 0 \rightarrow \Delta S_{\text{total}} > 0 \rightarrow \text{spontaneous}$$

$$\Delta G > 0 \rightarrow \Delta S_{\text{total}} < 0 \rightarrow \text{not spontaneous}$$

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## Foothold ideas: Energy distribution



- Due to the randomness of thermal collisions, even in (local) thermal equilibrium a range of energy is found in each degree of freedom.
- The probability of finding an energy  $E$  is proportional to the Boltzmann factor

$$P(E) \propto e^{-E/k_B T} \quad (\text{for one DoF})$$

$$P(E) \propto e^{-E/RT} \quad (\text{for one mole})$$

- At 300 K,  $k_B T \sim 1/40$  eV  
 $N_A k_B T = RT \sim 2.4$  kJ/mol

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### Foothold ideas:

#### Charge – A hidden property of matter

- Matter is made up of two kinds of electrical matter (positive and negative) that usually cancel very precisely.
- Like charges repel, unlike charges attract.
- Bringing an unbalanced charge up to neutral matter polarizes it, so both kinds of charge attract neutral matter
- The total amount of charge (pos – neg) is constant.



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### Foothold ideas:

#### Conductors and Insulators

- Insulators
  - In some matter, the charges they contain are bound and cannot move around freely.
  - Excess charge put onto this kind of matter tends to just sit there (like spreading peanut butter).
- Conductors
  - In some matter, charges in it can move around throughout the object.
  - Excess charge put onto this kind of matter redistributes itself or flows off (if there is a conducting path to ground).



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## Foothold idea: Coulomb's Law



- All objects attract each other with a force whose magnitude is given by

$$\vec{F}_{q \rightarrow Q} = -\vec{F}_{Q \rightarrow q} = \frac{k_C q Q}{r_{qQ}^2} \hat{r}_{q \rightarrow Q}$$

- $k_C$  is put in to make the units come out right.

$$k_C = 9 \times 10^9 \text{ N}\cdot\text{m}^2 / \text{C}^2$$

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## Foothold ideas: Energies between charge clusters



- Atoms and molecules are made up of charges.
- The potential energy between two charges is

$$U_{12}^{elec} = \frac{k_C Q_1 Q_2}{r_{12}} \quad \text{No vectors!}$$

- The potential energy between many charges is

$$U_{12\dots N}^{elec} = \sum_{i < j=1}^N \frac{k_C Q_i Q_j}{r_{ij}} \quad \text{Just add up all pairs!}$$

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## Foothold idea: Fields



- *Test particle*
  - We pay attention to what force it feels. We assume it does not have any affect on the source particles.
- *Source particles*
  - We pay attention to the forces they exert and assume they do not move.
- *Physical field*
  - We consider what force a test particle would feel if it were at a particular point in space and divide by its coupling strength to the force. This gives a vector at each point in space.

$$\vec{g} = \frac{1}{m} \vec{W}_{E \rightarrow m} \quad \vec{E} = \frac{1}{q} \vec{F}_{\text{all charges} \rightarrow q} \quad V = \frac{1}{q} U_{\text{all charges} \rightarrow q}^{elec}$$

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## Foothold ideas: Electric potential energy and potential



- The potential energy between two charges is
- The potential energy of many charges is
- The potential energy added by adding a test charge  $q$  is

$$U_{12}^{elec} = \frac{k_C Q_1 Q_2}{r_{12}}$$

$$U_{12\dots N}^{elec} = \sum_{i < j = 1}^N \frac{k_C Q_i Q_j}{r_{ij}}$$

$$\Delta U_q^{elec} = \sum_{i=1}^N \frac{k_C q Q_i}{r_{iq}} = qV$$

= the voltage at the position of the test charge

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## Units

- Gravitational field  
units of  $g$  = Newtons/kg
- Electric field  
units of  $E$  = Newtons/C
- Electric potential  
units of  $V$  = Joules/C = Volts
- Energy =  $qV$  so  $e\Delta V$  = the energy gained by an electron (charge  $e = 1.6 \times 10^{-19}$  C) in moving through a change of  $\Delta V$  volts.  
 $1 \text{ eV} = 1.6 \times 10^{-19} \text{ J}$

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## Foothold ideas: Electric charges in materials



- The electric field inside the body of a static conductor (no moving charges) is zero.
- The entire body of a static conductor (no charges moving through it) is at the same potential.
- The average electric field in an insulator is reduced (due to the polarization of the material by the field) by a factor that is a property of the material: the dielectric constant,  $\kappa$ .  
(Sometimes written in biology as  $\epsilon$ ) Since  $\kappa$  is the ratio of two fields, it is dimensionless.

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## Foothold ideas: Capacitors

$$\Delta V = E\Delta x = Ed$$

$$E = 4\pi k_c \sigma = 4\pi k_c \frac{Q}{A} \Rightarrow Q = \left( \frac{A}{4\pi k_c} \right) E$$

$$Q = \left( \frac{A}{4\pi k_c d} \right) \Delta V$$

$$Q = C\Delta V$$

What does this  
"Q" stand for?

$$C = \frac{\kappa \epsilon_0 A}{d}$$

If plates are separated  
by a material

$$\text{Energy stored} = \frac{1}{2} Q\Delta V$$

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