

#### Review of 8/29/2012

- · New class -
  - new physics at the convergence with biology and chemistry
  - taught in a "flipped class" with prereading and hands on in class activity
- · Be aware of how you learn!
  - Develop a framework of "intuition" for scientific reasoning
  - Question whether your intuitive answer makes sense
  - Learn to explain your reasoning to your peers and to challenge their reasoning

#### **Topics**

- Math in natural sciences
- Units and dimensions
- Estimation
- Scaling

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# Math in math vs Math in the natural sciences

I keep comments anonymous (add your name to the comment if you would like me to know your name associated with a comment)

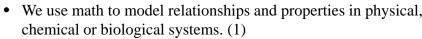
"Does "math in math" refer to math that is purely theoretical, without any context?"

"Isn't calculus considered an evaluation process as well, with problems such as trigonometry- where the answer isn't a designated value but rather a simplified expression from the original, given solution?"

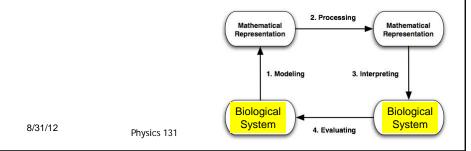
"I would like to know an example where the mathematical equation has taught scientists new insight about a physical system. "

"Why does the article try to explain math in math classes as useless knowledge to get to a meaningless number?"

## Foothold ideas: Modeling the world with math



- Mathematical processing allows us to make predictions (2) from the model that we can interpret (3) for the physical system.
- Very non-natural physical systems such as lasers, transistors have been designed via such "model based extrapolation".
- In biology, steps 1 and 3 are still very hard



## Foothold Idea Dimensional analysis

- Modeling physical systems requires numbers, i.e. measurements

  This is what the
- Measurements have dimensions:

[x] = L means "the dimension of x is a Length"

[t] = T means "the dimension of t is a Time"

[m] = M means "the dimension of m is a Mass"

[v] = L/T means "the dimension of velocity is Length/Time

brackets mean!

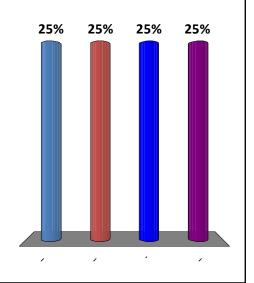
Models allow us to think about how the numbers fit together

<u>A first check on any model - Dimensional analysis:</u> Both sides of an equation have to have the same dimension

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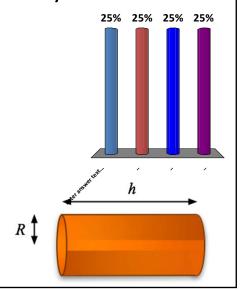
### Which equation represents the volume of a sphere of radius R

- $1.\underline{2}\pi R$
- 2. $\frac{4}{3}\pi R^{2}$ 3. $\frac{4}{3}\pi R^{3}$ 4. $\pi R^{2}$



#### Which equation could represent the surface area of a cylinder?

- 1.  $2\pi R + 2\pi Rh$
- 2.  $2\pi R^2 + 2\pi Rh$
- 3.  $2\pi R^2 + 2\pi h$
- 4.  $\pi R^2 h$



 It says different items can't be added or equated but can't you do that if you convert numbers into the same units or is it in some cases you just can't?

#### **Units**

- Units specify which particular measurement we have chosen.
  - The same Dimension can have different units
  - Units should be manipulated like algebraic quantities.
  - Units can be changed by multiplying by appropriate forms of "1" e.g. 1 = (1 inch)/(2.54 cm)

### Units are important:

#### A 125 Million \$ Mistake

http://en.wikipedia.org/wiki/Mars\_Climate\_Orbiter

Syringe Sizes:

#### An example from a math exam

 Writing the equation in this problem on a physics exam would receive 0 credit and the comment: "This is a meaningless equation!" The population density of trout in a stream is

$$r(x) = 20 \frac{1+x}{x^2+1}$$

where *r* is measured in trout per mile and x is measured in miles. *x* runs from 0 to 10.

(a) Write an expression for the total number of trout in the stream. Do not compute it.

How would you fix this?

#### Foothold Ideas: Estimation – Quantifying experience

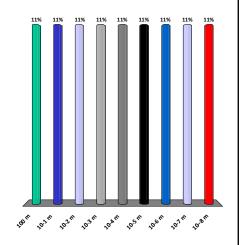


- Use 1-digit arithmetic
- Do figure out your estimations by starting with something you can plausibly know and scale up or down
- Do check your answer to see if it's reasonable
- You will learn useful numbers for biology

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# Estimate the thickness of a page in a textbook.

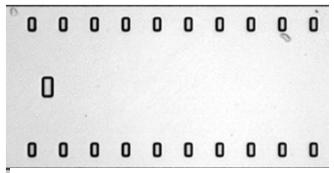
- 1. 10<sup>0</sup> m
- 2. 10<sup>-1</sup> m
- 3. 10<sup>-2</sup> m
- 4. 10<sup>-3</sup> m
- 5. 10<sup>-4</sup> m
- 6. 10<sup>-5</sup> m
- 7. 10<sup>-6</sup> m
- 8. 10<sup>-7</sup> m
- 9. 10<sup>-8</sup> m



#### Estimation Problem

At typical signal strength, how many signaling molecules sweep past a moving amoeboid cell in one minute?

First number to remember: Typical concentration of signaling molecules: 10 nM



**Chemical Signal comes from bottom**