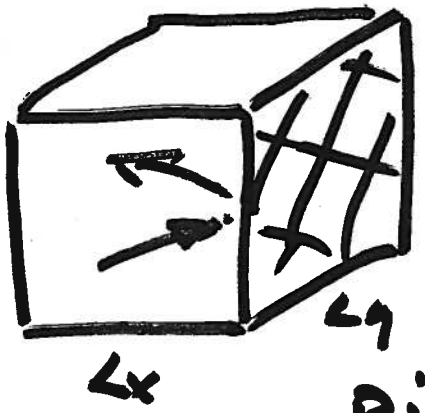


Ideal Gas Law: $PV = Nk_B T$

JERIFIN
11-19-07



COMPUTE P
of IDEAL GAS
from $F_x / L_y L_z$ on

Right Face of CUBE:

$$F_x = \sum_{i=1}^N F_{xi} = \sum_i \frac{\Delta p_{xi}}{\Delta t_i} = \sum_i \frac{2m v_{xi}}{2L_x / v_{xi}}$$

$$P = \frac{F_x}{A} = \frac{F_x}{L_y L_z} = \frac{1}{(L_x L_y L_z)} \sum_i m v_{xi}^2$$

i.e. $PV = P(L_x L_y L_z) = N \langle m v_{xi}^2 \rangle_{AVG}$
 & This MUST be $= Nk_B T$.

CONCLUDE: $k_B T \equiv \langle m v_{xi}^2 \rangle_{AVG}$

OR $\frac{3}{2} k_B T \equiv \langle \frac{3}{2} m v_{ix}^2 \rangle_{AVG}$
 $\equiv \langle KE \rangle_{AVG}$

(since $\langle 3 \cdot \frac{m}{2} v_{xi}^2 \rangle = \langle KE \rangle_{AVG}$.)

Note: EQUI-PARTITION THEOREM says:
 EACH Degree of Freedom gets $\frac{1}{2} k_B T$
 of energy in thermal EQUILIBRIUM