

■ **Theme Music: Wynton Marsalis**

*Where or When?*

■ **Cartoon: Jim Davis**

*Garfield*



# Outline

- Recap: Dimensional Analysis
- The Main Topic: Motion
- Describing Motion:
  - Coordinates in space and time
  - Vectors
  - Graphs
- The Idea of Velocity

# Letting dimensional analysis work for you



- In physics, if we try to add or equate quantities of different dimensions we get nonsense.
- If we didn't maintain dimensional correctness, an equality that worked in one measurement system wouldn't work in another.
- This is a very good way to check your work with equations. (But it's hard to do if you put numbers in too early!\*)

*\* You also won't get much partial credit on exams if you put numbers in too early since we may not be able to tell what equations<sup>3</sup> you are using and why!*

# What have we learned?



- In physics we assign numbers to physical objects by comparison counting against a particular standard.
- We have different kinds of quantities depending on how they were measured and these quantities change in different ways when you change your measuring units.
- It matters *what* you are counting, not just *how much*!
- Only quantities of the same type may be equated (or added) otherwise an equality for one person would not hold for another.

$$1 \text{ cm}^3 + 4 \text{ cm}^3 = 5 \text{ cm}^3$$



$$1 \text{ cm} + 4 \text{ cm}^2 \neq 5 \text{ (anythings)}$$



How would you fix the math  
exam example?

$$r(x) = 20 \frac{1 + x}{x^2 + 1}$$

# Fourth icon: Cat television



- When we do science, we don't try to solve the entire universe at once.
- We restrict our considerations to a limited set of data and try to understand it. Only when we get it do we try to expand further to more situations.
- This is like looking out a window onto a small segment of the world. Since cats like to do this, I call the process “choosing a channel on cat television.”

# The Main Question

*(for this term, at least)*



- Start by choosing a big question and then refining it:

*How do things move?*

**Why choose this?**

- concepts of measurement, rate of change, force are fundamental
- ties to everyday experience so can use and learn to build/refine intuition

# Describing Motion: Space

- Coordinates — telling where something is
- What do we need to do to specify the location of something so someone else can find it?
  - Note the difference between “length” or “distance” and “position”
  - Representing a position mathematically.



# Length vs. Position

- Example: Measure the length of table.
- Example: Measure my position along a line across the room.
- Fish story
- Mathematical model:  
Associating a number with my position.
- Limitations?



# Motion along a straight line (1-dimensional coordinates)

- We specify which direction we are talking about by drawing a little arrow of unit length in the positive direction.
- We specify that we are talking about this arrow in symbols by writing  $\hat{i}$
- A position a distance  $x$  from the origin is written  $\vec{r} = x\hat{i}$
- Note that if  $x$  is negative, it means a vector pointing in the direction opposite to  $\hat{i}$

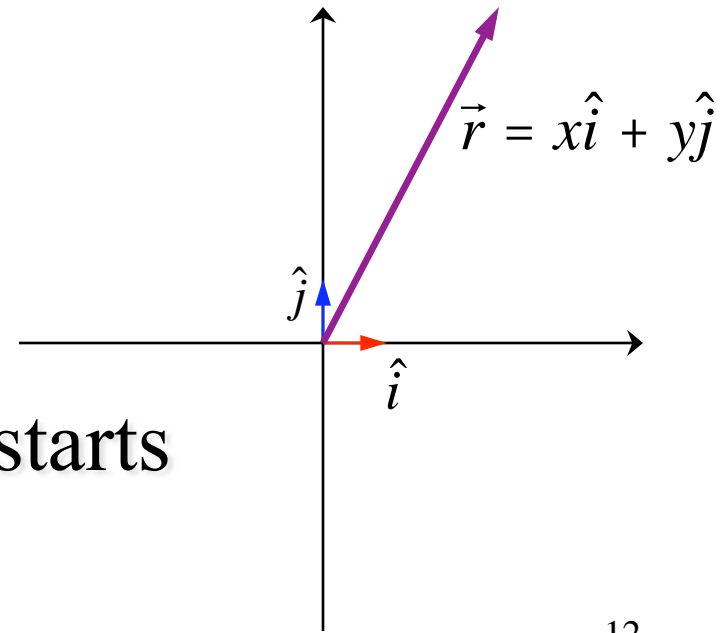
# Coordinates and Vectors

- Set up a coordinate system
  - Pick an origin
  - Pick perpendicular directions
  - Choose a measurement scale
- Each point in space is then specified by three numbers: the  $x$ ,  $y$ , and  $z$  coordinates.
- The position vector for a particular position is an arrow drawn from the origin to that position.

# Motion in a plane

## (2-dimensional coordinates)

- We specify the directions we are talking about by drawing two little arrows of unit length in two perpendicular directions.
- “ $x$ ” and “ $y$ ” are called the coordinates and can be positive or negative.
- A position vector always starts from the origin.



# Describing Motion: Time

- Time — if we're to describe something moving we need to tell when it is where it is.
- Time is a coordinate just like position
  - We need an origin (when we choose  $t = 0$ )
  - a direction (usually times later than 0 are +)
  - a scale (seconds, years, millennia)
- Note the difference between
  - clock reading,  $t$
  - a time interval,  $\Delta t$

**This is like the difference  
between position and length!**

# Writing the math

- Position at a clock time  $t$ :  $\vec{r}(t) = x(t)\hat{i} + y(t)\hat{j}$
- Position at a clock time  $t$ :  
(in 1-D, if we don't want to emphasize direction)  $x(t)$
- Change in position between two times ( $t_1$  and  $t_2$ )  $\Delta\vec{r} = \vec{r}(t_2) - \vec{r}(t_1)$
- Time interval  $\Delta t = t_2 - t_1$

# Displacement

- The displacement is the total change in position.
- If you make one change and then go back, it could cancel out the first change.

$$\vec{r}(t_1) \rightarrow \vec{r}(t_2) \rightarrow \vec{r}(t_3)$$

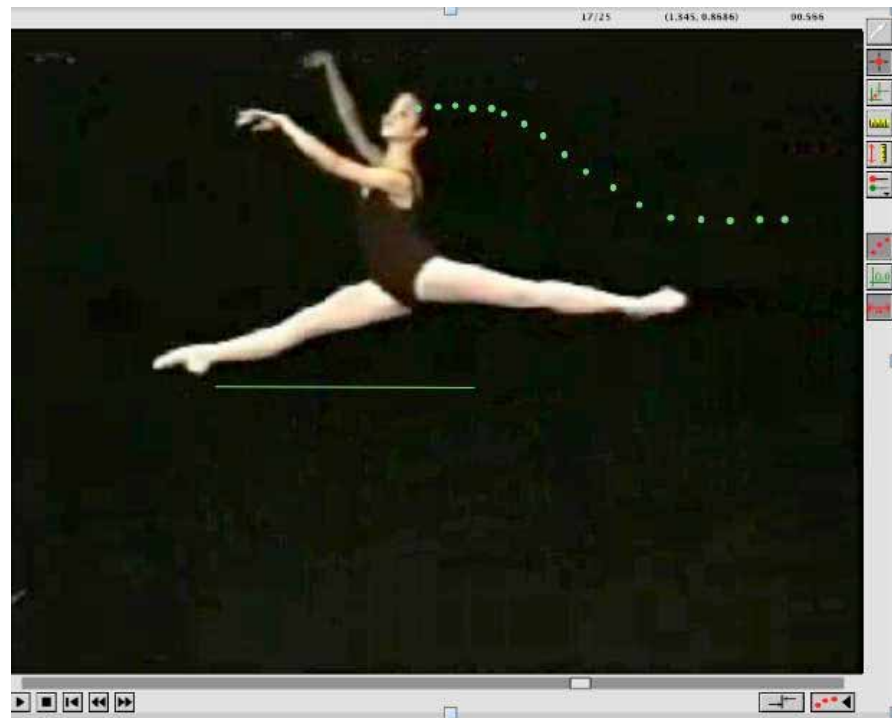
$$\Delta\vec{r}_{12} = \vec{r}(t_2) - \vec{r}(t_1)$$

$$\Delta\vec{r}_{23} = \vec{r}(t_3) - \vec{r}(t_2)$$

$$\begin{aligned}\Delta\vec{r}_{13} &= \Delta\vec{r}_{12} + \Delta\vec{r}_{23} \\ &= \vec{r}(t_2) - \vec{r}(t_1) + \vec{r}(t_3) - \vec{r}(t_2) \\ &= \vec{r}(t_3) - \vec{r}(t_1)\end{aligned}$$

# Graphing Position

- Graphs for the eye vs. graphs for the mind.
  - Describe where something is in terms of its coordinate at a given time.
- 
- Choose origin
  - Choose axes
  - Choose scale
  - Set scales on graph
  - Take data from video





# Average Velocity

- We need to keep track not only of the fact that something has moved but how long it took to get there.
- Define the average velocity by

$$\langle \vec{v} \rangle = \frac{\text{displacement}}{\text{time it took to make the displacement}}$$

$$\langle \vec{v} \rangle = \frac{\Delta \vec{r}}{\Delta t}$$

# Uniform motion

- If an object moves so that it changes its position by the same amount in each unit of time, we say it is in uniform motion.
- This means the average velocity will be the same no matter what interval of time we choose.

$$\langle \vec{v} \rangle = \frac{\Delta \vec{r}}{\Delta t} = v_0$$

$$\Delta \vec{r} = v_0 \Delta t$$

$$\vec{r}(t_2) - \vec{r}(t_1) = v_0 \Delta t$$

$$\vec{r}_{final} = \vec{r}_{initial} + v_0 \Delta t$$

