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2<sup>nd</sup> LAW of THERMODYNAMICS:

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increases as Heat flows from HOT to COLD;

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EQUIVALENT TO CARNOT'S STATEMENT;

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of STATE of SYSTEM.

CARNOT'S MAXIMALLY EFFICIENT  
CYCLIC HEAT ENGINE  $\Rightarrow$  2<sup>nd</sup> LAW

ACTUAL EFFICIENCY

$$\eta_{ACTUAL} = \frac{W_{NET}}{Q_{IN}} = \frac{Q_{IN} - Q_{OUT}}{Q_{IN}} = 1 - \frac{Q_{OUT}}{Q_{IN}}$$

for any ACTUAL Heat Engine  
& CARNOT proved that

CARNOT EFFICIENCY,

$$\eta_{CARNOT} = 1 - \frac{T_C}{T_H}$$

for CARNOT'S IDEALIZED Heat Engine

AND ALSO, by design of CARNOT ENGINE, that

$$\eta_{CARNOT} > \eta_{ACTUAL}$$

for any engine operating between  $T_H$  &  $T_C$

THEREFORE

$$\frac{Q_{OUT}}{Q_{IN}} > \frac{T_C}{T_H}$$

AND  $Q_{OUT} > 0$ , since  $T_C > 0$

(by 3<sup>rd</sup> LAW)

③ (EQUIVALENT!) VERSIONS  
OF 2<sup>ND</sup> LAW OF Thermodynamics

- 1) A HEAT ENGINE MUST EXHAUST HEAT.
- 2) A REFRIGERATOR MUST CONSUME WORK.
- 3) ENTROPY of a closed system  
ALWAYS INCREASES.

# CHANGE IN ENTROPY

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$$\Delta S = \sum \frac{Q_i^{IN}}{T_i} \quad \leftarrow \text{Definition of } \Delta S.$$

EG FOR  $Q$  transferred from  $T_H$

to  $T_C$

$$\Delta S = \frac{Q}{T_C} - \frac{Q}{T_H}$$

Clearly  $\Delta S > 0$  iff  $T_H > T_C$

ie  $\Delta S > 0 \iff \{Q \text{ flows from Higher to Lower } T.\}$

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ENTROPY STATEMENT IS  
EQUIVALENT TO CARNOT'S STATEMENT  
FOR HEAT ENGINE + SURROUNDINGS

$$\Delta S_{\text{UNIV.}} = \Delta S_{\text{SURE}} + \Delta S_{\text{ENGINE}}$$
$$= -\frac{Q_{\text{IN}}}{T_H} + \frac{Q_{\text{OUT}}}{T_C} + 0$$

because engine is same at end  
of cycle as at beginning.

$$\Delta S_{\text{UNIV.}} > 0 \Rightarrow \frac{Q_{\text{OUT}}}{T_C} > \frac{Q_{\text{IN}}}{T_H}$$

$$\Leftrightarrow \frac{Q_{\text{OUT}}}{Q_{\text{IN}}} > \frac{T_C}{T_H} : \text{CARNOT'S 2ND LAW}$$

$$\Delta S_{\text{UNIV.}} > 0 \Leftrightarrow Q_{\text{OUT}} > 0$$

THIRD FORM of 2nd LAW

is equivalent to 1st FORM!

# ENTROPY & PROBABILITY

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$$\text{ENTROPY } S = k (\ln W)$$

$k$  = Boltzmann's constant per molecule

$$= 1.38 \times 10^{-23} \text{ J/particle} \cdot \text{K}$$

&  $W$  = probability of macroscopic state of system.

THIS

INCREASE of ENTROPY is a process

↔ movement towards a state of higher probability.