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Physics 117
Quiz 5 (4/2/2003)

Use as far as possible formula and try to explain your reasoning.

- A) A cube of ice with a volume of 10 cm^3 is melted into a measuring cup. What is the volume of liquid water?

(Density of water= $D_{\text{water}}=1 \text{ gr/cm}^3$. Density of ice= $D_{\text{ice}}=0.92 \text{ gr/cm}^3$.)

The mass does not change during the melting (if you assume that no water evaporates away as a gas). The mass of ice is
 $(10 \text{ cm}^3)(.92 \text{ g/cm}^3) = 9.2 \text{ g}$.
That much water has a volume of 9.2 cm^3 .

- B) A solid block of wax has a density of 0.9 gr/cm^3 and a volume of 20 cm^3 . If the block is floating in a tank of water, what is the volume of liquid displaced?
(Density of water= $D_{\text{water}}=1 \text{ gr/cm}^3$.)

When the block is floating, the gravitational force balances the buoyant force, so the block's mass equals the mass of displaced water. The block has a mass of
 $(20 \text{ cm}^3)(.9 \text{ g/cm}^3) = 18 \text{ g}$.
18 g of water has a volume of 18 cm^3 .

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C) A plastic balloon full of air is immersed completely in ethyl alcohol. The balloon has a volume of 100 cm^3 . Calculate:

- 1) the weight of the balloon
- 2) the buoyancy force acting on the balloon
- 3) the force you have to exert on the balloon in order to keep it submerged.

($D_{\text{Balloon}} = \text{Density of air} = 0.001 \text{ gr/cm}^3$. Density of alcohol = 0.80 gr/cm^3 .)

The balloon has a mass of

$(100 \text{ cm}^3)(.001 \text{ g/cm}^3) = .1 \text{ g} = 1 \times 10^{-4} \text{ kg}$,
so it has a weight of $1 \times 10^{-3} \text{ N}$.

The displaced fluid has a mass of

$(100 \text{ cm}^3)(.80 \text{ g/cm}^3) = 80 \text{ g} = .08 \text{ kg}$,
so its weight, which equals the buoyant force, is 0.8 N .

To keep the balloon submerged, you have to push against the difference between the buoyant force and the gravitational force.

This is $.8 \text{ N}$ minus $.001 \text{ N} = .799 \text{ N}$.

Bonus Problem:

D) Two barometers are made with water and mercury, and they are both at sea level. On a normal day, the mercury column would be about 76 cm tall, but for this problem, imagine that it is 100 cm . How tall would the water column be?

(Density of water = $D_{\text{Water}} = 1 \text{ gr/cm}^3$. Density of Mercury = 13.6 gr/cm^3 .)

In these barometers, atmospheric pressure matches the pressure at the bottom of the column of liquid. That pressure is equal to the weight of fluid divided by cross-sectional area, so

$$P = F/A = (g)(\text{Density})(\text{Volume})/(\text{Area}) = (gD)(\text{height}).$$

The two barometers measure the same pressure, so

$$(D h)_{\text{water}} = (D h)_{\text{mercury}}$$

or

$$\begin{aligned} h_{\text{water}} &= h_{\text{mercury}}(D_{\text{mercury}}/D_{\text{water}}). \\ &= (100 \text{ cm})(13.6) \\ &= 13.6 \text{ m}, \end{aligned}$$

or roughly forty feet.