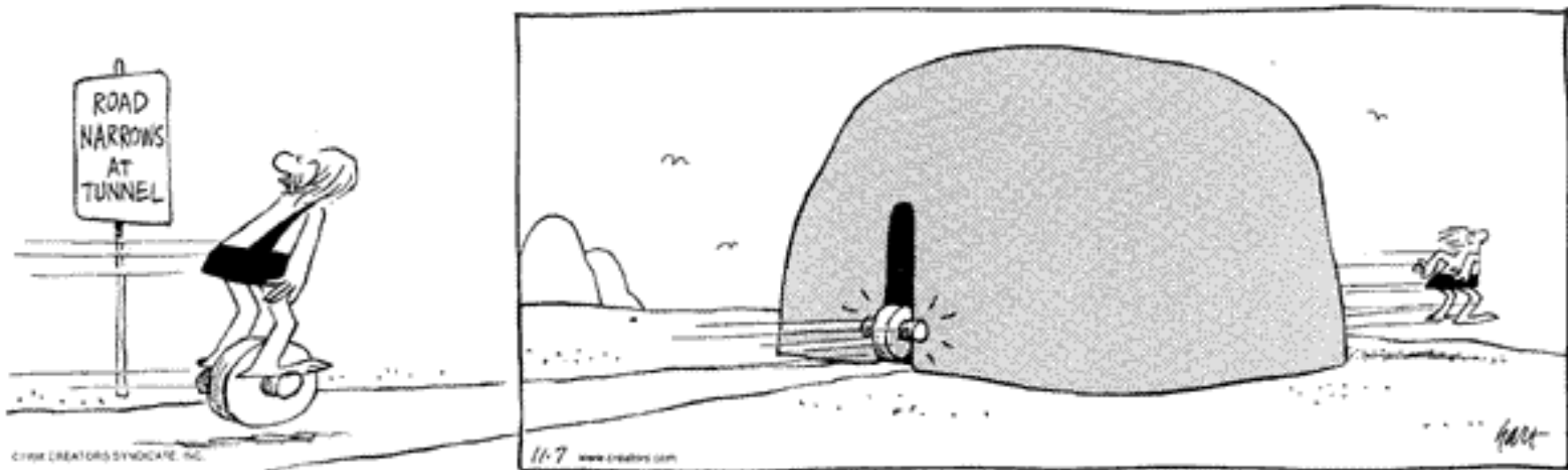


# ■ Theme Music: Run Like an Antelope

*Phish*

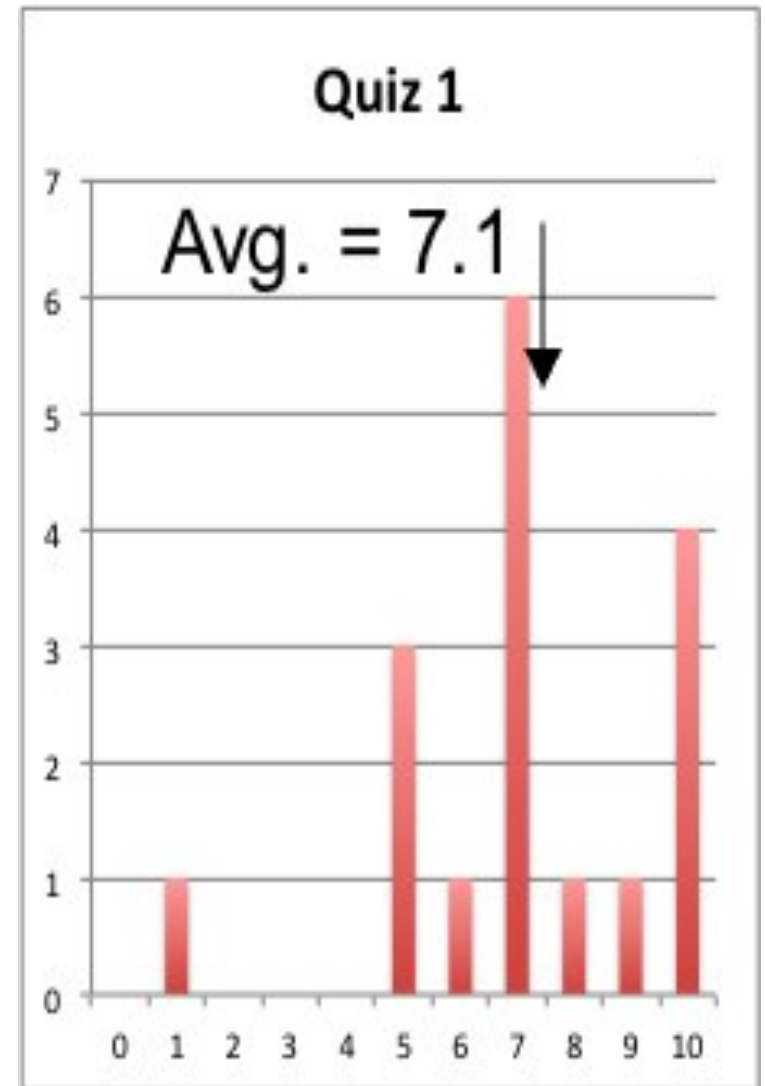
# ■ Cartoon: Johnny Hart

*BC*



# Quiz 1

	1.1		1.2		1.3
<b>a</b>	0%	$mR/v^2$	35%	<b>a</b>	0%
<b>b</b>	29%	$mR/v$	6%	<b>b</b>	88%
<b>c</b>	0%	$mRv^2$	59%	<b>c</b>	0%
<b>d</b>	47%			<b>d</b>	0%
<b>e</b>	18%			<b>e</b>	12%
<b>f</b>	0%			<b>f</b>	0%
<b>g</b>	6%				
<b>h</b>	35%				



# MCAT and Multiple Representations

- **From the recent guide on the revisions taking place to the MCAT. Physical science skills to be tested include:**

## ***MCAT Preview Guide***

### ***Skill 1: Knowledge of Scientific Concepts and Principles***

- Identifying the relationships between different representations of concepts (verbal, symbolic, graphic)
- Using mathematical equations to solve problems

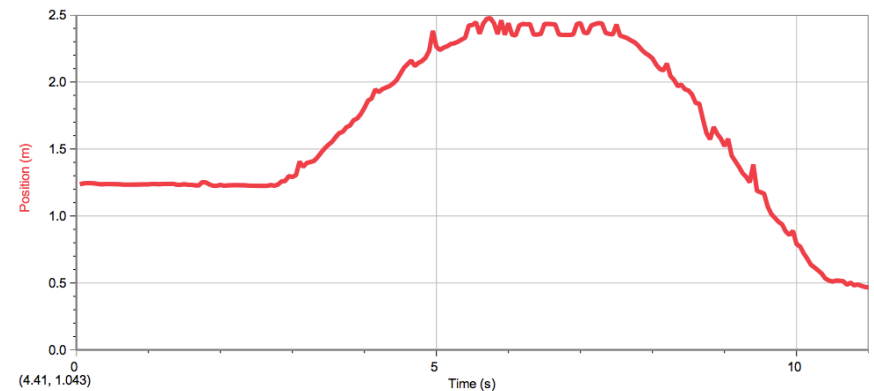
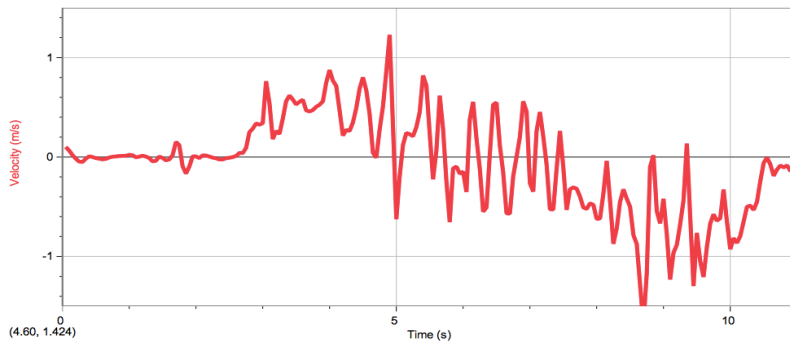
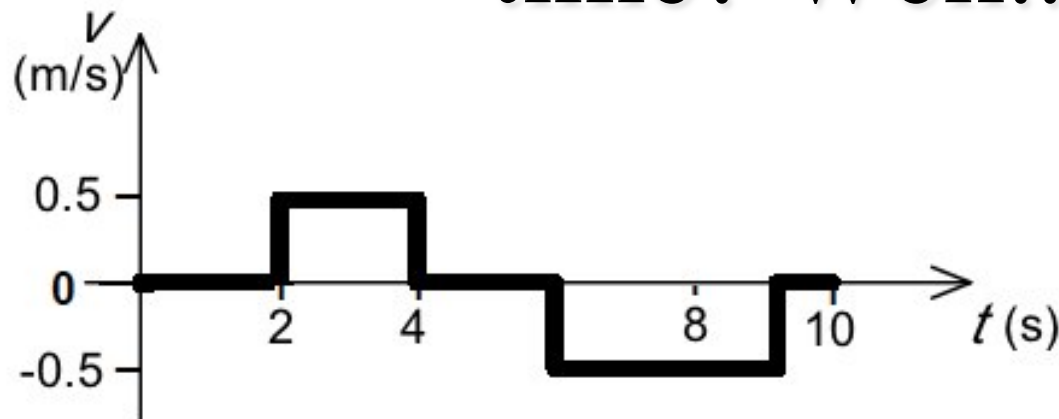
### ***Skill 2: Scientific Reasoning and Problem-solving***

- Determining and using scientific formulas to solve problems

### ***Skill 4: Data-based and Statistical Reasoning***

- Using, analyzing, and interpreting data in figures, graphs, and tables
- Evaluating whether representations make sense for particular scientific observations and data

# Average velocity as a function of time? Well... Yes!



# Foothold ideas: Velocity



- Average velocity is defined by

$$\langle \vec{v} \rangle = \frac{\Delta \vec{r}}{\Delta t} = \frac{\text{vector displacement}}{\text{time it took to do it}}$$

Note: an average velocity goes with a time interval.

- Instantaneous velocity is what we get when we consider a very small time interval (compared to times we care about)

$$\vec{v} = \frac{d\vec{r}}{dt}$$

Note: an instantaneous velocity goes with a specific time.

# Foothold ideas: Acceleration



- Average acceleration is defined by

$$\langle \vec{a} \rangle = \frac{\Delta \vec{v}}{\Delta t} = \frac{\text{change in velocity}}{\text{time it took to do it}}$$

Note: an average acceleration goes with a time interval.

- Instantaneous acceleration is what we get when we consider a very small time interval (compared to times we care about)

$$\vec{a} = \frac{d\vec{v}}{dt}$$

Note: an instantaneous acceleration goes with a specific time.

# Technical term alert!

- Note that in physics we use the term “**acceleration**” in a technically defined way:
  - “acceleration” = changing velocity
- The object may be speeding up or slowing down or keeping the same speed and changing direction. We still say “it is accelerating.”
- In common speech
  - “*acceleration*” = speeding up,
  - “*deceleration*” = slowing down, and
  - “*turning*” = changing direction.
- How many (physics) accelerators are there on your car?

# Uniformly changing motion

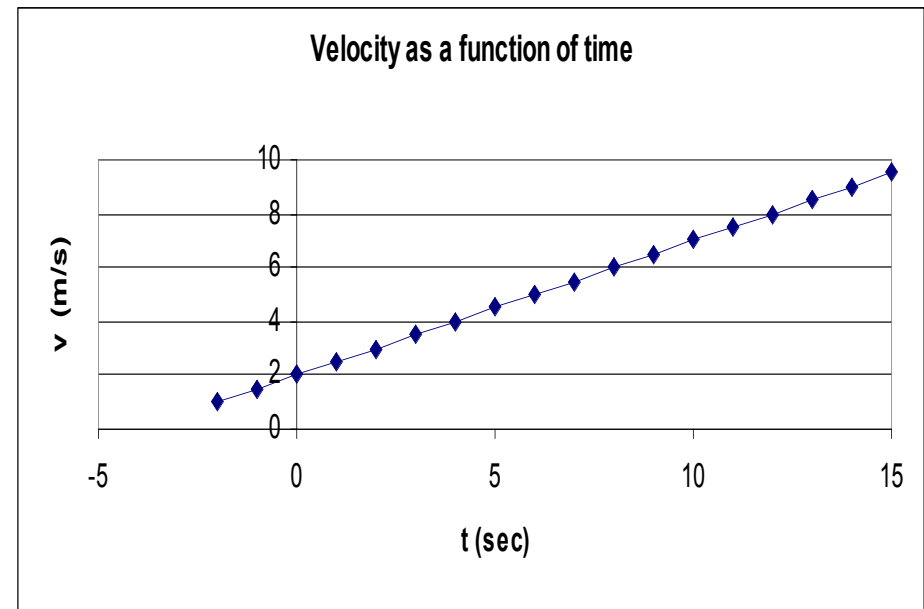
- If an object moves so that it changes its velocity by the same amount in each unit of time, we say it is in uniformly accelerated motion.
- This means the average acceleration will be the same no matter what interval of time we choose.

$$\langle \vec{a} \rangle = \frac{\Delta \vec{v}}{\Delta t} = \vec{a}_0$$

$$\Delta \vec{v} = \vec{a}_0 \Delta t$$

$$\vec{v}(t_2) - \vec{v}(t_1) = \vec{a}_0 \Delta t$$

$$\vec{v}_{final} = \vec{v}_{initial} + \vec{a}_0 \Delta t$$





			9	10	11	12	13
			A	B	H	O	R
			18	A	L	O	N
			19	A	U	R	A
	22			23	E	D	I
	26	25	A	L	B	E	R
31	A	D	I	O			
			35	B	O	O	N
			42	A	K	R	O
	45			49	E	T	O

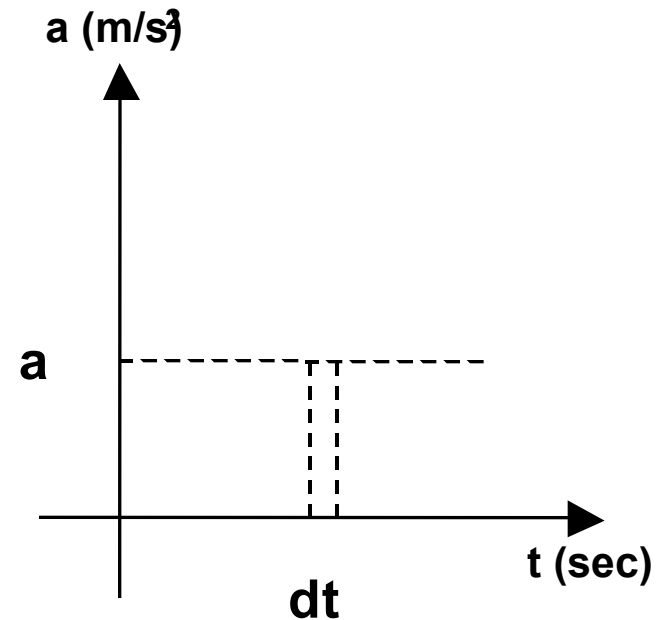
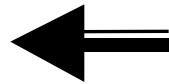
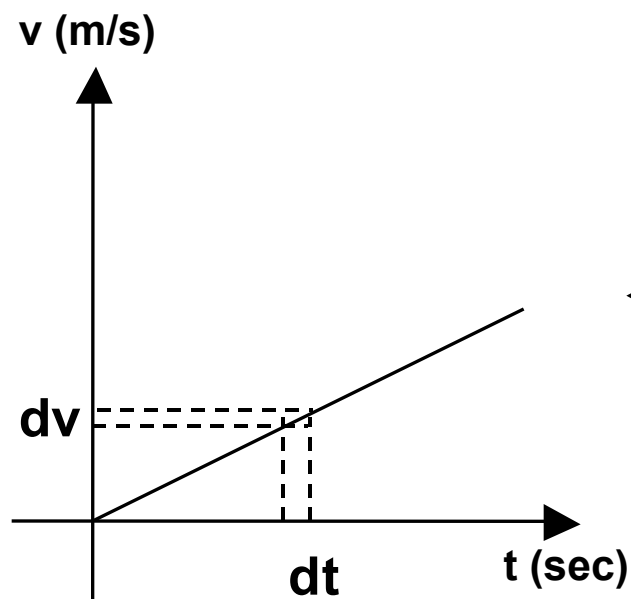


## Difference of two velocities at two (close) times

$$a(t) = \frac{v(t + \Delta t/2) - v(t - \Delta t/2)}{\Delta t}$$

# Acceleration to velocity

		10	11	12	13	14	15
		A	B	H	O	R	
		A	L	O	N	E	
		A	U	R	A	S	
	22		E	D	I	E	
	25	A	L	B	E	R	T
31	A	D	I	O			
	33	B	O	O	N	E	
	42	A	K	R	O	N	
45					E	T	O



$$dv = a(t) dt$$

change in velocity over  
a small time interval

sum ("Σ") in the  
changes in velocity  
over many small  
time intervals

$$v = \sum dv = \int a(t) dt$$

# What have we learned?



- Position  $\hat{r} = x\hat{i} + y\hat{j}$   
(where  $x$  and  $y$  are signed lengths)
- Velocity  $\langle \vec{v} \rangle = \frac{\Delta \vec{r}}{\Delta t}$   $\vec{v} = \frac{d\vec{r}}{dt}$
- Acceleration  $\langle \vec{a} \rangle = \frac{\Delta \vec{v}}{\Delta t}$   $\vec{a} = \frac{d\vec{v}}{dt}$
- Seeing from the motion
- Seeing consistency (graphs & equations)

# Figuring out acceleration

- Look at the y-t, and v<sub>y</sub>-t plots for a ball going up and down.
- Acceleration is the derivative of the velocity. How is the velocity changing? Why?

$$\vec{a} = \frac{d\vec{v}}{dt}$$

