

# Outline

## Waves

**Midterm II FRIDAY**

**Office hours in Course Center Thursday 1-2 and 5-6.30**

# Foothold principles: Mechanical waves



- *Key concept:* We have to distinguish the motion of the bits of matter and the motion of the pattern.
- *Mechanism:* the pulse propagates by each bit of string pulling on the next.
- *Pattern speed:* a disturbance moves into a medium with a speed that depends on the properties of the medium (but not on the shape of the disturbance)

$$v_0 = \sqrt{\frac{T}{\mu}}$$

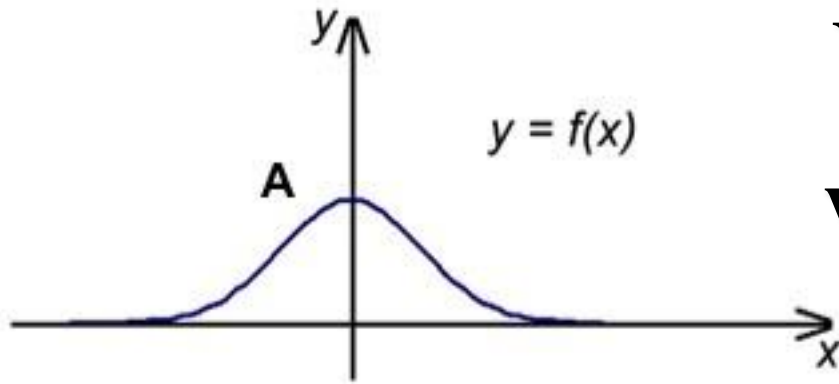
$v_0$  = speed of pulse

$T$  = tension of spring

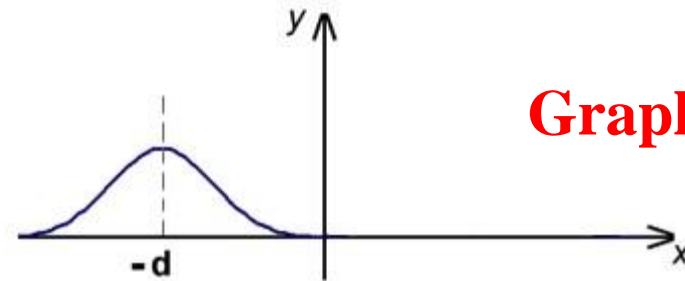
$\mu$  = mass density of spring ( $M/L$ )

- *Matter speed:* the speed of the bits of matter depend on both the size and shape of the pulse and pattern speed.

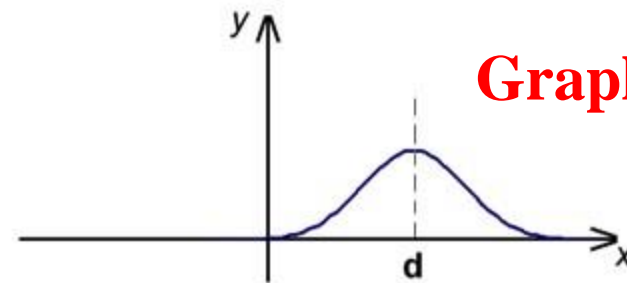
# Which goes with which?



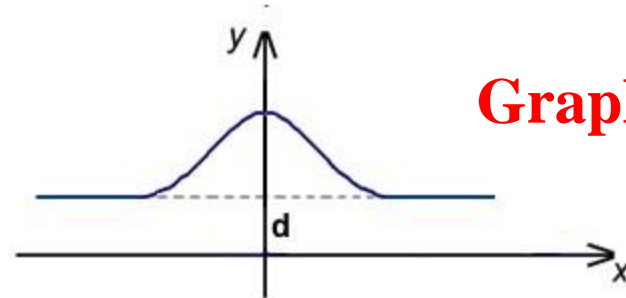
1.  $y = f(x + d)$
2.  $y = f(x - d)$
3.  $y = f(x) + d$
4.  $y = f(x) - d$
5. You can't tell if you don't know the form of  $f$ .
6. You can't tell for some other reason.



**Graph I**



**Graph II**



**Graph III**

# The math

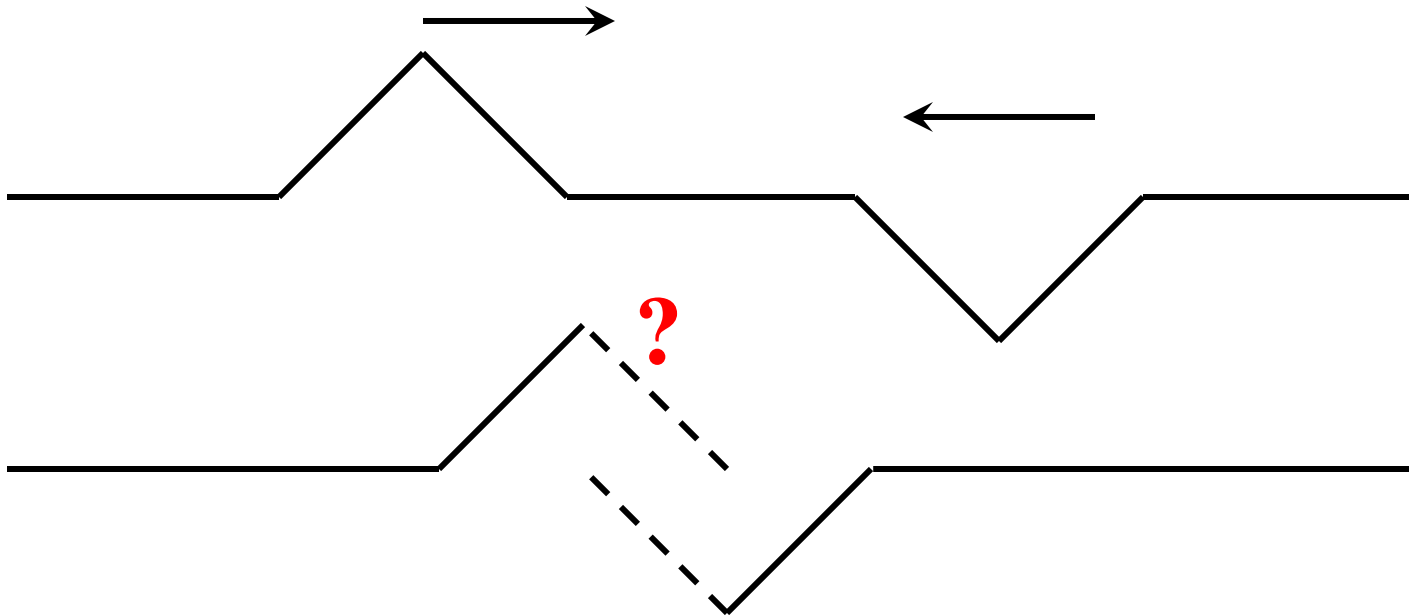
- We express the position of a bit of string at a particular time by labeling which bit of string by its  $x$  position, at  $x$  at time  $t$  the position of the string is  $y(x,t)$ .
- Since subtracting a  $d$  from the argument of a function ( $f(x) \rightarrow f(x - d)$ ) shifts the graph of the function to the right by an amount  $d$ , if we want to set the graph of a shape  $f(x)$  into motion at a constant speed, we just need to set  $d = v_0 t$  and take

$$f(x) \rightarrow f(x - v_0 t)$$

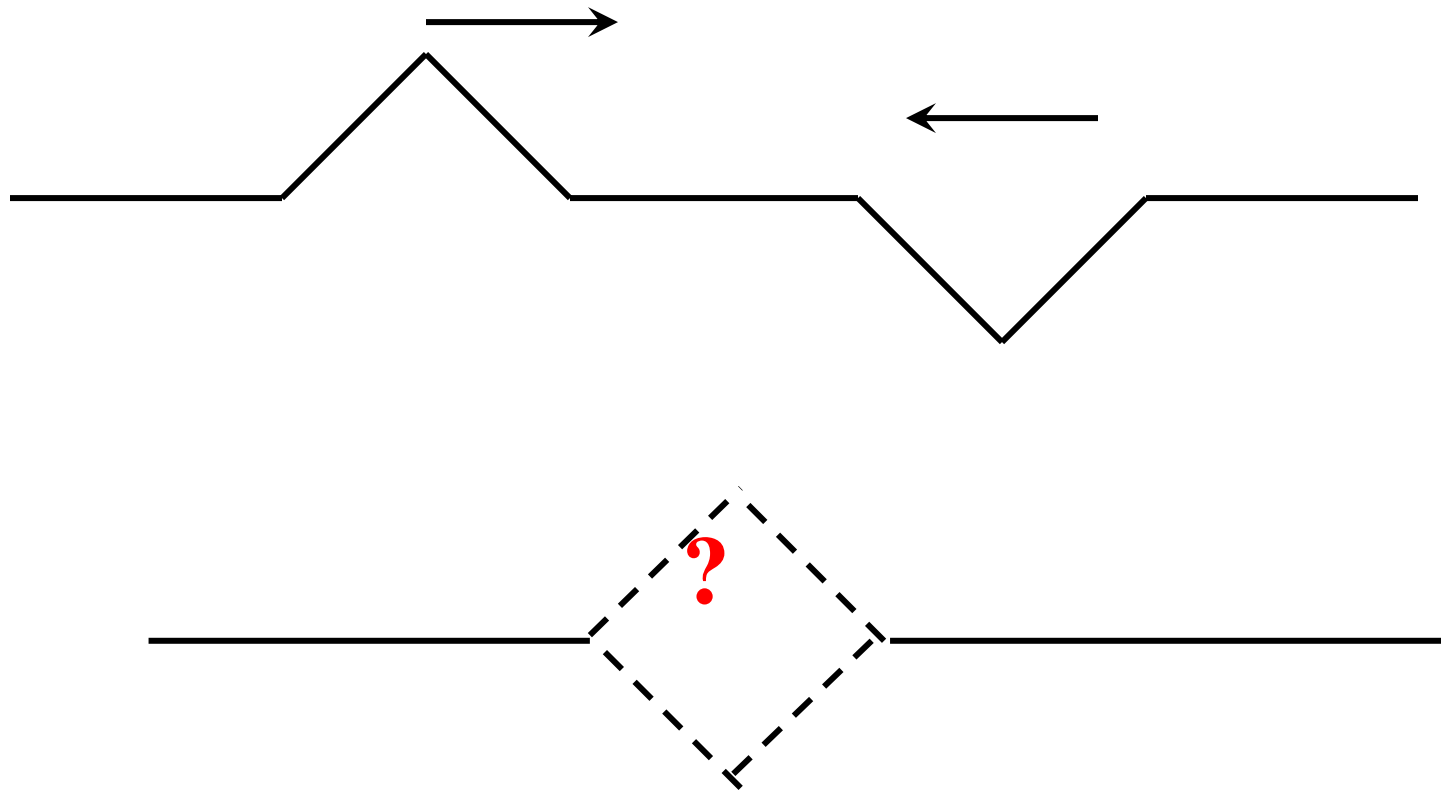
# How do waves combine?

We know how one wave moves.

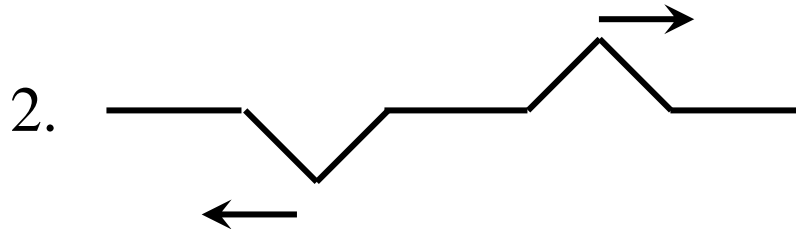
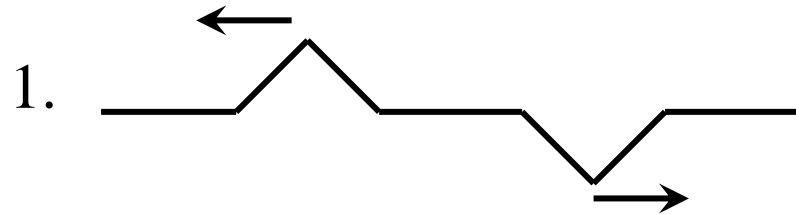
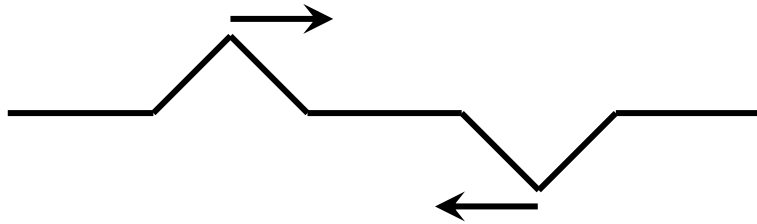
What happens when we get two waves on top of each other?



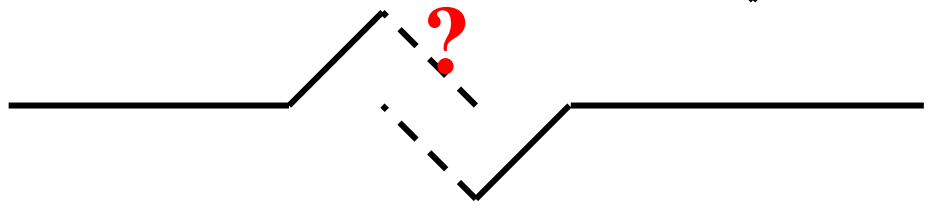
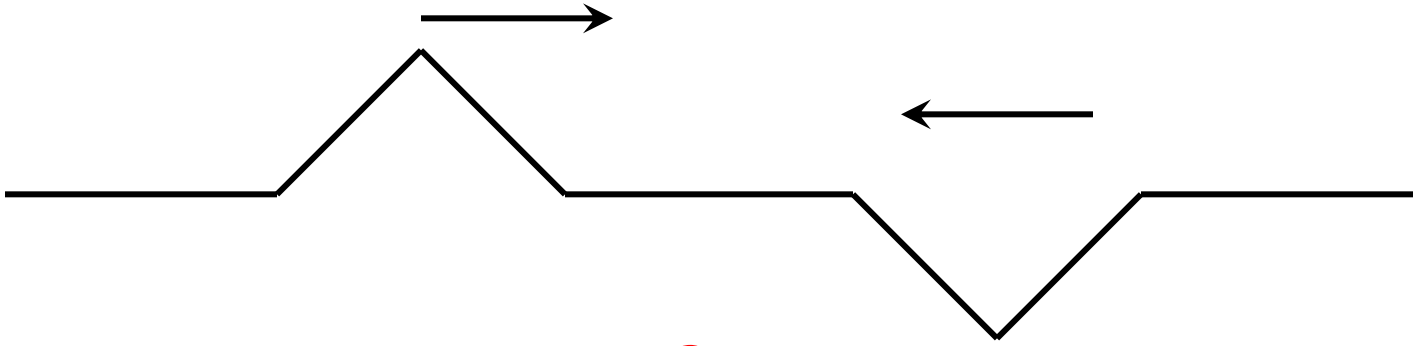
What happens  
when they overlap perfectly?



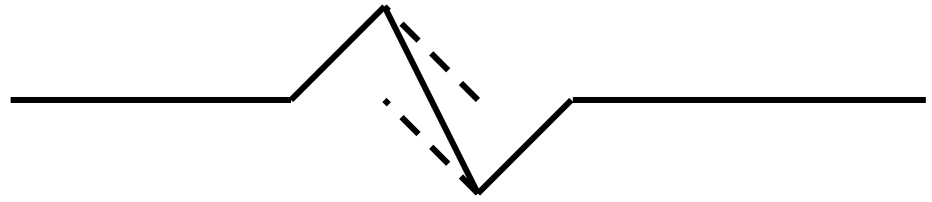
# What happens after the waves collide?



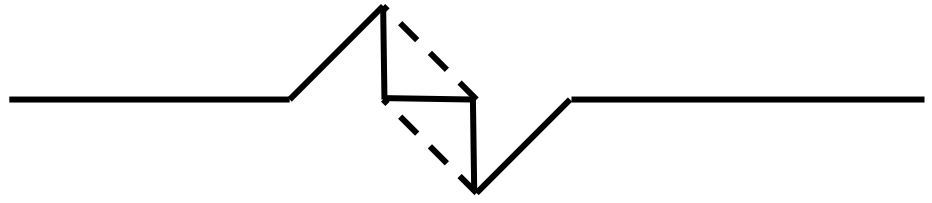
4. Other



1.



2.

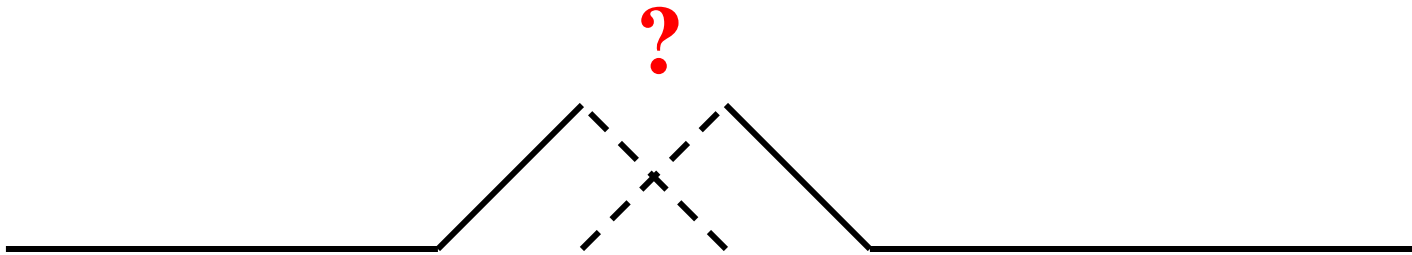


3.

Other



# How about on the same side?



# Sinusoidal waves

- Suppose we make a continuous wiggle. When we start our clock ( $t = 0$ ) we might have created shape something like

$$y(x, 0) = A \sin kx$$

Why do we need a "k"

- If this moves in the +x direction, at later times it would look like

$$y(x, t) = A \sin k(x - v_0 t)$$