

HW#13: Sec 14.8 Problems 34, 35, 36. (No Credit)

#34. (a) $v = f \cdot \lambda$. Given $f_1 = 261.6 \text{ Hz}$, find tension F , for $L = 0.700 \text{ m}$
 $M = 4.3 \times 10^{-3} \text{ kg}$ FOR FUNDAMENTAL, $L = \lambda/2$ (b)ALSO (c) $v = \sqrt{F/\mu}$ from Eq. (13.17).[Note "fundamental" is same as first harmonic & has $n=1$ half wave lengths in L .]and mass/unit length $= \mu = M/L$. (d)
Find expression for $F =$ tension in string: substituting from (a)(b)&(d) into (c):

$$F = v^2 \mu = v^2 \frac{M}{L} = f_1^2 \lambda^2 \frac{M}{L} = f_1^2 \cdot (4L)^2 \cdot \frac{M}{L} = 4f_1^2 LM$$

& check dimension $[F] = \text{N} = \text{kg} \cdot \text{m} / \text{s}^2$ 

$$\text{Then } F = (4)(261.6)^2 \cdot (0.700)(4.3 \times 10^{-3}) \frac{\text{kg} \cdot \text{m}}{\text{s}^2} \\ = 82.39 \times 10^{-3} = \boxed{82.4 \text{ N} = F = \text{Tension}}$$

#35 Third Harmonic has $n=3$ half wavelengths within string length L
so that $L = 3\lambda_3/2$, $\lambda_3 = 2L/3$
NODS ANTINODS
(a) Then nodes (zeros of vibn) are at
 $x=0$, $x=L/3$, $x=2L/3$, $x=L$
for $L=8.00 \text{ m}$ Nodes are at $\boxed{0.00, 2.667 \text{ m}, 5.333 \text{ m} \text{ \& } 8.00 \text{ m.}}$ Maxima (or Antinodes) are half way between nodes: $x = L/6, L/2, 5L/6 =$
 $\boxed{1.33 \text{ m}, 4.00 \text{ m}, 6.67 \text{ m.}}$

$$f_3 = v/\lambda_3 = \sqrt{\frac{F}{\mu}} \cdot \frac{3}{2L}$$

$$= \sqrt{\frac{FL}{M}} \cdot \frac{3}{2L} = \frac{3}{2} \sqrt{\frac{F}{LM}}$$

$$f_3 = (1.5) \left[\frac{(49)}{(8)(0.04)} \right]^{1/2} = \boxed{18.6 \text{ Hz} = f_3}$$

2 insert $F = 49.0 \text{ N}$
 $L = 8.0 \text{ m}$
 $M = 40.0 \text{ g} = 0.04 \text{ kg}$

#36 $L = 0.70 \text{ m}$; $M = 0.300 \text{ g} = 3 \times 10^{-4} \text{ kg}$; $F = 600 \text{ N}$

[Q] find f_1, f_2, f_3 . [A] From $v = f \cdot \lambda$, we have

$$f_i = v / \lambda_i. \quad \text{Also } \lambda_{1/2} = L, \lambda_2 = L; \lambda_3 = \frac{2L}{3}$$

$$\text{and } v = \sqrt{F/M} = \sqrt{FL/M}$$



$$L = \frac{\lambda_1}{2}, \lambda_2, \frac{3}{2}\lambda_3. \quad \text{Then } f_1 = v / \lambda_1 = \sqrt{\frac{FL}{M}} \cdot \frac{1}{2L} = \sqrt{\frac{F}{ML}} \cdot \frac{1}{2}$$

$$= \frac{1690}{2} = \boxed{845 \text{ Hz} = f_1}$$

$$f_2 = \sqrt{\frac{FL}{M}} \cdot \frac{1}{L} = 2f_1 = \boxed{1690 \text{ Hz} = f_2}$$

$$f_3 = \sqrt{\frac{FL}{M}} \cdot \frac{3}{2L} = 3f_1 = \boxed{2535 \text{ Hz} = f_3}$$