

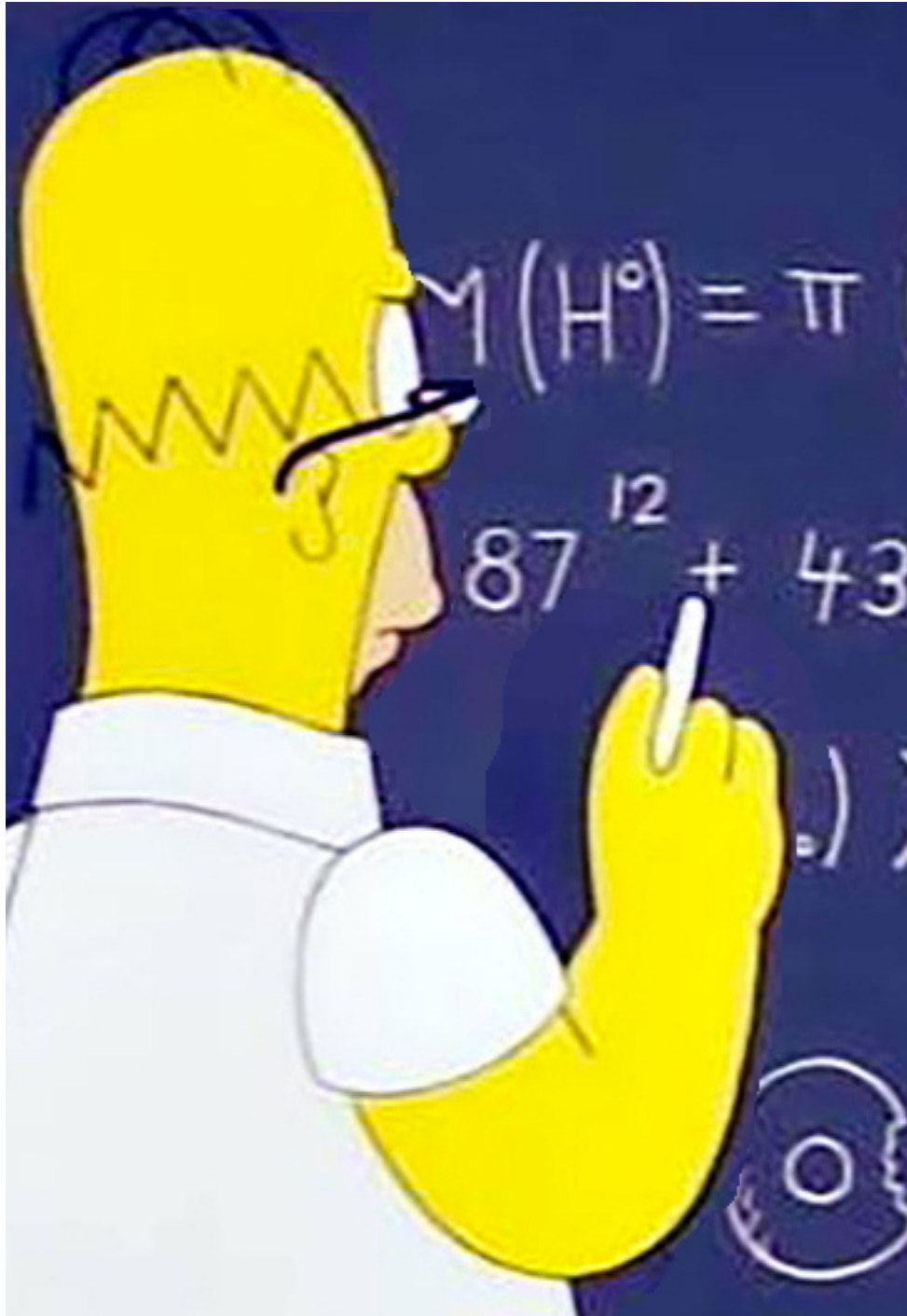
■ **Theme Music: Steve Dorff**

*Every which way but loose*

■ **Cartoon: Bob Thaves**

*Frank & Ernest*





# *The Equation of the Day*

## Vectors

$$\vec{r} = x\hat{i} + y\hat{j}$$

# Review of Vectors

## (2-dimensional coordinates)

- We have 2 directions to specify. We must
  - Choose a reference point (origin)
  - Pick 2 perpendicular axes (x and y)
  - Choose a scale
- We specify our x and y directions by drawing little arrows of unit length in their positive direction.  $\hat{i}, \hat{j}$

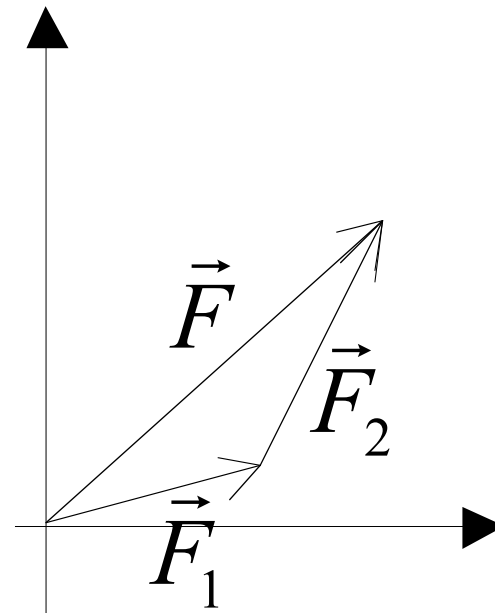
- A force vector is written

$$\vec{F} = F_x \hat{i} + F_y \hat{j} = (F_x, F_y)$$

# Adding Forces

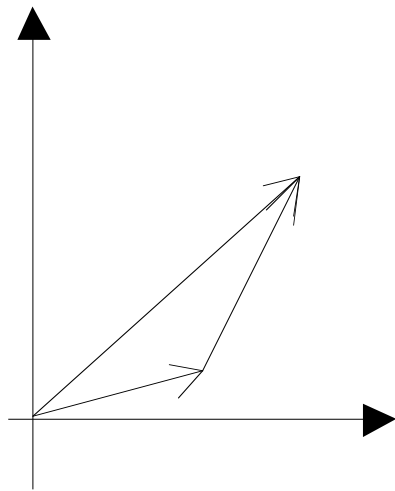
- We define the sum of two vectors as if they were successive displacements.

$$\vec{F} = \vec{F}_1 + \vec{F}_2$$

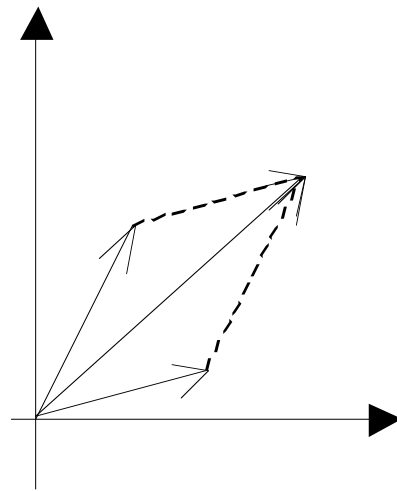


# Adding Vectors: Methods

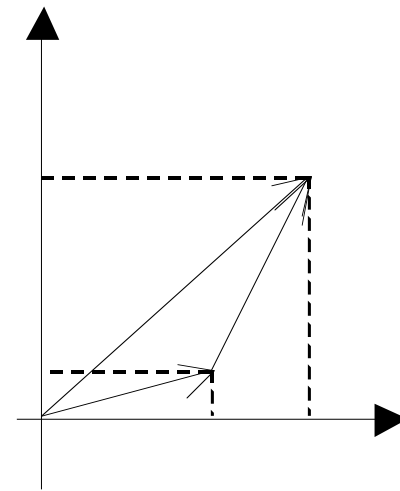
- There are 3 mathematical ways to add vectors



head  
to tail



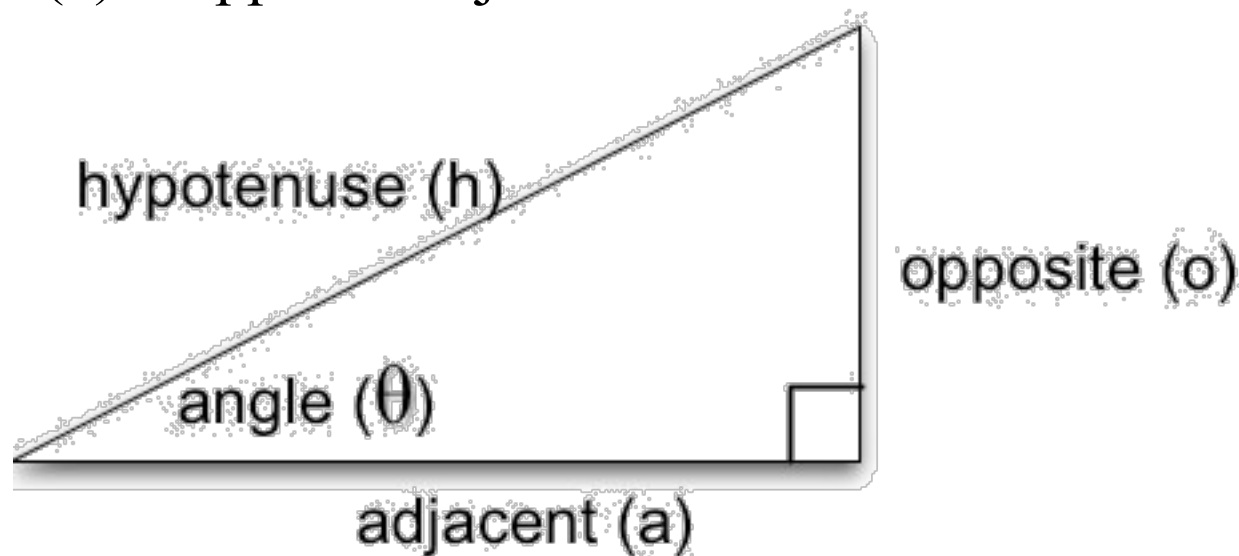
parallelogram  
rule



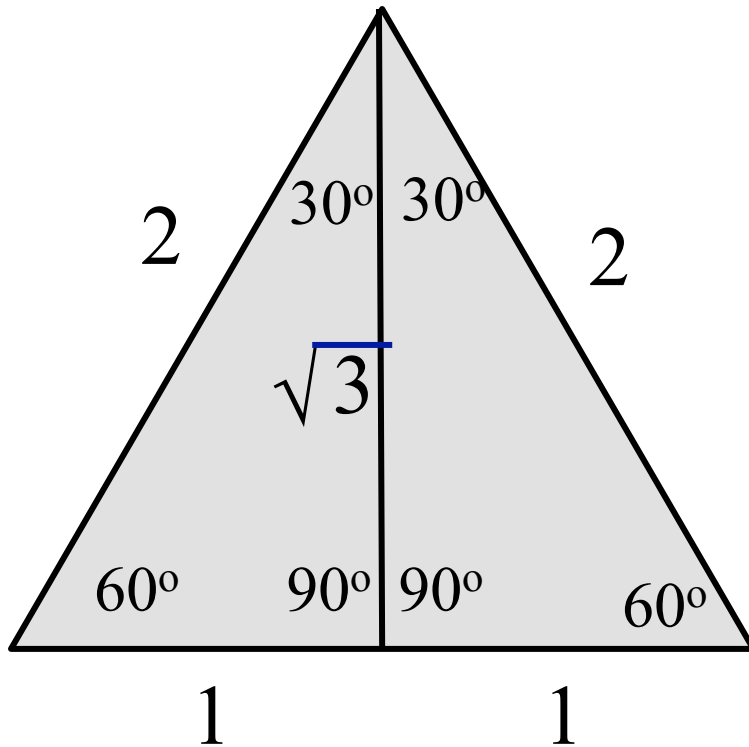
add components  
(may use trig)

# Trig review

- The ratios of a triangle's sides only depend on  $\theta$ .
  - $\sin(\theta) = \text{opposite}/\text{hypotenuse}$
  - $\cos(\theta) = \text{adjacent}/\text{hypotenuse}$
  - $\tan(\theta) = \text{opposite}/\text{adjacent}$ .



# Useful examples



$$\sin(30^\circ) = \frac{1}{2}$$

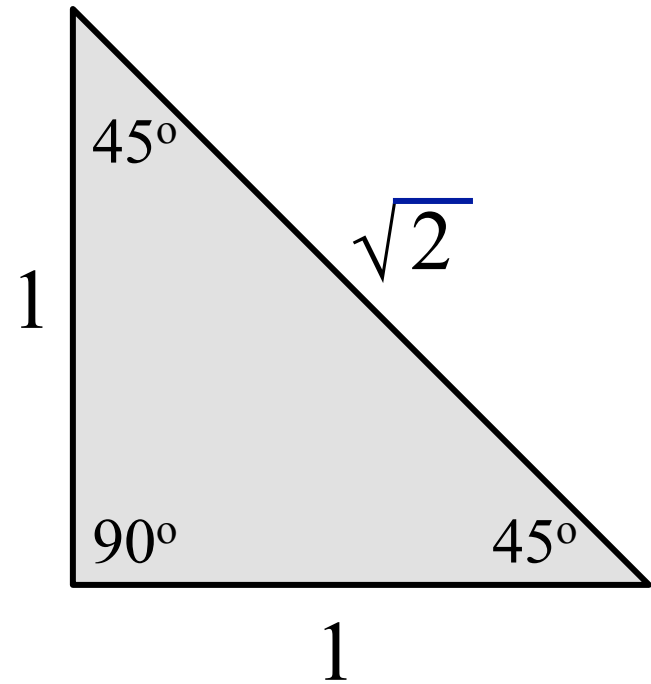
$$\cos(30^\circ) = \frac{\sqrt{3}}{2}$$

$$\tan(30^\circ) = \frac{1}{\sqrt{3}}$$

$$\sin(60^\circ) = \frac{\sqrt{3}}{2}$$

$$\cos(60^\circ) = \frac{1}{2}$$

$$\tan(60^\circ) = \sqrt{3}$$



$$\sin(45^\circ) = \frac{1}{\sqrt{2}}$$

$$\cos(45^\circ) = \frac{1}{\sqrt{2}}$$

$$\tan(45^\circ) = 1$$

# Vectors with trig – by components

$$\vec{A} = A_x \hat{i} + A_y \hat{j}$$

$$= (A \cos(\theta)) \hat{i} + (A \sin(\theta)) \hat{j}$$

$$\vec{B} = B_x \hat{i} + B_y \hat{j}$$

$$= (-B \sin(\phi)) \hat{i} + (B \cos(\phi)) \hat{j}$$

$$\vec{A} + \vec{B} = ?$$

